

Lecture 15

**Doppler shift or how the
police finds you speeding
or how astronomers find
galaxies moving**

Einstein's new relativity

- Galileo:
 - The laws of mechanics are the same in all inertial frames of reference
 - time and space are the same in all inertial frames of reference
- Einstein:
 - The laws of physics are the same in all inertial frames of reference
 - the speed of light in the vacuum is the same in all inertial frames of reference

⇒ time spans and distances are relative

Consequences

- breakdown of simultaneity:
whether or not two events happen simultaneously depends on the speed at which you are moving with respect to the events
- time dilation

$$\Delta t_R = \frac{\Delta t_P}{\sqrt{1 - \frac{v^2}{c^2}}}$$

- length contraction

$$d_P = d_R \sqrt{1 - \frac{v^2}{c^2}}$$

Boost factor

- Boost factor:

$$\Gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

- time dilation: $\Delta t_R = \Gamma \times \Delta t_P$
- length contraction: $d_P = d_R / \Gamma$

This is messy, so let's clean up a bit

- **proper time**: time measured by a clock at rest with respect to a specific observer
⇒ clock at the fastest possible rate
- **proper length**: length of an object as measured in its own rest frame
⇒ largest possible length
- time and length in other inertial frames can be calculated by the so-called **Lorentz transformation** (i.e. multiplying with or dividing by the boost factor Γ)

So $c + c = c$? yes, sort of ...

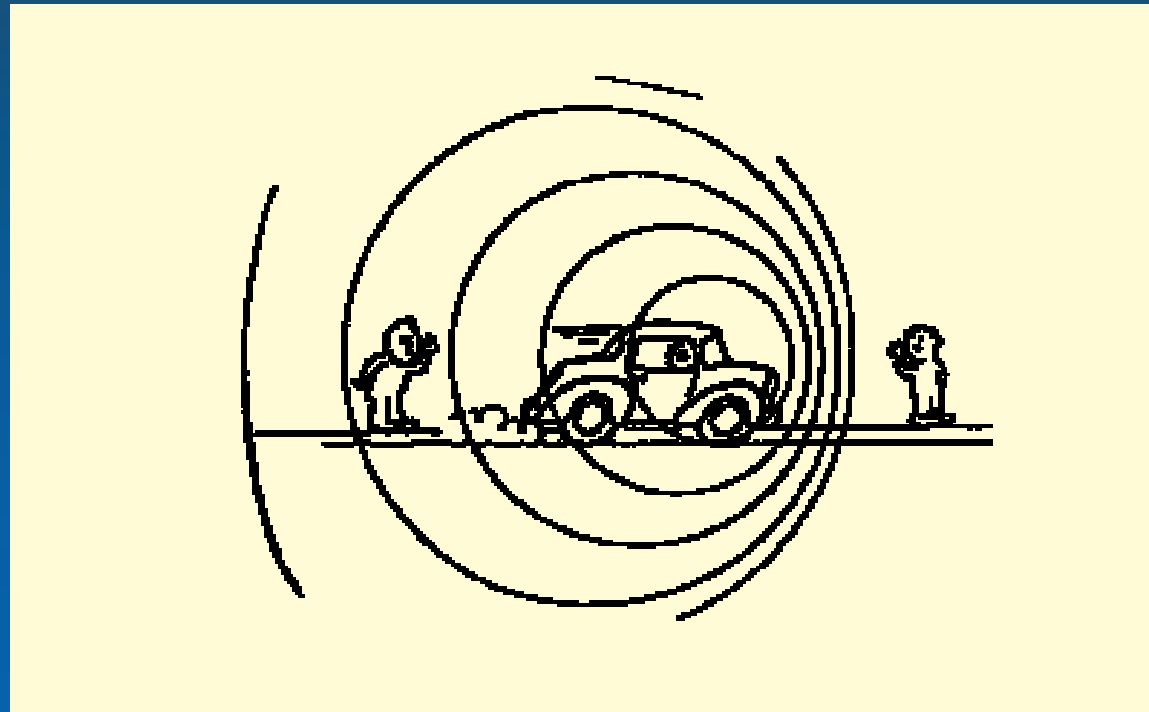
- **Q:** So how do we add velocities ?
A: by properly applying Lorentz transforms:

$$v_{tot} = \frac{v_1 + v_2}{1 + \frac{v_1 v_2}{c^2}}$$

- **Example:** shoot a torpedo ($v_2 = 0.5c$) from the Enterprise, moving at $v_1 = 0.5c$ outside observer: $v_{torpedo} = 0.8c$

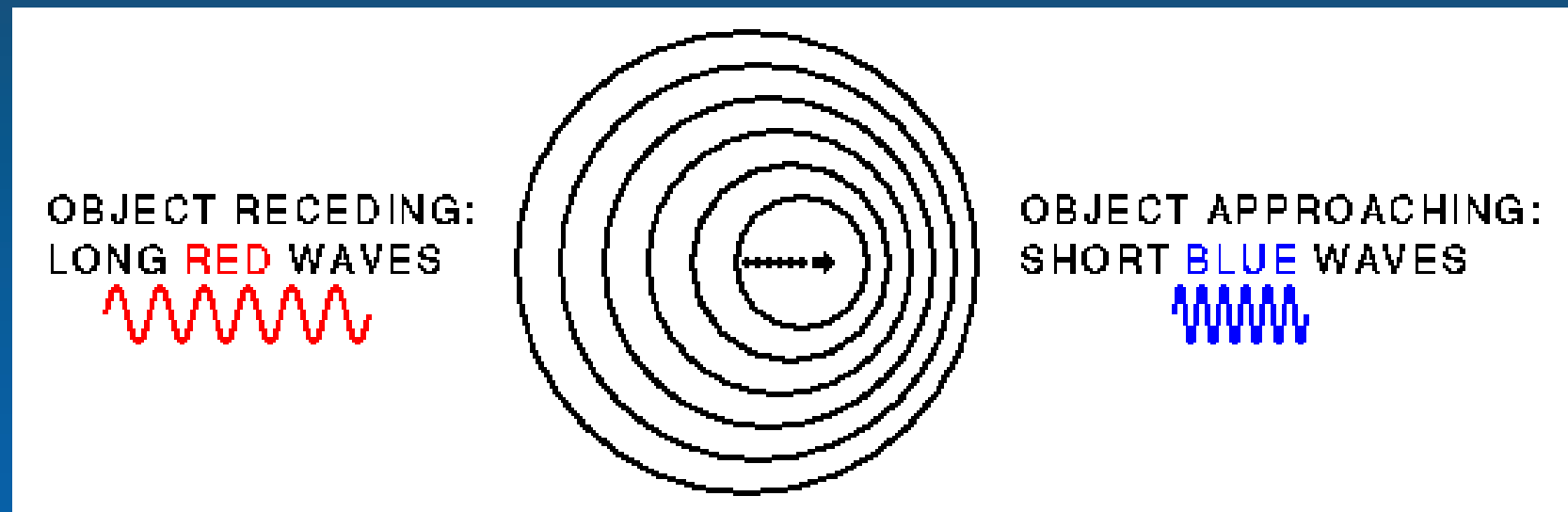
Doppler effect (for sound)

The pitch of an approaching car is higher than that of a car moving away.



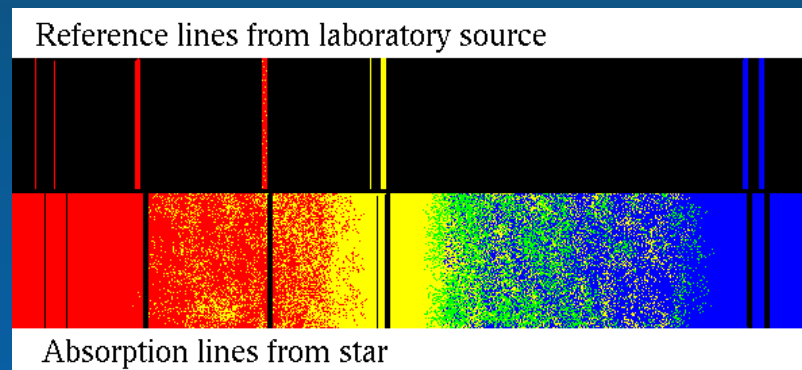
Doppler effect (for light)

The light of an approaching source is shifted to the blue, the light of a receding source is shifted to the red.

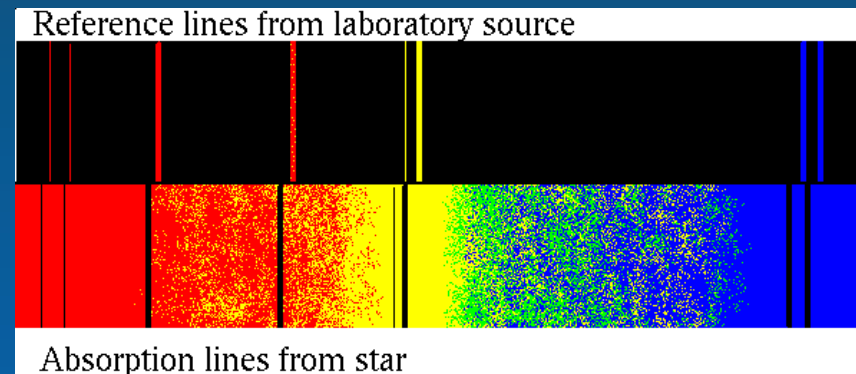


Doppler effect

The light of an approaching source is shifted to the blue, the light of a receding source is shifted to the red.



blue shift



red shift

Doppler effect

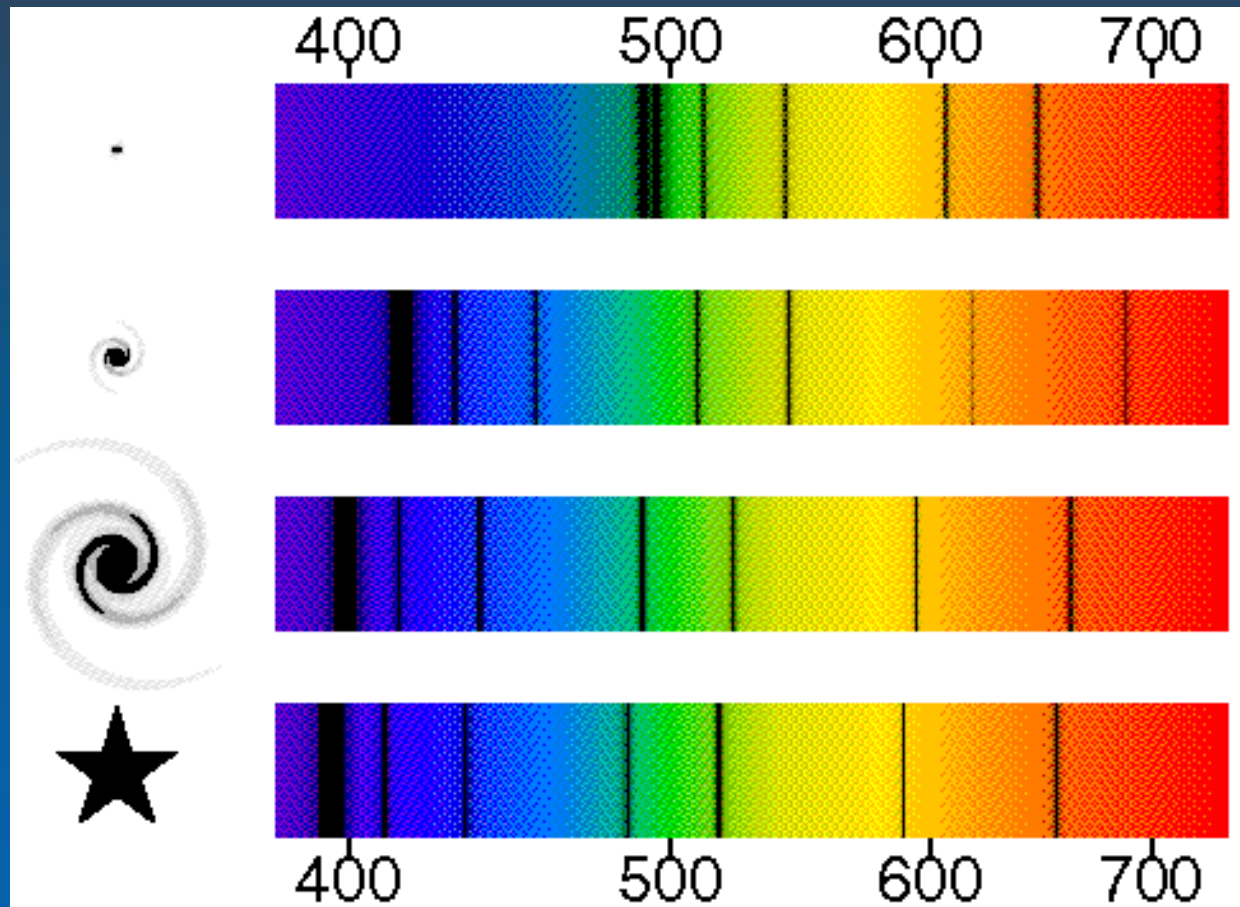
redshift:

$$1+z = \sqrt{\frac{1+v/c}{1-v/c}}$$

$z=0$: not moving

$z=2$: $v=0.8c$

$z=\infty$: $v=c$



Energy

- **Energy**: the capacity to do work
- **total energy is conserved**, i.e. it is only transformed from one form of energy into another.
 - breaks: transform energy of motion (kinetic energy) into heat
 - falling body: transform gravitational energy into kinetic energy

Energy

- Newton:

- kinetic energy: $E_{kin} = 1/2 m v^2$

- $v=0 \Rightarrow E_{kin} = 0$

- Einstein:

- $E = \Gamma m_0 c^2$

- $v=0 \Rightarrow E = m_0 c^2$ “rest energy”

- $E_{kin} = (\Gamma - 1) m_0 c^2$

- Example:

energy required to accelerate 1kg of mass to
 $v=0.87c \Rightarrow$ equivalent of 20 megatons of TNT