Linfor3D User Manual

IDL version 6.5.7

Matthias Steffen, Hans-Günter Ludwig, Sven Wedemeyer & Andrew J. Gallagher

F90 version 0.7.5

Andrew J. Gallagher & Matthias Steffen

Contents

1	Intr	oduction ————————————————————————————————————	7
	1.1	The IDL version	7
	1.2	The F90 version	7
	1.3	The differences	8
	1.4	Final word	8
2	Gett	ting started	9
_	2.1	Running the IDL version	9
	2.2	Running the F90 version	
	2.2	2.2.1 Getting a custom installation	
		2.2.1 Setting a custom instantation	
3	Basi	ic Equations of Radiative Transfer	12
	3.1	Transfer equation for the continuum intensity	12
	3.2	Transfer equation for the line intensity	13
	3.3	Transfer equation for the line depression	14
	3.4	Contribution functions	15
	3.5	Grey test case	17
4			21 21
	4.1	Reading input data	
	4.2	Writing data to file	
	4.3		21
	4.4	Computing 3D continuous opacities	
	4.5	Computing all radiative transfer	
		4.5.1 DoRT in full 3D	
			25 26
	16	4.5.3 DoRT in 1D without Curve-of-growth computations	20 27
	4.6	Limitations of Limorad with MP1	21
5	Inst	alling GDL and running Linfor3D	29
	5.1	Running Linfor3D with GDL	29
	5.2	Running Linfor3D in parallel	30
			21
6	•		31
	6.1		31
	6.2		32 32
	6.3	•	32 24
	6.4 6.5		34 35
	0.3	ryo riles	33
7	Para	ameter Input: linfor_setcmd.pro (IDL) linfor3d.setcmd (F90)	38
	7.1	F90 specific flags and settings	38
		7.1.1 outfile	38
		7.1.2 printcobold	38
		7.1.3 debug	38
		7.1.4 wr3x3	39
		7.1.5 d1_flag	39
	7.2	IDL specific flags and settings	39
		7.2.1 plt_flag	39
		7.2.2 free_flag	39
		7.2.3 ff_path	39

7.3	Program		40
	7.3.1	run_flag	40
	7.3.2	cv1_flag	41
	7.3.3		41
	7.3.4	cv3_flag	41
	7.3.5	1 - 2	11
	7.3.6	$oldsymbol{arepsilon}$	12
	7.3.7	nlte_flag	12
7.4	Genera	<mark>l paths</mark>	12
	7.4.1	abupath	12
	7.4.2	opapath	13
	7.4.3	gaspath	13
	7.4.4	eospath	13
7.5	Model	data	13
	7.5.1	context	13
	7.5.2	rhdpath	14
	7.5.3	modelid	14
	7.5.4	parfs	14
	7.5.5	xbcpath3	14
	7.5.6	xbcpathx	14
	7.5.7	xbcpath	14
	7.5.8	abuid	1 5
	7.5.9	abuidx	45
	7.5.10	dmetal	45
	7.5.11	dalpha	4 5
	7.5.12	nx_skip	46
		r	
	7.5.13	ny_skip	46
7.6	7.5.13 More n	ny_skip	46
7.6	7.5.13 More n 7.6.1	ny_skip	46 46
7.6	7.5.13 More n 7.6.1 7.6.2	ny_skip	46 46 46
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3	ny_skip	46 46 46 46
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4	ny_skip	46 46 46 46
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5	ny_skip	16 16 16 16 17
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile gasfile eosfile htau0 qmol Teff	16 16 16 16 17 17
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7	ny_skip	16 16 16 17 17 17
	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8	ny_skip	16 16 16 17 17 17
7.6	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile gasfile eosfile htau0 qmol Teff grav tsurffac data - reading of 'full' files (CO ⁵ BOLD only)	16 16 16 17 17 17 17
	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile gasfile eosfile htau0 qmol Teff grav tsurffac data - reading of 'full' files (CO ⁵ BOLD only) isnap_full_1	16 16 16 17 17 17 17 18 18
	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile	16 16 16 17 17 17 17 18 18
7.7	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile	16 16 16 17 17 17 17 18 18 18
	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile	16 16 16 17 17 17 17 18 18 18 18
7.7	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 ⟨3D⟩ m 7.8.1	ny_skip	16 16 16 17 17 17 18 18 18 19
7.7	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 ⟨3D⟩ m 7.8.1 Externa	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) 4 opafile 4 easfile 4 eosfile 4 htau0 4 qmol 4 Teff 4 grav 4 tsurffac 4 data - reading of 'full' files (CO ⁵ BOLD only) isnap_full_1 4 isnap_full_2 4 istep_full 4 ean model 4 mavg 4 Il 1D reference model 4	16 16 16 17 17 17 17 18 18 18 19 19
7.7	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) 4 opafile 4 gasfile 4 eosfile 4 htau0 4 qmol 4 Teff 4 grav 4 tsurffac 4 data - reading of 'full' files (CO ⁵ BOLD only) isnap_full_1 4 isnap_full_2 4 istep_full 4 ean model 4 mavg 4 at ID reference model 4 atmpath 4	16 16 16 17 17 17 17 18 18 19 19
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile gasfile eosfile htau0 qmol Teff grav tsurffac data - reading of 'full' files (CO ⁵ BOLD only) isnap_full_1 isnap_full_2 istep_full ean model mavg dl 1D reference model atmpath atmfile	16 16 16 17 17 17 18 18 19 19 19
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da	ny_skip nodel information (MOST read from parameter file for CO ⁵ BOLD data) opafile gasfile eosfile htau0 qmol Teff grav tsurffac data - reading of 'full' files (CO ⁵ BOLD only) isnap_full_1 isnap_full_2 istep_full ean model mavg ul 1D reference model atmpath atmfile tat and radiative transfer	16 16 16 17 17 17 18 18 19 19 19 19
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da 7.10.1	ny_skip	46 46 46 47 47 47 47 48 48 49 49 49 49 49
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da 7.10.1 7.10.2	ny_skip	16 16 16 17 17 17 17 18 18 19 19 19 19 50
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da 7.10.1 7.10.2 7.10.3	ny_skip nodel information (MOST read from parameter file for CO5BOLD data) opafile gasfile eosfile htau0 qmol Teff grav tsurffac data - reading of 'full' files (CO5BOLD only) isnap_full_1 isnap_full_2 ean model mavg ul 1D reference model atmpath atmfile ta and radiative transfer linfs lutau1 lutau2	16 16 16 17 17 17 17 18 18 19 19 19 19 19 19 19
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da 7.10.1 7.10.2 7.10.3 7.10.4	ny_skip 4 nodel information (MOST read from parameter file for CO5BOLD data) 4 opafile 4 gasfile 4 eosfile 4 htau0 4 qmol 4 Teff 4 grav 4 tsurffac 4 data - reading of 'full' files (CO5BOLD only) 4 isnap_full_1 4 isnap_full_2 4 ean model 4 mavg 4 il 1D reference model 4 atmpath 4 atmfile 4 ta and radiative transfer 5 linfs 5 lutau1 5 lutau2 5 dlutau 5	16 16 16 17 17 17 18 18 18 19 19 19 50 50
7.7 7.8 7.9	7.5.13 More n 7.6.1 7.6.2 7.6.3 7.6.4 7.6.5 7.6.6 7.6.7 7.6.8 Model 7.7.1 7.7.2 7.7.3 (3D) m 7.8.1 Externa 7.9.1 7.9.2 Line da 7.10.1 7.10.2 7.10.3 7.10.4 7.10.5	ny_skip 4 nodel information (MOST read from parameter file for CO5BOLD data) 4 opafile 4 gasfile 4 eosfile 4 htau0 4 qmol 4 Teff 4 grav 4 tsurffac 4 data - reading of 'full' files (CO5BOLD only) 4 isnap_full_1 4 isnap_full_2 4 istep_full 4 ean model 4 mavg 4 tl 1D reference model 4 atmpath 4 atmfile 4 ta and radiative transfer 5 lutau1 5 lutau2 5 dlutau 5 lctau1 5	16 16 16 17 17 17 17 18 18 19 19 19 19 19 19 19

			dletau	
		7.10.8	Hbrd	51
		7.10.9	vsini	51
		7.10.10	ximicx	51
			ximic1	
			eximic3	
			ximacx	
			ximac1	
			ximac3	
			vfacx	
			vfacy	
		7.10.18	vfacz	53
		7.10.19	micro	53
		7.10.20) xi_a	53
		7.10.21	xi_b	53
		7.10.22	xi_d	53
			dclam	
			intmode	
			intline	
	7.11		nchunk	
	7.11	_	quadrature schemes	
			ntheta	
			nphi	
			mu0	
		7.11.4	kphi	55
		7.11.5	raybase	56
	7.12	Curve-	of-Growth computations	56
		7.12.1	cog	56
				56
			gflgmin	
			gflgmax	
	7 13		cample	
			ample	
	7.14	1.90 Ex	ample	JU
8	Line	Data F	ile: line.dat	64
•	8.1			64
	0.1	8.1.1		64
		0.1.1		64
	0.0	8.1.2		
	8.2			64
		8.2.1		64
		8.2.2		65
		8.2.3	<i>'</i>	66
		8.2.4	Single line calculations, complete line data format '2'	68
		8.2.5	Single line calculations, complete line data format '3'	69
		8.2.6	Single line calculations, complete line data format '4'	70
		8.2.7		71
		8.2.8		71
		8.2.9	•	71 72
		8.2.10		72 73
	Q 2		•	74
	8.3		01	
		8.3.1		74 7.
		8.3.2	Van der Waals broadening	75

		8.3.3 8.3.4	ABO van der Waals broadening formalism			
0	Dom	oler.			• •	
9	Depa 9.1		C <mark>oefficients</mark> c file			78 78
	9.1		c2 file			
	9.2	THE XU	az me		• •	19
10	Outp	out files				80
	10.1	uio_sav	e			80
	10.2	uio_res	tore	. 		83
	10.3	Useful	UIO information			83
11	Out	out file s	tructures			85
	11.1	linfor_3	D_1.uiosave			85
		11.1.1	ABU			85
		11.1.2	ATOM	. 		85
		11.1.3	CMD	. 		85
		11.1.4	CONST			85
		11.1.5	INFO			
		11.1.6	LINE			
	11.2	linfor_3	D_2.uiosave	. . .		
			CONTF			
			IMUPHI			
			MAPS			
			RESULT			
	11.3		D_3.uiosave			
			CONTF3D			
	11.4	lintor_	X.uiosave			94
12	Plott	ting out	out			95
			g the synthesis			95
			g contribution functions			
	12.3	Plotting	g the Curve-of-Growth			97
13	Timi	ing stati	stics			98
1.4	IOM	DIC				100
14	ION					100
	14.2	14.2.1	Some definitions			
			Equations			
			Criterion for convergence			
			Initial guess			
			Variable names			
15	iono	-				107
		-				
		•				
			l			
	10.1	OSTYM	•			100

6 LIST OF TABLES

	ggas
	namj
	Ofracj
15.1	1zeta
15.1	2init
15.1	3 dm
15.1	4dalpha
15.1	5avm
15.1	6ehe
15.1	7abupath
	8nami
	9abui
	0Example
10.2	ozampe
16 iono	ppa2 113
	temp
	gin
	alam
	pe
	pg
	densnc
	okappa
	osigma
	qflg
	Onamj
	1fracj
	2zeta
	3init
	4dm
	5dalpha
16.1	6avm
16.1	7ehe
16.1	8abupath
16.1	9nami
16.2	0abui
	1Example
T • .	A T31
List o	f Figures
1	Analytical Curve-of-Growth
List o	f Tables
1	List of install options
2	List of shared routines
3	List of all structures in common blocks 'linfordata'
4	List of all IDL modules
5	List of all F90 modules
19	List of atoms
20	Small molecular network: 5 atoms, 8 molecules
21	Large molecular network: 10 atoms, 14 molecules 102

1 Introduction

Linfor3D is based on the old code LINFOR (short for LINe FORmation code). There are two versions of the code that are currently being developed side-by-side.

The first version of the code has been developed and tested from conception in IDL. This can also run on certain versions of GDL (see Sect. 5). The bulk of the heavy computations are done inside Fortran routines, which are called by the IDL code's program flow.

The second version of the code is based on the first version, but is completely written in Fortran. This version has the advantage of being faster overall for a given compiler (e.g. Intel[©] Fortran or GNU Fortran) as it is capable of running in parallel with MPI (Message Passing Interface), which is discussed later.

Like the codes themselves this user manual is under construction, too. Nevertheless, it will be of substantial help while installing and running Linfor3D, creating new command and spectral line data files for Linfor3D in either IDL or Fortran, and interpreting the output data.

To get a brief overview of how to install and run both versions of Linfor3D in their simplest forms, you should read the "Getting started" section (Sect. 2) after this brief overview of both codes.

1.1 The IDL version

Here is a short break down of the limitations of the IDL/GDL version of the code:

- **Geometry:** This version is limited to spectrum synthesis from **local hydrodynamical models** (solar-type convective atmospheres).
- Efficiency: No effort was yet taken to really improve the execution speed of this IDL/Fortran code. In fact there are still some parts in the code which are unnecessary for the current operation. Their execution should be controlled by additional flags in a future release.
- Parallel processing: The newer versions of Linfor3D (version 6.0.0 onwards) have been ported so that it runs on GDL as well as IDL. This means that parallel processing as an embarassingly parallel job is possible. See Sect. 5.2 for further information and updates. However, no effort has been made to add parallel processing in to the internal program flow of Linfor3D.

1.2 The F90 version

The Fortran version is newer, and as such has been developed to remove some of the IDL versions' limitations:

- **Geometry:** Like its IDL counterpart, this version is limited to spectrum synthesis from **local hydrodynamical models** (solar-type convective atmospheres).
- Effeciency: Efforts have been made to improve efficiency of the code's execution where possible. However, because both codes are reliant on the same modules that are resposible for the majority of the heavy computing, certain <u>deliberate</u> inefficiencies had to be included, which affect the memory usage, particularly when running in parallel. Once the two codes begin to diverge, this inefficiencies can be readdressed and improved.
- Parallel processing: The Fortran version of the code has been developed with parallelization in mind. As such, the code is parallelized over several dimensions that are automatically sorted according to a priory decided by the code (this is discussed later).

8 1 INTRODUCTION

1.3 The differences

The F90 version of Linfor3D was written so that it closely follows its IDL counterpart. This was so that both could continue to be developed together. As such, the more computationally expensive parts of Linfor3D are still called by both versions. One reason behind this is so that bugs can be more easily found and fixed. Another reason is that it is important to have a working code and a reference while efforts are made to include new state-of-the-art physics, which is always in consideration.

At the moment there are some small differences in the behaviour of the two versions:

- 1. **Installing:** The methods of installing the two codes differ slightly. The F90 version of the code as a script install that will deal with most machine-dependent issues this version may face. The IDL version is installed from a more traditional Makefile (see Sect 2).
- 2. **Parallelization:** While it is possible to run the IDL version of Linfor3D using an "*embarrasingly parallel*" approach (although mostly through GDL because of licensing concerns, see Sect. 5), this version of Linfor3D remains an inherently serial code. The F90 version was written to use with MPI in mind (see Sect. 4).
- 3. **Memory:** The F90 version of the code will use somewhat more memory during its execution than the IDL counterpart, which is increased with increasing CPU numbers. This is because the F90 version of the code must load all data in to memory before it computes any radiate transfer. This is so it can parallelize these computations. The code was designed to run on large cluster machines in this mode. The IDL version only loads a single atmosphere to memory at a time and executes the program flow sequentially. The F90 version will follow the same operation if only one CPU is used.
- 4. **Program flow information:** You will notice as you experiment with Linfor3D that information that is printed to screen is quite dynamic, especially in the new F90 verion of the code. This is so that the screen or a file is not overwhelmed with trivial information, or in the case of the F90 version, the same print outs on every CPU. This version can also print much more detailed information about the input data when CO⁵BOLD models are provided.
- 5. **Plotting:** The IDL version of Linfor3D can be used to plot output in several ways depending on how one sets up the parameter file (see Sect. 7). The F90 version does not do this. In all likelyhood, this will not be a feature of this code.

1.4 Final word

It is important to stress that while the two codes will eventually deviate so much that the IDL version is deprecated, the main objective to any and all development has always been user friendlyness. All post-process libraries available to the community should continue to work in the same way, and there are no plans to ever change this.

2 Getting started

This section deals with installing and executing the simplest form of Linfor3D.

WARNING: No efforts have been made to compile nor test Linfor3D in Apple OSX[©]. As such, we can offer **no** support for those that attempt to run Linfor3D on this OS.

2.1 Running the IDL version

First make sure that you have all files which are listed in Tables 4 and ??. These files should be put together in a directory which can be accessed under IDL (or GDL using versions 6.0.0 onwards).

The routines responsible for the most computationally expensive parts of Linfor3D are called as external Fortran routines by linfor_3D_ionopa.pro and linfor_dort.pro. In order to properly run Linfor3D, the Linux path variable \$IDL_SO should be defined. After unpacking Linfor3D, create a new sub-directory within the directory tree called bin, then define IDL_SO:

```
> export IDL_SO=<LINFOR_DIRECTORY>/bin/
```

This needs to be added to your Linux login script to be consistently defined by your Linux OS.

Next you need to compile the Fortran libraries dort_idl.so and ionopa2_idl.so. The source code and Makefiles are located inside the xmono directory. By default, the libraries are compiled using the Intel[©] Fortran, IFORT, compilers as the Makefile is linked to Makefile_ifort. One can change the link to any other Makefile in the directory. To compile simply enter the following command:

> make

If the shell variable \$IDL_SO is properly defined, the two libraries should compile and be moved to the bin sub-directory. If the compilation fails, please check this variable and that the directory it points to exists and the compiler selected is available on your machine.

Now two files have to be edited and provided in order to run Linfor3D:

• linfor_setcmd.pro:

This file, which is an IDL script, defines the data structure cmd. This structure contains all necessary information (except for spectral line data) like, e.g., paths and names of model file(s). See Sect. 7 for more details.

• line.dat:

This file contains all data for spectral line such as, e.g., oscillator strength and broadening parameters. The usual file name is line.dat but it might be given another name which then has be to entered in linfor_setcmd.pro. For a quick execution, examples of these line files in every file format (see Sect. 8 for details on these formats) are supplied within the directory tree under the Data subdirectory.

Finally, all IDL/GDL versions of Linfor3D require the "Universal Input Output" (UIO) IDL routine library (written by B. Freytag) for I/O related to CO⁵BOLD files, and version 6.0.0 onwards requires them for ALL I/O done during its execution.

This directory must be defined in the \$IDL_PATH either in one's BASH script or an IDL starup script. After doing so, you can run Linfor3D by starting IDL or GDL (see Sect. 5) and type:

```
IDL> .r linfor_3D.pro
```

10 2 GETTING STARTED

Several output files are created. It is possible to load these files in IDL or GDL. See Sect. 10 for more details.

Normally, one uses a bespoke linfor_setcmd.pro file in a directory of their choosing. If this is the case then one must start IDL or GDL in the proper sub-directory and then type the following:

```
IDL> common linfordata, info, cmd, const, atom, abu, line, gas, eos, result
IDL> .com bespoke_linfor_setcmd.pro
% Compiled module: LINFOR_SETCMD.
IDL> .r linfor_3D.pro
```

One of the most efficient ways to run Linfor3D is to create an IDL/GDL wrapper around one's bespoke setcmd program, as the following example depicts:

```
common linfordata, info, cmd, const, atom, abu, line, gas, eos, result
outfile = 'output.uiosave'
.compile bespoke_linfor_setcmd.pro
.run linfor_3D.pro
if keyword_set(cmd.cc3d_flag) then $
uio_save, filename = outfile, /verbose, $
info, cmd, const, atom, abu, line, result, maps, imuphi, contf, contf3d $
else $
uio_save, filename = outfile, /verbose, $
info, cmd, const, atom, abu, line, result, maps, imuphi, contf
exit
```

This runs the bespoke Linfor3D script and saves the entire output as a tailored save file, as well as the default uiosave files usually output by Linfor3D that splits the contents of the structures mostly defined in linfordata.

A brief description of the changes made for all Linfor3D releases (up to the version you are running) is given in readme_<version> given in the top directory of your Linfor3D installation.

2.2 Running the F90 version

The f90/ subdirectory contains all modules necessary to compile Linfor3D. Currently, the code will compile using the GNU OpenMPI and Intel[©] parellel studios X MPI Fortran compilers; mpifort, mpif90, mpiifort, respectively. The Intel[©] compiler must be newer than the 2017 version. If one wishes to use the Intel[©] compiler suite, we highly recommend that the user install the latest version, which is available to most linux and UNIX-based systems via Intel[©] oneAPI. The instructions for downloading and installing Intel[©] oneAPI can be found in this link. The install file – install – will expect one of these compilers on your machine so that it can compile Linfor3D. By default it will look for the faster Intel[©] compilers first. One can also force the install script to use a particular compiler using the install –c <compiler name> option. If it cannot find any compiler the script will exit. No efforts have been made to compile this code on the Apple[©] OSX.

Installation is similar to installing CO⁵BOLD:

> install

The install file is used to create a bespoke Makefile then that is used to compile the code using all available CPUs. Several architecture-defined IO related flags¹ that should be defined by the computer Linfor3D is installed on.

¹The I0 framework UIO – written and developed by B. Freytag – requires bespoke compiler flags to properly extract information from the binary UIO formatted input files.

Once properly compiled create a new working directory, copy or link the executable to this directory and copy linfor3d.setcmd from Data/. Edit this file so that all input files and directories can be found. This file is extremely similar to linfor_setcmd.pro discussed above in Sect. 2.1.

The code can be executed with the following command:

> ./linfor3d.x

Unlike its IDL companion, the F90 version of Linfor3D is capable of executing on multiple CPUs. To run the same set up on multiple CPUs one must execute the code with the following command:

```
> mpirun -np <NCPU> linfor3d.x
```

where NCPU is the number of CPUs requested by the user at execution. The parallelization module will then use this to parallelize the job over the number of CPUs allocated by the user.

If you wish to compile a fresh copy of Linfor3D type:

> make fresh

To remove all compiled modules and objects while leaving the module links and Linfor3D executable type:

> make clean

To uninstall Linfor3D simply type:

> make uninstall

This will completely remove all compiled objects and modules, and also remove the Makefile itself. One can the install once again as before using the install file.

2.2.1 Getting a custom installation

In addition to the basic installation illustrated in Sect. 2.2, install can also install a more custom version of Linfor3D using the options now tabulated.

Command	Description
install -h	Returns the complete help guide to terminal. No code is compiled.
install -d	Compiles Linfor3D with some useful debug options. Will stop all optimization.
	Not recommended for normal use.
install -m	Compiles the code without using the F90-only dort_module module flags, es-
	sentially compiling the same version of dort.f90 as is compiled for use with the
	IDL version of the code. Not recommend.
install -D	Compiles Linfor3D with a large amount of debug options, including all warnings.
	For use only for development. Not recommended for normal use.
install -c <arg></arg>	Compiles Linfor3D with a user specified compiler.
install -s	Will compile the Makefile on a single CPU. Normally install looks at the machine
	architecture and makes the install on as many CPUs as possible to speed up the
	compilation time.
install -1 <arg></arg>	The default Makefile created by install links the default location of xmono direc-
	tory to the Linfor3D directory tree. This option uses the directory expressed in
	<arg> instead.</arg>
install -x <arg></arg>	The Makefile created calls the executable linfor3d.x as standard. This option
	changes the executable name to what is expressed inside <arg>.</arg>

Table 1: A list of options that can be included in install to create a custom Linfor3D compilation.

3 Basic Equations of Radiative Transfer

3.1 Transfer equation for the continuum intensity

$$\frac{\mathrm{d}I_{\lambda}^{c}}{\mathrm{d}s} = -\kappa_{\lambda}^{c}I_{\lambda}^{c} + \kappa_{\lambda}^{c}S_{\lambda}^{c} \tag{1}$$

together with the definition of the optical depth along the ray

$$d\tau_{\lambda}^{c} = -\kappa_{\lambda}^{c} ds, \qquad (2)$$

reads

$$\frac{\mathrm{d}\,I_{\lambda}^{c}}{\mathrm{d}\,\tau_{\lambda}^{c}} = I_{\lambda}^{c} - S_{\lambda}^{c}.\tag{3}$$

The solution of Eq. (3) is

$$I_{\lambda}^{c}(\tau_{\lambda}^{c}) = \int_{\tau_{\lambda}^{c}}^{\tau_{\lambda}^{b}} S_{\lambda}^{c}(\tau') \exp\{-(\tau' - \tau_{\lambda}^{c})\} d\tau' + I_{\lambda}^{c}(\tau_{\lambda}^{b}) \exp\{-(\tau_{\lambda}^{b} - \tau_{\lambda}^{c})\}$$

$$\tag{4}$$

where τ_{λ}^{b} is the continuum optical depth at the lower boundary. The **emergent** continuum intensity is:

$$I_{\lambda}^{c}(\tau_{\lambda}^{c}=0) = \int_{0}^{\tau_{\lambda}^{b}} S_{\lambda}^{c}(\tau') \exp\{-\tau'\} d\tau' + I_{\lambda}^{c}(\tau_{\lambda}^{b}) \exp\{-\tau_{\lambda}^{b}\}.$$
 (5)

Defining

$$u_{\lambda}^{c} = I_{\lambda}^{c} - S_{\lambda}^{c} \tag{6}$$

we have the transport equation

$$\frac{\mathrm{d}\,u_{\lambda}^{c}}{\mathrm{d}\,\tau_{\lambda}^{c}} = u_{\lambda}^{c} - \frac{\mathrm{d}\,S_{\lambda}^{c}}{\mathrm{d}\,\tau_{\lambda}^{c}}\,.\tag{7}$$

The solution for u_{λ}^{c} is found by replacing S_{λ}^{c} by $dS_{\lambda}^{c}/d\tau_{\lambda}^{c}$ in Eq.(4):

$$u_{\lambda}^{c}(\tau_{\lambda}^{c}) = \int_{\tau_{\lambda}^{c}}^{\tau_{\lambda}^{c}} \frac{\mathrm{d} S_{\lambda}^{c}(\tau')}{\mathrm{d} \tau_{\lambda}^{c}} \exp\{-(\tau' - \tau_{\lambda}^{c})\} \,\mathrm{d} \tau' + u_{\lambda}^{c}(\tau_{\lambda}^{b}) \exp\{-(\tau_{\lambda}^{b} - \tau_{\lambda}^{c})\}$$
(8)

The emergent intensity can also be obtained from Eq.(8):

$$I_{\lambda}^{c}(\tau_{\lambda}^{c}=0) = S_{\lambda}^{c}(\tau_{\lambda}^{c}=0) + \int_{0}^{\tau_{\lambda}^{b}} \frac{\mathrm{d}S_{\lambda}^{c}(\tau')}{\mathrm{d}\tau_{\lambda}^{c}} \exp\{-\tau'\} \,\mathrm{d}\tau' + u_{\lambda}^{c}(\tau_{\lambda}^{b}) \exp\{-\tau_{\lambda}^{b}\}. \tag{9}$$

Now we define a fixed central wavelength, λ_0 , with the corresponding **fixed** (universal) optical depth scale τ_0 , which is equidistant in $\log \tau_0$ and may used alternatively for all integrations. On this optical depth scale, Eq.(4) becomes

$$I_{\lambda}^{c}(\tau_{0}) = \int_{\tau_{0}}^{\tau_{0}^{b}} \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} S_{\lambda}^{c}(\tau_{0}^{\prime}) \exp\{-\left(\tau_{\lambda}^{c}(\tau_{0}^{\prime}) - \tau_{\lambda}^{c}(\tau_{0})\right)\} d\tau_{0}^{\prime} + I_{\lambda}^{c}(\tau_{0}^{b}) \exp\{-\left(\tau_{\lambda}^{c}(\tau_{0}^{b}) - \tau_{\lambda}^{c}(\tau_{0})\right)\},$$
 (10)

giving the continuum intensity at wavelength λ as a function of optical depth τ_0 . Note the factor $\kappa_{\lambda}^c/\kappa_0^c$ under the integral. The intensity at the lower boundary, $I_{\lambda}^c(\tau_0^b)$, can be computed from the diffusion approximation,

$$I_{\lambda}^{c}(\tau_{0}^{b}) = S_{\lambda}^{c}(\tau_{0}^{b}) + \frac{\kappa_{0}^{c}}{\kappa_{\lambda}^{c}} \frac{\mathrm{d} S_{\lambda}^{c}}{\mathrm{d} \tau_{0}}(\tau_{0}^{b}), \tag{11}$$

but the boundary term may also be neglected, at least for the emergent intensity, because the exponential factor is usually very small. For the **emergent** intensity we have from Eq.(5):

$$I_{\lambda}^{c}(\tau_{0}=0) = \int_{0}^{\tau_{0}^{b}} \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} S_{\lambda}^{c}(\tau_{0}^{\prime}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{\prime})\} d\tau_{0}^{\prime} + I_{\lambda}^{c}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{b})\}.$$
 (12)

Similarly, Eq.(8) becomes

$$u_{\lambda}^{c}(\tau_{0}) = \int_{\tau_{0}}^{\tau_{0}^{b}} \frac{\mathrm{d} S_{\lambda}^{c}}{\mathrm{d} \tau_{0}}(\tau_{0}^{c}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{c}) - \tau_{\lambda}^{c}(\tau_{0})\} \,\mathrm{d} \tau_{0}^{c} + u_{\lambda}^{c}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{b}) - \tau_{\lambda}^{c}(\tau_{0})\}. \tag{13}$$

Note the absence of the factor $\kappa_{\lambda}^{c}/\kappa_{0}^{c}$ under the integral in this case. $u_{\lambda}^{c}(\tau_{0}^{b})$ is obtained from the diffusion approximation,

$$u_{\lambda}^{c}(\tau_{0}^{b}) = \frac{\kappa_{0}^{c}}{\kappa_{\lambda}^{c}} \frac{\mathrm{d} S_{\lambda}^{c}}{\mathrm{d} \tau_{0}}(\tau_{0}^{b}). \tag{14}$$

The emergent intensity can be computed from Eq.(13) as:

$$I_{\lambda}^{c}(\tau_{0}=0) = S_{\lambda}^{c}(\tau_{0}=0) + \int_{0}^{\tau_{0}^{b}} \frac{\mathrm{d}S_{\lambda}^{c}}{\mathrm{d}\tau_{0}}(\tau_{0}^{\prime}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{\prime})\} \,\mathrm{d}\tau_{0}^{\prime} + u_{\lambda}^{c}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}^{c}(\tau_{0}^{b})\}. \tag{15}$$

In the latest version of Linfor3D, the continuum intensity is calculated from Eqs.(8) and (9), at 3 different wavelengths: $\lambda_0 - \Delta \lambda$, λ_0 , and $\lambda_0 + \Delta \lambda$, where $\Delta \lambda$ is specified by the parameter dclam. We ensure that the derivative d $S_0^2/d\tau_0$ fulfills the condition

$$\int_{\tau_{\lambda}}^{\tau_{2}} \frac{\mathrm{d} S_{\lambda}^{c}}{\mathrm{d} \tau_{\lambda}} (\tau_{\lambda}^{\prime}) \, \mathrm{d} \tau_{\lambda}^{\prime} = S_{\lambda}^{c}(\tau_{2}) - S_{\lambda}^{c}(\tau_{1}). \tag{16}$$

The reason for using Eqs.(8) and (9) instead of Eq.(5) is that the quantity $u_{\lambda}^{c}(\tau)$ is needed to compute the line depression source function (see Sect. 3.3). We have checked that the usual transfer equation, Eq.(5), gives numerically very closely the same results for the emergent continuum intensity as Eq.(9).

3.2 Transfer equation for the line intensity

In the presence of lines, the transfer equation at wavelength λ reads

$$\frac{\mathrm{d}I_{\lambda}^{\ell}}{\mathrm{d}s} = -\left(\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}\right) I_{\lambda}^{\ell} + \kappa_{\lambda}^{c} S_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell} S_{\lambda}^{\ell}. \tag{17}$$

The line source functions S_{λ}^{ℓ} may be different from the LTE continuum source function S_{λ}^{c} . With the definition of the total optical depth

$$d\tau_{\lambda} = -\left(\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}\right) ds \equiv d\tau_{\lambda}^{c} + d\tau_{\lambda}^{\ell}, \qquad (18)$$

and the total source function

$$S_{\lambda} = \frac{\kappa_{\lambda}^{c} S_{\lambda}^{c}}{\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}} + \frac{\sum_{\ell} \kappa_{\lambda}^{\ell} S_{\lambda}^{\ell}}{\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}} = \frac{S_{\lambda}^{c} + \eta \overline{S_{\lambda}^{\ell}}}{1 + \eta} = \frac{1 + \beta}{1 + \eta} S_{\lambda}^{c}, \tag{19}$$

where

$$\overline{S_{\lambda}^{\ell}} = \frac{\sum_{\ell} \kappa_{\lambda}^{\ell} S_{\lambda}^{\ell}}{\sum_{\ell} \kappa_{\lambda}^{\ell}}, \quad \eta = \frac{\sum_{\ell} \kappa_{\lambda}^{\ell}}{\kappa_{\lambda}^{c}}, \quad \beta = \frac{\sum_{\ell} \kappa_{\lambda}^{\ell} S_{\lambda}^{\ell}}{\kappa_{\lambda}^{c} S_{\lambda}^{c}}, \quad (20)$$

we can write

$$\frac{\mathrm{d}I_{\lambda}^{\ell}}{\mathrm{d}\tau_{\lambda}} = I_{\lambda}^{\ell} - S_{\lambda}. \tag{21}$$

In LTE, $S_{\lambda} = S_{\lambda}^{c}$. The solution of Eq.(21) is

$$I_{\lambda}^{\ell}(\tau_{\lambda} = 0) = \int_{0}^{\tau_{\lambda}^{h}} S_{\lambda}(\tau_{\lambda}^{\prime}) \exp\{-\tau_{\lambda}^{\prime}\} d\tau_{\lambda}^{\prime} + I_{\lambda}^{\ell}(\tau_{\lambda}^{b}) \exp\{-\tau_{\lambda}^{b}\}.$$
 (22)

In analogy to Eq.(12), we can also obtain the emergent line intensity by integration on the universal optical depth scale τ_0 :

$$I_{\lambda}^{\ell}(\tau_{0}=0) = \int_{0}^{\tau_{0}^{b}} \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} (1+\eta) S_{\lambda}(\tau_{0}^{\prime}) \exp\{-\tau_{\lambda}(\tau_{0}^{\prime})\} d\tau_{0}^{\prime} + I_{\lambda}^{\ell}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}(\tau_{0}^{b})\},$$
 (23)

or, substituting S_{λ} from Eq.(19),

$$I_{\lambda}^{\ell}(\tau_{0}=0) = \int_{0}^{\tau_{0}^{b}} \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} (1+\beta) S_{\lambda}^{c}(\tau_{0}^{\prime}) \exp\{-\tau_{\lambda}(\tau_{0}^{\prime})\} d\tau_{0}^{\prime} + I_{\lambda}^{\ell}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}(\tau_{0}^{b})\}.$$
 (24)

Integration on the $\log \tau_0$ scale $(z_0 \equiv \log \tau_0)$ gives:

$$I_{\lambda}^{\ell}(z_{0}^{a}) = \int_{z_{0}^{a}}^{z_{0}^{b}} \ln(10) \, \tau_{0}(z_{0}^{\prime}) \, \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} (1 + \beta) \, S_{\lambda}^{c}(z_{0}^{\prime}) \, \exp\{-\tau_{\lambda}(z_{0}^{\prime})\} \, \mathrm{d} \, z_{0}^{\prime} + I_{\lambda}^{\ell}(z_{0}^{b}) \, \exp\{-\tau_{\lambda}(z_{0}^{b})\}, \tag{25}$$

where z_0^a is the minimum log optical depth. Alternatively, in analogy to Eq.(9) we obtain:

$$I_{\lambda}^{\ell}(\tau_{\lambda} = 0) = S_{\lambda}(\tau_{\lambda} = 0) + \int_{0}^{\tau_{\lambda}^{b}} \frac{\mathrm{d}S_{\lambda}}{\mathrm{d}\tau_{\lambda}}(\tau_{\lambda}^{\prime}) \exp\{-\tau_{\lambda}^{\prime}\} \,\mathrm{d}\tau_{\lambda}^{\prime} + u_{\lambda}^{\ell}(\tau_{\lambda}^{b}) \exp\{-\tau_{\lambda}^{b}\}, \tag{26}$$

where we have defined

$$u_{\lambda}^{\ell} = I_{\lambda}^{\ell} - S_{\lambda}, \tag{27}$$

which in the diffusion approximation may be written as

$$u_{\lambda}^{\ell}(\tau_{\lambda}^{b}) = \frac{\mathrm{d} S_{\lambda}}{\mathrm{d} \tau_{\lambda}}(\tau_{\lambda}^{b}) \quad \text{or} \quad u_{\lambda}^{\ell}(\tau_{0}^{b}) = \frac{\kappa_{0}^{c}/\kappa_{\lambda}^{c}}{1+\eta} \frac{\mathrm{d} S_{\lambda}}{\mathrm{d} \tau_{0}}(\tau_{0}^{b}). \tag{28}$$

On the universal optical depth scale τ_0 we obtain from Eq.(26:

$$I_{\lambda}^{\ell}(\tau_{0}=0) = S_{\lambda}(\tau_{0}=0) + \int_{0}^{\tau_{0}^{b}} \frac{\mathrm{d}S_{\lambda}}{\mathrm{d}\tau_{0}}(\tau_{0}^{\prime}) \exp\{-\tau_{\lambda}(\tau_{0}^{\prime})\} \,\mathrm{d}\tau_{0}^{\prime} + u_{\lambda}^{\ell}(\tau_{0}^{b}) \exp\{-\tau_{\lambda}(\tau_{0}^{b})\}, \tag{29}$$

In LTE, where $S_{\lambda} = S_{\lambda}^{c}$, the integral in Eq.(29) differs from the integral in Eq.(15) only by the exponential factor which involves the total optical depth τ_{λ} instead of the continuum optical depth τ_{λ}^{c} . The absolute line depression is then calculated as

$$D_{\lambda} = I_{\lambda}^{c}(\tau = 0) - I_{\lambda}^{\ell}(\tau = 0). \tag{30}$$

In the current version of Linfor3D, Eq.(25) is used if the parameter intline is set to -1, and Eq.(26) is used if intline is set to -2.

3.3 Transfer equation for the line depression

We may analyse the transfer equation for the absolute line depression defined in Eq.(30):

$$\frac{\mathrm{d}D_{\lambda}}{\mathrm{d}s} = \frac{\mathrm{d}I_{\lambda}^{c}}{\mathrm{d}s} - \frac{\mathrm{d}I_{\lambda}^{\ell}}{\mathrm{d}s} = -\kappa_{\lambda}^{c}I_{\lambda}^{c} + \left(\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}\right)I_{\lambda}^{\ell} - \sum_{\ell} \kappa_{\lambda}^{\ell}S_{\lambda}^{\ell}$$
(31)

or

$$\frac{\mathrm{d}D_{\lambda}}{\mathrm{d}s} = -\left(\kappa_{\lambda}^{c} + \sum_{\ell} \kappa_{\lambda}^{\ell}\right) D_{\lambda} + \left(I_{\lambda}^{c} \sum_{\ell} \kappa_{\lambda}^{\ell} - \sum_{\ell} \kappa_{\lambda}^{\ell} S_{\lambda}^{\ell}\right)$$
(32)

or

$$\frac{\mathrm{d}D_{\lambda}}{\mathrm{d}\tau_{\lambda}} = D_{\lambda} - S_{\lambda}^{D},\tag{33}$$

where the line depression source function is

$$S_{\lambda}^{D} = \frac{\eta}{1+\eta} \left(I_{\lambda}^{c} - \overline{S_{\lambda}^{\ell}} \right) = \frac{\eta}{1+\eta} \left((I_{\lambda}^{c} - S_{\lambda}^{c}) + (S_{\lambda}^{c} - \overline{S_{\lambda}^{\ell}}) \right). \tag{34}$$

In LTE, $\overline{S_{\lambda}^{\ell}} = S_{\lambda}^{c}$, and

$$S_{\lambda}^{D} = \frac{\eta}{1+\eta} \left(I_{\lambda}^{c} - S_{\lambda}^{c} \right). \tag{35}$$

The solution of Eq.(33) is

$$D_{\lambda}(\tau_{\lambda} = 0) = \int_{0}^{\tau_{\lambda}^{b}} S_{\lambda}^{D}(\tau_{\lambda}') \exp\{-\tau_{\lambda}'\} d\tau_{\lambda}', \tag{36}$$

neglecting the boundary term. Integration on the fixed τ_0 scale:

$$D_{\lambda}(\tau_0 = 0) = \int_0^{\tau_0^b} \frac{\kappa_{\lambda}^c}{\kappa_0^c} (1 + \eta) S_{\lambda}^D(\tau_0') \exp\{-\tau_{\lambda}(\tau_0')\} d\tau_0'.$$
 (37)

Substituting S_{λ}^{D} from Eq.(34) gives

$$D_{\lambda}(\tau_0 = 0) = \int_0^{\tau_0^b} \frac{\kappa_{\lambda}^c}{\kappa_0^c} \eta \left(I_{\lambda}^c - \overline{S_{\lambda}^{\ell}} \right) \exp\{-\tau_{\lambda}(\tau_0')\} d\tau_0', \tag{38}$$

where κ_{λ}^c , κ_0^c , η , I_{λ}^c , $\overline{S_{\lambda}^{\ell}}$, and τ_{λ} are defined as a function of τ_0 . We can also write

$$D_{\lambda}(\tau_0 = 0) = \int_0^{\tau_0^b} \frac{\kappa_{\lambda}^c}{\kappa_0^c} \eta \left(u_{\lambda}^c + (S_{\lambda}^c - \overline{S_{\lambda}^\ell}) \right) \exp\{-\tau_{\lambda}(\tau_0')\} d\tau_0', \tag{39}$$

where

$$\frac{\eta}{1+\eta} \left(S_{\lambda}^{c} - \overline{S_{\lambda}^{\ell}} \right) = S_{\lambda}^{c} \frac{(\eta - \beta)}{1+\eta} \tag{40}$$

is the NLTE correction to the line depression source function. Integration on the $\log \tau_0$ scale ($z_0 \equiv \log \tau_0$) gives:

$$D_{\lambda}(z_0^a) = \int_{z_0^a}^{z_0^b} \ln(10) \, \tau_0(z_0') \, \frac{\kappa_{\lambda}^c}{\kappa_0^c} \, \eta \, \left(u_{\lambda}^c + (S_{\lambda}^c - \overline{S_{\lambda}^\ell}) \right) \exp\{-\tau_{\lambda}(z_0')\} \, \mathrm{d} \, z_0' \,. \tag{41}$$

In the current version of Linfor3D, Eq.(41) is used to compute the line depression if the parameter intline is set to 1, while Eq.(36) is used if intline = 2.

3.4 Contribution functions

The <u>Continuum Intensity Contribution Function</u> for a ray with inclination angle $\mu = \cos \theta$, azimuthal angle ϕ , and wavelength λ is simply the horizontal average of the integrand of Eq.(12)

$$C_I^c(\tau_0, \mu, \phi, \lambda) = \frac{1}{\mu} \left\langle \frac{\kappa_{\lambda}^c}{\kappa_0^c} S_{\lambda}^c(\tau_0/\mu) \exp\{-\tau_{\lambda}^c(\tau_0/\mu)\} \right\rangle_{x,y}, \tag{42}$$

such that

$$I_{\lambda}^{c}(\tau_{0}=0,\mu,\phi,\lambda) = \int_{0}^{\tau_{0}^{b}} C_{I}^{c}(\tau_{0}',\mu,\phi,\lambda) \,\mathrm{d}\,\tau_{0}' = \int_{0}^{z_{0}^{b}} \ln(10)\,\tau_{0}(z_{0}')\,C_{I}^{c}(\tau_{0}(z_{0}'),\mu,\phi,\lambda) \,\mathrm{d}\,z_{0}' \,. \tag{43}$$

Note that now (τ_0/μ) is the optical depth along the line-of-sight, and τ_0 is the corresponding vertical optical depth (a formal quantity in the presence of horizontal inhomogeneities).

The Continuum Flux Contribution Function at wavelength λ is consequently

$$C_F^c(\tau_0, \lambda) = \int_0^{2\pi} \int_0^1 \mu' \, C_I^c(\tau_0, \mu', \phi', \lambda) \, \mathrm{d}\mu' \, \mathrm{d}\phi' \,, \tag{44}$$

such that

$$F_{\lambda}^{c}(\tau_{0}=0,\lambda) = \int_{0}^{\tau_{0}^{b}} C_{F}^{c}(\tau_{0}',\lambda) \,\mathrm{d}\,\tau_{0}' = \int_{0}^{z_{0}^{b}} \ln(10)\,\tau_{0}(z_{0}') \,C_{F}^{c}(\tau_{0}(z_{0}'),\lambda) \,\mathrm{d}\,z_{0}'. \tag{45}$$

Note that the horizontal averaging in Eq.(42) works only because the transfer equation is integrated on the fixed universal optical depth scale, τ_0 . The contribution functions $C_I^c(\tau_0, \mu_0, \phi_0, \lambda_0)$ and $C_F^c(\tau_0, \lambda_0)$ are saved in contf.cfc3i and contf.cfc3f, respectively. Corresponding contribution functions are also computed for the $\langle 3D \rangle$ model and saved in contf.cfc1i and contf.cfc1f, respectively, and for the external 1D reference atmosphere (contf.cfcxi and contf.cfcxf).

Similarly, we can also write down the <u>Line Intensity Contribution Function</u> as the horizontal average of the integrand of Eq.(24):

$$C_I^{\ell}(\tau_0, \mu, \phi, \lambda) = \frac{1}{\mu} \left\langle \frac{\kappa_{\lambda}^{c}}{\kappa_0^{c}} (1 + \beta) S_{\lambda}^{c}(\tau_0/\mu) \exp\{-\tau_{\lambda}(\tau_0/\mu)\} \right\rangle_{x,\mu}, \tag{46}$$

such that the intensity at a given wavelength in the line profile is

$$I_{\lambda}^{\ell}(\tau_{0}=0,\mu,\phi,\lambda) = \int_{0}^{\tau_{0}^{b}} C_{I}^{\ell}(\tau_{0}',\mu,\phi,\lambda) \,\mathrm{d}\,\tau_{0}' = \int_{0}^{z_{0}^{b}} \ln(10)\,\tau_{0}(z_{0}') \,C_{I}^{\ell}(\tau_{0}(z_{0}'),\mu,\phi,\lambda) \,\mathrm{d}\,z_{0}' \,. \tag{47}$$

The Line Flux Contribution Function at wavelength λ is

$$C_F^{\ell}(\tau_0, \lambda) = \int_0^{2\pi} \int_0^1 \mu' \, C_I^{\ell}(\tau_0, \mu', \phi', \lambda) \, \mathrm{d}\mu' \, \mathrm{d}\phi' \,, \tag{48}$$

such that

$$F_{\lambda}^{\ell}(\tau_{0}=0,\lambda) = \int_{0}^{\tau_{0}^{b}} C_{F}^{\ell}(\tau_{0}',\lambda) \,\mathrm{d}\,\tau_{0}' = \int_{0}^{z_{0}^{b}} \ln(10)\,\tau_{0}(z_{0}') \,C_{F}^{\ell}(\tau_{0}(z_{0}'),\lambda) \,\mathrm{d}\,z_{0}' \,. \tag{49}$$

 $C_I^{\ell}(\tau_0, \mu_0, \phi_0, \lambda_0)$ and $C_F^{\ell}(\tau_0, \lambda_0)$ are stored in contf.cfl3i and contf.cfl3f, respectively, and similarly for the 1D atmospheres in contf.cfl1i, contf.cfl1f, contf.cflxi, and contf.cflxf.

Formally, a Line Depression Contribution Function could be defined as

$$\tilde{C}_{I}^{D} = C_{I}^{c} - C_{I}^{\ell} = \frac{1}{\mu} \left\langle \frac{\kappa_{\lambda}^{c}}{\kappa_{0}^{c}} S_{\lambda}^{c}(\tau_{0}/\mu) \exp\{-\tau_{\lambda}^{c}(\tau_{0}/\mu)\} \left(1 - (1 + \beta) \exp\{-\tau_{\lambda}^{\ell}(\tau_{0}/\mu)\}\right) \right\rangle_{x,y},$$
 (50)

such that the absolute line depression at any wavelength in the line profile is

$$D_{I}(\tau_{0} = 0, \mu, \phi, \lambda) = \int_{0}^{\tau_{0}^{b}} \tilde{C}_{I}^{D}(\tau_{0}', \mu, \phi, \lambda) \, d\tau_{0}' = \int_{0}^{z_{0}^{b}} \ln(10) \, \tau_{0}(z_{0}') \, \tilde{C}_{I}^{D}(\tau_{0}(z_{0}'), \mu, \phi, \lambda) \, dz_{0}'. \tag{51}$$

Note however, that \tilde{C}_I^D does not have the desired physical meaning, because the factor $(1-(1+\beta)\exp\{-\tau_{\lambda}^{\ell}\})$ (i) becomes negative when τ_{λ}^{ℓ} is small $(\tau_{\lambda}^{\ell}$ is the optical depth due to the line opacity only), and (ii) it is non-zero also in layers where the line opacity vanishes. For this reason, \tilde{C}_I^D is not considered useful and hence is not computed in the current version of Linfor3D.

A much better way to define the <u>Line Depression Contribution Function</u> is to consider Eq.(39) and to define it as

$$C_I^D(\tau_0, \mu, \phi, \lambda) = \frac{1}{\mu} \left\langle \frac{\kappa_{\lambda}^c}{\kappa_0^c} \left(\eta \, u_{\lambda}^c(\tau_0/\mu) + (\eta - \beta) \, S_{\lambda}^c(\tau_0/\mu) \right) \exp\{-\tau_{\lambda}(\tau_0/\mu)\} \right\rangle_{x,y}. \tag{52}$$

Note that this contribution function vanisches whereever the line opacity (η, β) is zero. For the flux spectrum we define, as before,

$$C_F^D(\tau_0, \lambda) = \int_0^{2\pi} \int_0^1 \mu' \, C_I^D(\tau_0, \mu', \phi', \lambda) \, \mathrm{d}\mu' \, \mathrm{d}\phi' \,. \tag{53}$$

3.5 Grey test case

Then the absolute line depression at any wavelength in the line profile is

$$D_{I}(\tau_{0} = 0, \mu, \phi, \lambda) = \int_{0}^{\tau_{0}^{b}} C_{I}^{D}(\tau'_{0}, \mu, \phi, \lambda) d\tau'_{0} = \int_{0}^{z_{0}^{b}} \ln(10) \tau_{0}(z'_{0}) C_{I}^{D}(\tau_{0}(z'_{0}), \mu, \phi, \lambda) dz'_{0},$$
 (54)

and

$$D_F(\tau_0 = 0, \lambda) = \int_0^{\tau_0^b} C_F^D(\tau_0', \lambda) \, \mathrm{d}\, \tau_0' = \int_0^{z_0^b} \ln(10) \, \tau_0(z_0') \, C_F^D(\tau_0(z_0'), \lambda) \, \mathrm{d}\, z_0', \tag{55}$$

for the intensity and flux spectrum, respectively.

The Equivalent Width Contribution Function is computed as

$$C_I^W(\tau_0, \mu, \phi) = \int_{\mathcal{A}} C_I^D(\tau_0, \mu, \phi, \lambda') d\lambda', \qquad (56)$$

and

$$W_{I}(\mu,\phi) = \frac{1}{\langle I_{\lambda}^{c}(\mu,\phi,\lambda)\rangle} \int_{0}^{\tau_{0}^{b}} C_{I}^{W}(\tau_{0}',\mu,\phi) d\tau_{0}'$$

$$= \frac{1}{\langle I_{\lambda}^{c}(\mu,\phi,\lambda)\rangle} \int_{0}^{z_{0}^{b}} \ln(10) \tau_{0}(z_{0}') C_{I}^{W}(\tau_{0}(z_{0}'),\mu,\phi) dz_{0}',$$
(57)

where

$$\langle I_{\lambda}^{c}(\mu,\phi,\lambda)\rangle = \frac{\int_{\lambda} D_{I}(\mu,\phi,\lambda') \,\mathrm{d}\,\lambda'}{\int_{\lambda} D_{I}(\mu,\phi,\lambda')/I_{\lambda}^{c}(\mu,\phi,\lambda') \,\mathrm{d}\,\lambda'}.$$
 (58)

For the flux spectrum we have

$$C_F^W(\tau_0) = \int_{\lambda} C_F^D(\tau_0, \lambda') \mathrm{d}\lambda', \qquad (59)$$

and

$$W_{F} = \frac{1}{\langle F_{\lambda}^{c}(\lambda) \rangle} \int_{0}^{\tau_{0}^{b}} C_{F}^{W}(\tau_{0}') d\tau_{0}'$$

$$= \frac{1}{\langle F_{\lambda}^{c}(\lambda) \rangle} \int_{0}^{z_{0}^{b}} \ln(10) \tau_{0}(z_{0}') C_{F}^{W}(\tau_{0}(z_{0}')) dz_{0}',$$
(60)

with

$$\langle F_{\lambda}^{c}(\lambda) \rangle = \frac{\int_{\lambda} D_{F}(\lambda') \, \mathrm{d} \, \lambda'}{\int_{\lambda} D_{F}(\lambda') / F_{\lambda}^{c}(\lambda') \, \mathrm{d} \, \lambda'} \,. \tag{61}$$

Irrespective of the parameter intline, the structures contf.cfd3i and contf.cfd3f hold the contribution functions $C_I^D(\tau_0,\mu 0,\phi_0,\lambda 0)$ and $C_F^D(\tau_0,\lambda 0)$, while $C_I^W(\tau_0,\mu 0,\phi_0)$ and $C_F^W(\tau_0)$ are stored in contf.cfw3i and contf.cfw3f, respectively.

3.5 Grey test case

If cmd.context is set to 'grey', a 3D ($n_x = n_y = 10$) hydrostatic atmosphere is constructed, instead of reading a 3D model. The temperature stratification on the Rosseland optical depth scale is given by

$$T(\tau_{\text{Ross}}) = T_{\text{eff}} \left(\frac{1}{2} + \frac{3}{4}\tau_{\text{Ross}}\right)^{1/4}$$
 (62)

and the source function is linear in τ_{Ross} :

$$S(\tau_{\text{Ross}}) = \frac{\sigma}{\pi} T_{\text{eff}}^4 \left(\frac{1}{2} + \frac{3}{4} \tau_{\text{Ross}} \right). \tag{63}$$

The Eddington-Barbier relation is strictly correct in this case. For any inclination $\mu = \cos \theta$, the emergent continuum intensity is given by

$$I_c(\mu) = \frac{\sigma}{\pi} T_{\text{eff}}^4 \left(\frac{1}{2} + \frac{3}{4} \mu \right).$$
 (64)

In particular, at disk-center ($\mu = 1$) the continuum intensity is

$$I_c(\mu = 1) = \frac{5}{4} \frac{\sigma}{\pi} T_{\text{eff}}^4,$$
 (65)

and the flux is

$$F_c = 2\pi \int_0^1 \mu I_c(\mu) \, \mathrm{d}\mu = \sigma T_{\text{eff}}^4.$$
 (66)

Comparison of the results obtained from Linfor3D for continuum intensity and flux for

TEFF = 5000.00, GRAV = 316.200

LUTAU1 = -8.0000000, LUTAU2 = 2.0000000, DLUTAU = 0.0800000

OPAFILE = 't5000g250mm30_marcs_idmean3xRT3.opta',

GASFILE = 'gas_cifist2006_m30_a04_15.eos',

EOSFILE = 'eos_cifist2006_m30_a04_15.eos'

with the above theoretical results yields (Linfor3D 3.1.3):

ratio			ntheta		
numerical / analytical	1	2	3	-3	4
$I_c(\text{linfor3D})/I_c(\text{Eq.}(65))$	1.0005573	1.0005573	1.0005573	1.0005573	1.0005573
$F_c(\text{linfor3D})/F_c(\text{Eq.}(66))$	1.0004105	1.0148776	1.0079553	1.0004507	1.0050481

If the ratio η of line opacity, κ_{ℓ} and continuum opacity, κ_{c} is constant with optical depth ($\eta = \kappa_{\ell}/\kappa_{c}$), the intensity in the line is simply

$$I_{\ell}(\mu) = \frac{\sigma}{\pi} T_{\text{eff}}^4 \left(\frac{1}{2} + \frac{3}{4} \frac{\mu}{1+\eta} \right),$$
 (67)

the absolute line depression is

$$D_I(\mu) = I_c(\mu) - I_\ell(\mu) = \frac{\sigma}{\pi} T_{\text{eff}}^4 \frac{3}{4} \mu \frac{\eta}{1+\eta}, \tag{68}$$

and the **relative** line depression at disk-center is

$$D_I(\mu = 1)/I_c(\mu = 1) = \frac{3}{5} \frac{\eta}{1+\eta}$$
 (69)

The absolute line depression for flux is

$$D_F = F_c - F_\ell = 2\pi \int_0^1 \mu D_I(\mu) \,\mathrm{d}\,\mu = \sigma \, T_{\text{eff}}^4 \, \frac{1}{2} \, \frac{\eta}{1+\eta} \,, \tag{70}$$

and the relative line depression for flux is

$$D_F/F_c = \frac{1}{2} \frac{\eta}{1+\eta} \,. \tag{71}$$

The ratio between the relative line depression in flux and at disk-center is therfore 5/6, and the same ratio holds for the equivalent widths.

The local absorption line profile is now defined by

$$\eta(\alpha, v) = \eta_0 H(\alpha, v), \tag{72}$$

3.5 Grey test case

where $v = (\lambda - \lambda_0)/\Delta \lambda_D$, and $\alpha = \Delta \lambda_N/2/\Delta \lambda_D$ ($\Delta \lambda_D$: Doppler width, $\Delta \lambda_N$: full width at half maximum of the Lorentzian damping profile). The 'Voigt function' $H(\alpha, v)$ is normalized such that (for $\alpha \ll 1$), $H(\alpha, v) \approx 1$. Assuming that η_0 , α , and $\Delta \lambda_D$ are constant, we can compute the emergent line profile from Eq. (69) or (71). At disk-center, we have

$$D_I(\mu = 1)/I_c(\mu = 1) = R_I = \frac{3}{5} \frac{\eta_0 H(\alpha, v)}{\eta_0 H(\alpha, v) + 1},$$
(73)

and for flux

$$D_F/F_c = R_F = \frac{1}{2} \frac{\eta_0 H(\alpha, v)}{\eta_0 H(\alpha, v) + 1}.$$
 (74)

Clearly, the emergent line profiles are no longer Voigt profiles due to saturation effects.

The (reduced) disk-center equivalent width is obtained from numerical integration of the emergent line profile:

$$\tilde{W}_I = \int_{-\infty}^{+\infty} R_I(v, \eta_0, \alpha) \, \mathrm{d} v \,, \tag{75}$$

and $\tilde{W}_F = 5/6 \, \tilde{W}_I$. An 'analytical' Curve-of-Growth, $\tilde{W}(\eta_0; \alpha = 0.01)$ is shown in Fig. 1.

The equivalent width in [mA] is obtained from the reduced equivalent width by

$$W_{\lambda}[\mathbf{m}\mathring{\mathbf{A}}] = 1000 \,\lambda_0[\mathring{\mathbf{A}}] \,\frac{\Delta v_D}{c} \,\tilde{W} \,. \tag{76}$$

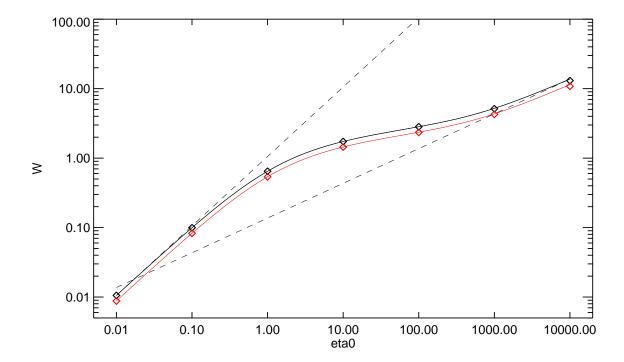


Figure 1: Analytical Curve-of-Growth showing the (reduced!) equivalent width (integrated from v = -100 to v = +100) as a function of η_0 , assuming $\alpha = 0.01$. **Black**: disk-center, **red**: flux. The dashed lines have slopes 0.5 and 1.0. Diamonds show the numerical results obtained with Linfor3D (integration from v = -50 to v = +50).

The results of a number of test calculations are listed below. The wavelength resolution was chosen to be 1/10 of the Doppler width: $\delta\lambda = 0.1 \lambda_0 \Delta v_D/c$. The wavelength range was set to ±50 Doppler widths; $\Delta v_D = 6$ km/s, $\alpha = 0.01$. The line file used for the test calculations is shown below.

```
alam
        Vdop
                 eta0
                         avgt
                                 dlam
                                         ddlam
    7
Test
       grey sf
                Vdop=2.D-5, eta0=1.0D-2, avgt=1.D-2
   7
                          1.0D-2 4.00D0 0.80D-2
4000.000 2.0D-5
                 1.0D-2
                Vdop=2.D-5, eta0=1.0D-1, avgt=1.D-2
Test
       grey sf
1 7
4000.000 2.0D-5
                 1.0D-1
                         1.0D-2 4.00D0 0.80D-2
Test
       grey sf
                Vdop=2.D-5, eta0=1.0D0, avgt=1.D-2
4000.000 2.0D-5
                 1.0D0
                          1.0D-2 4.00D0 0.80D-2
                Vdop=2.D-5, eta0=1.0D1, avgt=1.D-2
Test
       grey sf
1 7
4000.000 2.0D-5
                 1.0D1
                          1.0D-2 4.00D0 0.80D-2
       grey sf Vdop=2.D-5, eta0=1.0D2, avgt=1.D-2
Test
4000.000 2.0D-5
                 1.0D2
                          1.0D-2 4.00D0 0.80D-2
Test
       grey sf Vdop=2.D-5, eta0=1.0D3, avgt=1.D-2
   7
4000.000 2.0D-5
                          1.0D-2 4.00D0 0.80D-2
                 1.0D3
       grey sf
                Vdop=2.D-5, eta0=1.0D4, avgt=1.D-2
Test
                 1.0D4
4000.000 2.0D-5
                         1.0D-2 4.00D0 0.80D-2
clam
           gfscale
-4000.000
           1.0
```

For the following tabulations we have defined

$$\Delta W_I = \log_{10} W_I(\text{linfor3D}) - \log_{10} W_I(\text{Eq.}(75)), \tag{77}$$

and

$$\Delta W_F = \log_{10} W_F(\text{linfor3D}) - \log_{10} \frac{5}{6} W_I(\text{Eq.}(75)), \tag{78}$$

These results are obtained with intline=1:

$\overline{\eta_0}$	ΔW_I		ΔW_F	
	[dex]	ntheta=-3	ntheta=3	ntheta=4
1.0E-02	+0.000342	+0.000336	-0.002949	-0.001690
1.0E-01	+0.000331	+0.000327	-0.002958	-0.001698
1.0E+00	+0.000269	+0.000271	-0.003014	-0.001755
1.0E+01	+0.000072	+0.000081	-0.003203	-0.001942
1.0E+02	-0.000820	-0.000807	-0.004088	-0.002831
1.0E+03	-0.005441	-0.005432	-0.008714	-0.007456
1.0E+04	-0.021428	-0.021421	-0.024704	-0.023446

These results are obtained with intline=-2:

η_0	ΔW_I		ΔW_F	
	[dex]	ntheta=-3	ntheta=3	ntheta=4
1.0E-02	+0.000334	+0.000328	-0.002957	-0.001698
1.0E-01	+0.000324	+0.000320	-0.002965	-0.001706
1.0E+00	+0.000261	+0.000263	-0.003022	-0.001762
1.0E+01	-0.000063	+0.000074	-0.003211	-0.001950
1.0E+02	-0.000825	-0.000814	-0.004097	-0.002838
1.0E+03	-0.005447	-0.005438	-0.008720	-0.007463
1.0E+04	-0.021432	-0.021425	-0.024708	-0.023450

4 Linfor3D and MPI

This section will briefly detail what aspects of the Linfor3D program flow runs in parallel and what aspects do not. Reasons as to why are also given.

Considerable effort has been put into writing the F90 version of Linfor3D so that it can be executed in parallel. It was written and developed using the GNU OpenMP MPI libraries. Consequently, the code has only been tested using mpifort and mpif90. While it is most likely that the code will compile and run using the Intel[©] MPI compiler with the correct corresponding compiler flags, mpiifort, we have not tested this, as this compiler is expensive for personal use and is most commonly found on High Performance Computing (HPC) centre cluster or super computer machines. Moreover, the current version of build has not been designed with mpiifort in mind and does not currently recognise it as a valid compiler. This could be changed.

There are two stages when the program flow parallelizes the execution. Once when the continuous opacities for **3D model atmospheres** are computed with the IONDIS opacity package, and again when all radiative transfer is computed.

4.1 Reading input data

At present all input data is read in to Linfor3D sequentially, and only to the MASTER CPU. The reason for this is to maintain parity with the IDL version of the code, i.e. use of the IONDIS package and the radiative transfer modules inside dort.f90 in their present condition. Almost all data stored during execution is only available on the MASTER CPU. This also saves massive amounts of memory-per-CPU. As the code deviates from its IDL counterpart, it may be necessary to improve this inefficiency and further parallelize the code. This is a low priority.

4.2 Writing data to file

Only the MASTER CPU writes data to file using the UIO package. Until input data is read in parallel there is no need for this to change. This is a **very** low priority.

4.3 Computing 1D continuous opacities

During execution of a standard setup, Linfor3D uses the IONDIS package to compute continuous opacities for two 1D models; the $\langle 3D \rangle$ model and the 1D external model. As this is done so quickly, it was not even considered to be written in a non-sequential way. If input data becomes CPU dependent, this will most likely have to change. This is a **very** low priority.

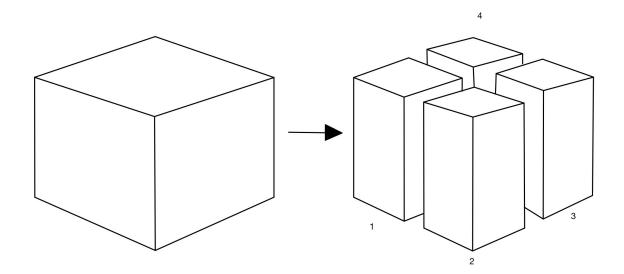
4.4 Computing 3D continuous opacities

The execution of the IONDIS package for a 3D atmosphere can be time consuming in Linfor3D. It depends on the parameters of the input 3D atmosphere(s). Consequently, Linfor3D executes the IONDIS package in a parallel way when it is made available. The code creates smaller domains – or subdomains – within each 3D cube, dividing over horizontal x and y dimensions according to the number of CPUs that have been assigned to the execution. Therefore, the number of subdomains is quivalent to the number of CPUs. The vertical z dimension is not considered as opacities are computed from the bottom of the 3D cube to the top in 1D columns.

The following diagram depicts how the parallelization scheme creates subdomains when four CPUs are assigned to a single snapshot. This is known as 2D domain decomposition.

4 LINFOR3D AND MPI

22



The size of the x and y indexes have each decreased by a factor of 2. As a result each CPU only performs a quarter of the number of the computations a lone CPU would have to during a sequential (or IDL) execution.

As a priority, Linfor3D divides the number of snapshots over the available number of CPUs as equally as possible. This is because they are the most time consuming "dimension" dealt with by the IONDIS package. The remaining CPUs are then divided across the x and y dimensions of every 3D cube as was just explained. To summerize, Linfor3D parallelizes over three dimensions; the number of snapshots (nsnap), the x (nx) and y (ny) horizontal dimensions.

The following example demonstrates how the parallelization scheme behaves when it is given a domain consisting of a single snapshot – or 3D cube – which consists of 28×28 grid points. There are 8 CPUs over which the parallelization scheme has to divide the domain in to subdomains:

	S	ubdoma	in ind	ex sch	ieme :	 for I	ON	 OPA:		
n_CPU	= 8,	n_snap) = 1,	 x-grid	l = 28	8, y-	gr	id = 2	28	
CPU	sn	apshot	:s)	-gri	d	1		-gri	i
ID	ss1	ss2	ds	x 1	x2	dx	I	y 1	y2	dy
0 I	 1	1	1	 1	14	 14	. – – I	 1	 7	 7
1	1	1	1	1	14	14	i	8	14	7
2	1	1	1	1	14	14		15	21	7
3	1	1	1	1	14	14		22	28	7
4	1	1	1	15	28	14		1	7	7
5	1	1	1	15	28	14		8	14	7
6	1	1	1	15	28	14		15	21	7
7	1	1	1	15	28	14		22	28	7

As you can see, the parallelization scheme has divided the horizontal dimensions as equally as it can. The next example represents a more typical run of Linfor3D whose domain now consists of 20 snapshots, and 28×28 horizontal grid points. The parallelization scheme was given 16 CPUs to create 16 subdomains:

======	=====	=====	======	=====	=====	======	=====	=====	====
n_CPU	= 16,	n_sn	ap = 20), x-g	rid =	28, y-	grid :	= 28	
CPU	sn	apsho	ts		x-gri	d		y-gri	d
ID	ss1			x 1	x2	dx	y1	y2	dy
0	1	5	5	1	14	 14	1	14	 14
1	6	10	5	1	14	14	1	14	14
2	11	15	5	1	14	14	1	14	14
3	16	20	5	1	14	14	1	14	14
4	1	5	5	1	14	14	15	28	14
5	6	10	5	1	14	14	15	28	14
6	11	15	5	1	14	14	15	28	14
7	16	20	5	1	14	14	15	28	14
8	1	5	5	15	28	14	1	14	14
9	6	10	5	15	28	14	1	14	14
10	11	15	5	15	28	14	1	14	14
11	16	20	5	15	28	14	1	14	14
12	1	5	5	15	28	14	15	28	14
13	6	10	5	15	28	14	15	28	14
14	11	15	5	15	28	14	15	28	14
15	16	20	5	15	28	14	15	28	14

Subdomain index scheme for IONOPA:

As expected, the parallelization scheme has divided the snapshots as equally as possible into four subdomains. The remaining CPUs are assigned to the horizontal grid points for a total of 16 unique subdomains over which the IONDIS package computes in parallel.

4.5 Computing all radiative transfer

The primary reason that Linfor3D was ported to Fortran was so that the "heavy-duty" computations could take advantage of the MPI modules. The most time consuming parts of a typical Linfor3D run is the execution of dort.f90 for the 3D model atmospheres and for the 1D model atmospheres when dort.f90 is expected to compute curves—of—growth. However, because dort.f90 performs several different operations depending on the type of atmosphere and the set up requirements requested by the user, it was necessary to write an equally adaptive parallization scheme for each atmosphere type. Appropriately, the execution of this parallelization scheme differs enough that each one is described below in separate sections.

4.5.1 DoRT in full 3D

The execution of dort.f90 using full 3D model atmospheres is made up of four dimensions; the number of 3D model atmospheres (nsnap), the number of rays (nmuphi), the number linelists inside the input line file (kline), and the number of wavelength points over which to perform the radiative transfer computations (nlam). The parallelization scheme sets priorities on how these dimensions are divided into subdomains. The number of subdomains is equivalent to the number of CPUs assigned to a job execution. The highest priority is given to nsnap, followed by nrays, then kline and finally nlam. For example, if 8 CPUs are assigned to compute spectra containing 401 lambda points, for a single snapshot, with 13 rays for a single line list, the parallelization scheme will return the following set up:

====== n_	CPU	= 8	, n_s	nap	=	1, r	ray	s =	13	 3, kl	ine	= 1,	nl	ambda = 4	101	
СР	 U	sna	apsho	ots			nray	s		k	 line]	ambda	
I	D	ss1	ss2	ds		r1	r2	dr	1	ks	ke	dk		11	12	dl
	0	1	1	1	 	1	7	7	 	 1	1	1	 	1	100	100
	1	1	1	1		8	13	6	Τ	1	1	1		1	100	100
	2	1	1	1	-	1	7	7	1	1	1	1	1	101	200	100
	3	1	1	1		8	13	6	-	1	1	1		101	200	100
	4	1	1	1		1	7	7		1	1	1		201	300	100
	5	1	1	1		8	13	6		1	1	1		201	300	100
	6	1	1	1	\perp	1	7	7	1	1	1	1		301	401	101
	7	1	1	1	1	8	13	6	1	1	1	1	1	301	401	101

Here, it is shown that as there are few data points in the dimensions with highest priorities, there are enough remaining CPUs to divide computations over wavelength. A more typical run would be to compute a series of snapshots and perhaps more than a single line list. In this example there are 20 snapshots, 13 rays, 7 lines, and 401 wavelength points. There are 16 CPUs assigned to this job:

======	===	=====	====	====	===	====	====	====	==	=====	====	====	===	======	=======	======
				5	Sub	doma	ain i	ndex	: :	schem	e fo	r 3I	D	oRT:		
======= n	=== CPU	===== = 16	===== 5. n	snar	===	==== 20.	==== . n r	avs	===	===== 13.	==== klin	:===: .e =	=== 7.	====== nlambda	======= = 401	======
							· <u>-</u> -									
CP	U	sna	apsho	ots	1		nray	s	1	k	line	!			lambda	
I	D	ss1	ss2	ds	I	r1	r2	dr		ks	ke	dk	1	11	12	dl
	0	1	 5		 I	1	 7	7	. – . 	 1	4	4	 	1	401	401
	1	6	10	5	İ	1	7	7	İ	1	4	4	İ	1	401	401
	2	11	15	5	1	1	7	7		1	4	4		1	401	401
	3	16	20	5	1	1	7	7		1	4	4	Τ	1	401	401
	4	1	5	5		8	13	6		1	4	4		1	401	401
	5	6	10	5	1	8	13	6		1	4	4	1	1	401	401
	6	11	15	5	1	8	13	6		1	4	4	1	1	401	401
	7	16	20	5	1	8	13	6		1	4	4		1	401	401
	8	1	5	5	1	1	7	7		5	7	3		1	401	401
	9	6	10	5		1	7	7		5	7	3		1	401	401
1	0	11	15	5	1	1	7	7		5	7	3	1	1	401	401
1	1	16	20	5	1	1	7	7		5	7	3	1	1	401	401
1	2	1	5	5	1	8	13	6		5	7	3	1	1	401	401
1	3	6	10	5	1	8	13	6		5	7	3		1	401	401
1	4	11	15	5		8	13	6		5	7	3		1	401	401
1	5	16	20	5		8	13	6		5	7	3		1	401	401

As a result of the increased number of data points in each dimension, the whole domain is much larger than the previous example. Even with 4 times as many CPUs, the parallelization routines cannot assign any CPUs to running the wavelength range in parallel.

4.5.2 DoRT in 1D with Curve-of-growth computations

When the user requests Curve–of–Growth computations in the SETCMD input file, the parallelization scheme stops any parallelization over the wavelength dimension. As Linfor3D computes the 1D spectra for either the external 1D model atmosphere, 1DX, or the average 3D model atmosphere(s), \langle 3D \rangle , the program flow must decide whether it (a) is running a 1D atmosphere with several snapshots or whether it (b) computes spectra for an external model atmosphere.

The following example shows how a $\langle 3D \rangle$ model atmosphere would divide the provided 8 CPUs into 8 subdomains as equally as possible. The domain contains 3 model snapshots, 13 rays, a single line list and 401 wavelength points.

====	======	====	=====	=====	====		=====	====	-====	====	===	=======	:=====:	======
				Subd	lomai	in in	dex s	scher	ne fo	r <3I)>	DoRT:		
====	======	====	====	=====	====	====	====	====	=====	====	===	:=======	======	======
	n_CPU	= 8	, n_s	nap =	1, r	ı_ray	s = 1	13, l	cline	= 1	, n	lambda = 4	101	
	 CPU	cn.		 ts		nrav		 I	klin		 I		ambda	
			-	-		-					!	_		
	ID	ss1	ss2	ds	r1	r2	dr	ks	s ke	dk	ı	11	12	dl
	0	1	1	1	1	2	2	:	l 1	1		1	401	401
	1	1	1	1	3	4	2	:	l 1	1	1	1	401	401
	2	1	1	1	5	6	2	:	l 1	1	1	1	401	401
	3	1	1	1	7	8	2		l 1	1	Ĺ	1	401	401
	4	1	1	1	9	10	2	:	l 1		Ι	1	401	401
	5	1	1	1	11	12	2		l 1	1	Ĺ	1	401	401
	6	1	1	1	13	13	1	:	l 1	1	Τ	1	401	401
	7	1	1	1	13	13	1		l 1	1	Ī	1	401	401

As there are only 13 dimensions to divide into 8 subdomains, there are two domains that repeat themselves. Finally, when the 1DX atmosphere is computed on 8 CPUs, the same subdomains are created:

 			Su	==== bdoma	ain i	ndex s	chem	e fo	r 1I	=== DX 1	DoRT:		
 n_CPU	= 8	 , n_s	===== nap =	1, r	 n_ray	rs = 13	 3, kl	ine	= 1,	, n	======================================	 01 	
CPU	sna	apsho	ts		nray	rs	k	line		ı	1	ambda	
ID	ss1	ss2	ds	r1	r2	dr	ks	ke	dk		11	12	dl
0	1	1	1	1	2	2	1	1	1		1	401	401
1	1	1	1	3	4	2	1	1	1		1	401	401
2	1	1	1	5	6	2	1	1	1		1	401	401
3	1	1	1	7	8	2	1	1	1		1	401	401
4	1	1	1	9	10	2	1	1	1		1	401	401
5	1	1	1	11	12	2	1	1	1		1	401	401
6	1	1	1	13	13	1	1	1	1		1	401	401
 7	1	1	1	13	13	1	1	1	1		1	401	401

In the following example, the user has assigned 8 CPUs (subdomains) to compute spectra for 3 snapshots, with 13 rays, for a single line list, over 401 wavelenghts.

26 4 LINFOR3D AND MPI

	==		====	==== S1	=== ubd	==== lomai	n in	dex	sc	:==== :heme	==== for	==== <3I	===)>	====== DoRT: 		
n_CP	U	= 8,	. n_s	nap	=	3, r	 ı_ray	s =	13	s, kl	ine	= 1,	n	 lambda =	401	
СРИ		sna	apsho	ts			nray	s		k	 line				lambda	
ID		ss1	ss2	ds	-	r1	r2	dr		ks	ke	dk	Ι	11	12	dl
	. .					1				1					401	401
0		1	2			1	3	3	•	1	1	1	•	1	401	401
1	1	3	3	1		1	_	3	1	1	1	1		1	401	401
2		1	2	2		4	6	3		1	1	1		1	401	401
3		3	3	1		4	6	3		1	1	1		1	401	401
4	1	1	2	2		7	9	3	1	1	1	1		1	401	401
5		3	3	1		7	9	3		1	1	1		1	401	401
6	1	1	2	2		10	13	4		1	1	1		1	401	401
7		3	3	1	1	10	13	4		1	1 	1		1	401	401

However, the 1DX atmosphere consists of a single model to compute spectra for. So the parallelization scheme treats this differently than the $\langle 3D \rangle$ model atmospheres:

=====	======		====	=====	====	-===	=====		====	====	===		:======:	======
				Sul	odoma	ain i	ndex s	chem	e fo	r 10	X I	DoRT:		
=====	======	====	====	=====	====	====	=====	====	====	====	===	=======	:======	======
	n_CPU	= 8,	n_s	nap =	1, r	ı_ray	s = 13	B, kl	ine	= 1,	n.	lambda =	401	
	CPU	sna	 psho	ts		nray	's	k	line				lambda	
	ID	ss1	ss2	ds	r1	r2	dr	ks	ke	dk	I	11	12	dl
	0	1	 1	1	1	2	2	1	1	1	 	 1	401	401
	1	1	1	1	3	4	2	1	1	1	1	1	401	401
	2	1	1	1	5	6	2	1	1	1	1	1	401	401
	3	1	1	1	7	8	2	1	1	1	1	1	401	401
	4	1	1	1	9	10	2	1	1	1		1	401	401
	5	1	1	1	11	12	2	1	1	1		1	401	401
	6	1	1	1	13	13	1	1	1	1		1	401	401
	7	1	1	1	13	13	1	1	1	1	1	1	401	401

Linfor3D cannot currently run multiple wavelength subdomains for a 1D atmosphere if the user requests Curve—of—Growth calculations. This can slow radiative transfer computations quite substantially.

4.5.3 DoRT in 1D without Curve-of-growth computations

If the user deactivates Curve–of–Growth computations (cog = 0) then the lambda dimension can also be parallelized. As an example, if Linfor3D was requested to compute spectra for 3 snapshots over 13 rays, for a single line list, over a wavelength range containing 401 wavelength points, the code may create the following subdomains:

CPU	I		apsho		l		nray		I	_	line		ļ		lambda	
ID		ss1	ss2	ds		r1	r2	dr		ks	ke	dk	-	11	12	dl
0		1	3	3		1	7	7		1	1	1		1	100	100
1		1	3	3		8	13	6		1	1	1		1	100	100
2		1	3	3		1	7	7		1	1	1		101	200	100
3		1	3	3		8	13	6		1	1	1		101	200	100
4		1	3	3		1	7	7		1	1	1		201	300	100
5		1	3	3		8	13	6		1	1	1		201	300	100
6		1	3	3		1	7	7		1	1	1		301	401	101
7		1	3	3		8	13	6		1	1	1		301	401	101

In this case it cannot divide the 3 snapshots over equally over the 8 subdomains (CPUs), Linfor3D splits the rays and and lambda points next. When the 1DX model atmosphere is computed, the snaps dimension is set to 1:

=====	=====	====	-====	=====	=====	=====	=====	=====	====	====	===	=======	======	======
				S	ubdom	ain i	ndex	schen	e fo	r 1I)X]	DoRT:		
	n_CPI	===== U = 8 	===== 3, n_s	===== snap =	===== = 1, 	===== n_ray	rs = 1	===== 3, kl	ine	==== = 1,	n	======= lambda = 4 	====== 01 	
	CPU	sr	apsho	ots	I	nray	/s	k	line		ı	1	ambda	
	ID	ss1	ss2	ds	r1	r2	dr	ks	ke	dk	1	11	12	dl
	0	 I 1	. 1	1	 I 1	7	7 I	 1	1	1	. – – · I	 1	100	100
	1	1	. 1	1	8		6	1	1	1	i	1	100	100
	2	1	. 1	1	1	. 7	7	1	1	1	1	101	200	100
	3	1	. 1	1	8	13	6	1	1	1	1	101	200	100
	4	1	. 1	1	1	. 7	7	1	1	1	1	201	300	100
	5	1	. 1	1	8	13	6	1	1	1	1	201	300	100
	6	1	. 1	1	1	. 7	7	1	1	1	1	301	401	101
	7	1	. 1	1	8		6	1	1	1	I	301	401	101

4.6 Limitations of Linfor3D with MPI

This version of F90 Linfor3D was written to mostly follow the program flow of the IDL counterpart. This was so that the two most computationally expensive parts of Linfor3D could be used in the same manner in both versions, as was previously mentioned. Naturally, this leads to certain issues that cannot be resolved in the short term. The largest issue concerns the memory requirements as the CPU number increases.

Each CPU requires certain information when computing the radiative transfer or opacities. While the flowfield remains on the MASTER CPU only, some of that data is copied to local arrays on unique CPUs. These arrays only exist during the execution of dort.f90, but nevertheless the code will require larger amounts of memory during these executions. As the IONDIS package uses domain decomposition, the resulting local arrays remain roughly the same size as the global arrays on the MASTER CPU. For the moment, dort.f90 does not allow for domain decomposition. Certain full 3D input arrays – such as the temperature, velocities, and continuous opacities – from the MASTER CPU must be copied to each CPU to properly execute dort.f90.

28 4 LINFOR3D AND MPI

It is therefore highly recommended that the user does not run large Linfor3D jobs² with more than half of all available CPUs on their personal computer unless it has more than 16Gb of RAM. For example, a compute with 16 CPUs and 16Gb of RAM can run Linfor3D fairly safely on 4 to 8 CPUs so long as the horizontal dimensions of the 3D model atmospheres have less than 50 grid points each. Whenever possible, run Linfor3D in MPI mode on a cluster machine or a super computer. One can still run Linfor3D safely in sequential mode on a personal computer like is done in the IDL version.

²A large job represents $nlam \ge 20$, kline > 1

5 Installing GDL and running Linfor3D

While SourceForge constantly update their libraries, to this date, the version of GDL supplied via their download libraries is not complete enough to successfully run Linfor3D. (This was last checked on 10/01/2017). Therefore, one needs to download the current CVS version of GDL.

Linfor3D has only been successfully tested on CVS versions of GDL 0.9.4 and 0.9.5. We are currently testing Linfor3D with GDL versions 0.9.6 and 0.9.7, however, so far we have been unsuccessful in getting Linfor3D to run with them.

To install the CVS version of GDL after download ³ follow these basic instructions. Before installation, you will need to make sure that you have the latest version of cmake and eigan3 version 3.2.7 onwards (see GDL install notes⁴.

Once this is done, **as root**, create a directory in /usr/local called gdl and extract it to a named sub-directory of your choice. (This means that one can get later versions of GDL without deleting previous versions.) Finally make a sub-directory within that directory called build:

```
/ $> mkdir /usr/local/gdl
/ $> mkdir /usr/local/gdl/tarball
/ $> mv <gdl.tarball> /usr/local/gdl/tarball
/ $> cd /usr/local/gdl/
gdl/ $> tar -xzvf ../tarball/<gdl.tarball>
gdl/ $> cd gnudatalanguage
gnudatalanguage/ $> mkdir build
gnudatalanguage/ $> cd build
```

Run cmake within the build directory (if libraries are missing during the cmake procedure, install them as necessary and rerun cmake, making sure that you remove the CMakeCache.txt file beforehand). Then, once the procedure has successfully finished "make" the build (using all the computer cores, N, available):

```
build/ $> cmake ..
build/ $> make -j <N>
```

Once complete, add a symbolic link of the gdl command (<gdl_directory>/src/gdl) to /usr/local/bin/ and run gdl. To check the compatibility of the build, run the command "make check" from the build directory.

5.1 Running Linfor3D with GDL

Installing and running Linfor3D under GDL does not differ from running under IDL. However, for those who wish to exploit its new ability of running on GDL (e.g. use with HPC centres, etc.) a small change must be made in the routine monocubic.pro. Line 165 contains the following:

```
iout=(0 > long(interpol(findgen(n)+1.0,xin,xout))) < n</pre>
```

This must be replaced with the following more formal syntax, because of the minute differences in which GDL and IDL handle array information:

```
iout=(0 > long(interpol(findgen(n)+1.0,xin,[xout]))) < n</pre>
```

This change will not effect any part of the IDL version of Linfor3D, but prevents a fatal error when running Linfor3D under GDL. To make sure this condition is always upheld, and to make sure that user changes do not affect the output from Linfor3D, linfor_monocubic.pro was added to the Routines list in March 2022. Linfor3D will compile this version of monocubic during normal execution.

³Available at http://gnudatalanguage.cvs.sourceforge.net/

⁴http://gnudatalanguage.sourceforge.net/

Finally, copy your IDL_PATH and IDL_STARTUP to GDL_PATH and GDL_STARTUP, and add in the PRO library from the GDL install to the start of the GDL_PATH. If this is properly done, Linfor3D will run without error by using the start guide in Sect. 2.

5.2 Running Linfor3D in parallel

The most important new feature of Linfor3D, now that it runs on GDL, is its ability to run in parallel without the concerns of IDL licenses. This means that completion times for jobs run sequentially can be split into much quicker jobs by, e.g. snapshot or wavelength interval (for large wavelength ranges), which can later be combined. Therefore, for the first time, one can compute large wavelength ranges or complex molecules in hours, not days or weeks. This requires you to create elaborate BASH or TCSH scripts that use EOFs to edit linfor_setcmd.pro.

6 Program Files

In this section all the program files making up the two versions of Linfor3D are listed. While the two codes work independently, and the user is free to choose which version of the code they wish to run, it should be noted that there are some Fortran-based routines and modules that both versions of the code share. All of those routines are found in the subdirectory <LINFOR_DIRECTORY>/xmono/:

File name	Type	Description
dort.F90	M/S	Does all radiative transfer
cubint_module.f90	M	Performs a cubic interpolation/ integration
ha_convol_module.f90	M	Used by cubint_module.f90
ionopa2.f90	S	Control routine for the IONDIS opacity package
iondis.f90	S	Computes pressures and densities
opalam.f90	S	Computes opacities
abuini.f90	S	Initializes the IONDIS package

Table 2: List of routines shared by F90 and IDL/GDL versions of Linfor3D: the table shows the file name, the type (Subroutine or Module, and its description.

In the first three subsections below, an overview of the program flow, the structures in common block linfordata, and a list of its programs are provided for the IDL/GDL version of Linfor3D. The final two subsections describe the program flow in the F90 version of Linfor3D, followed by a list of its modules with a brief description.

6.1 IDL program flow

Basically, the calling sequence is as follows (incomplete listing of linfor_3D.pro):

- Read input parameters (linfor_setcmd.pro)
- Initialize atomic data (linfor_atom.pro)
- Read line data: (linfor_rdline.pro)
- Initialize ionopa abundances, opacity tables and EOS tables
- Set constants (linfor_init)
- Define ff, type linfor_flowfield (linfor_flowfield__define.pro)
- Define f1, type linfor_flowfield: (linfor_flowfield__define.pro)
- Define fx, type linfor_flowfield: (linfor_flowfield__define.pro)
- Define ss, type linfor_spectrum: (linfor_spectrum__define.pro)
- Define s1, type linfor_spectrum: (linfor_spectrum__define.pro)
- Define sx, type linfor_spectrum: (linfor_spectrum__define.pro)
- Read model data into ff structure (linfor_rduio.pro)
- Recompute model on refined z-grid (linfor_regrid.pro)

32 6 PROGRAM FILES

• Compute ionopa quantities (pe, kappa, zeta) and monochromatic tau for 3D model (linfor_ionopa_3d.pro)

- Construct 1D reference atmosphere from ff, store in f1: (linfor_refatm.pro)
- Compute ionopa quantities (pe, kappa, zeta) and monochromatic tau for 1D reference atmosphere (linfor_ionopa_3d)
- Do radiative transfer calculations for 3D model (linfor_dort.pro)
- Do radiative transfer calculations for averaged 3D atmosphere (linfor_dort.pro)
- Store results for later evaluation (linfor_eval, ss, s1, nf, kl)
- Make Plots of line profiles and bisectors (linfor_plot1.pro)
- Do radiative transfer calculations for 1D reference atmosphere (linfor_dort.pro)
- Store results for later evaluation (linfor_evalx.pro)
- Create postcript file(s) (linfor_plot2.pro)
- Generate output files linfor_3D_1.uiosave and linfor_3D_2.uiosave (uio_save.pro).
- (Generate linfor_3D_3.uiosave if cc3d_flag=1.)
- (Generate linfor_3D_1X.uiosave if run_flag=-3.)
- Free pointers to structures ff, f1, fx, ss, s1, and sx if free_flag = 1 (see Sect. 7.2) (linfor_flowfield_free.pro)

6.2 Structures in Common Block linfordata

Table 3 shows a list of the structrues in common block 'linfordata' used by the linfor_3D package.

Structure	Defined in	Description
atom	linfor_atom.pro	Atomic weights & ionization potentials
const	linfor_init.pro	Physical & model constants
cmd	linfor_setcmd.pro	Input parameters controlling program execution
line	linfor_rdline.pro	Line data derived from 'line.dat'
gas	linfor_init.pro	GAS tables initialized by 'tabinter_rdcoeff'
eos	linfor_init.pro	EOS tables initialized by 'tabinter_rdcoeff'
result	linfor_init.pro	Basic results for computing abundance corrections

Table 3: List of all structures in common block 'linfordata': the table shows the name of the structure, the routine where it is defined, and a description. A brief description of the arrays/sub-structures contained within each structure is given in Sect. 10.

6.3 IDL/GDL Files

Table 4 shows a list of all source files necessary to run Linfor3D.

All **IDL/GDL** versions of Linfor3D require the UIO library to handle the I/O of the CO⁵BOLD files, and version 6.0.0 and above requires them for ALL I/O done during the program flow.

6.3 IDL/GDL Files 33

File name	Type	Description
linfor_3D.pro	S	main program
linfor_flowfielddefine.pro	S	Definition of flow field structure
linfor_spectrumdefine.pro	S	Definition of spectrum structure
linfor_raysysdefine.pro	S	Definition of ray system structure
linfor_atom.pro	S	Defines atomic data
linfor_setwts.pro	S	Defines weights for angle quadrature (deprecated after version 6.2.7)
linfor_setwts_lobatto.pro	S	Replacement for linfor_setwts.pro. Further explanations given in Sect. 7.11
linfor_setwts_dblgaus.pro	S	Additional definition for angle quadrature. See Sect. 7.11
linfor_setwts_dblrdau.pro	S	Additional definition for angle quadrature. See Sect. 7.11
linfor_setwts_special.pro	S	Special definition for angle quadrature. See Sect. 7.11
linfor_setcmd.pro	S	Command file, parameter input
linfor_rdxatm.pro	S	Reads 1D reference atmosphere,
		calling linfor_rdatmos, linfor_rdatlas9,
		linfor_rdmarcs, rdl50 or linfor_rdfalmod
linfor_rdatlas9.pro	S	Reads ATLAS9 1D atmosphere (atm.dat)
linfor_rdmarcs.pro	S	Reads MARCS 1D atmosphere (atm.dat)
linfor_rdfalmod.pro	S	Reads FAL 1D atmosphere (atm.dat)
linfor_rdatmos.pro	S	Reads ATMOS 1D atmosphere (atm.dat)
linfor_rdf15.pro	S	Reads a sequence of FOR15 snapshots
		from 2D Kiel hydro simulations (FOR15)
linfor_rdsav.pro	S	Reads 3D snapshot from Copenhagen code (savfs)
linfor_rduio.pro	S	Reads 3D snapshot from CO ⁵ BOLD uio output files
linfor_rdvog.pro	S	Reads 3D snapshot from Voegler MHD code
linfor_findff.pro	S	Finds cached flow fields
linfor_rdline.pro	S	Reads line data (line.dat)
linfor_init.pro	S	Initializes ionopa, EOS, Opacities, several constants
linfor_bisector.pro	S	Computes line bisector positions
		called by linfor_plot1 and linfor_plot2
linfor_convol.pro	S	Convolves line profile with Gauss kernel
		called by linfor_plot1 and linfor_plot2
linfor_dort.pro	S	Computes spectrum from flow field
		(main RT module calling several lower level routines)
linfor_eval.pro	S	Evaluates mean spectrum, "abundance corrections"
linfor_evalx.pro	S	Evaluates reference spectrum, "abundance corrections"
linfor_incline.pro	S	Inclines 3D flow field, called by linfor_ztau
linfor_ionopa_3d.pro	S	Calculates electron pressure, ionization fractions,
		and monochromatic optical depth for given flow field
linfor_rad3.pro	S	Integration of RT equation
linfor_refatm.pro	S	Define 1D reference atmosphere from 3D flow field
linfor_regrid.pro	S	Cut out surface layers from original model, re-define grid
linfor_tauinfo.pro	S	Prints information about optical depth scales
linfor_ztau.pro	S	Prepares bundle of (inclined) rays on monochromatic tau
linfor_monocubic.pro	F	Performs monotonic piecewise cubic interpolation.
		r

34 6 PROGRAM FILES

rdl50.pro	S	Reads the LHD 150 file format.
linfor_plot0.pro	S	Plots flow field
linfor_plot1.pro	S	Plots spatially resolved line profiles
linfor_plot2.pro	S	Plots averaged line profiles
(linfor_plot3.pro)	S	Plots monochromatic granulation images
alpha_line.pro	F	Computes α -parameter for VOIGT function
eta0.pro	F	Computes η_0 , the opacity at line center of metal lines
rrca.pro	F	Computes mean square orbital radius of electron
		(Unsöld)
vdop.pro	F	Computes (thermal+turbulent) Doppler velocity $[c_s]$
linfor_timing.pro	S	Prepares and gathers timing statistics
linfor_timing_print.pro	S	Print timing statistics
uio_save.pro	S	UIO formatted save procedure
uio_restore.pro	S	UIO formatted restore procedure

Table 4: List of all IDL modules: the table shows the file name, the type (Subroutine or Function, and its description.

6.4 F90 program flow

The F90 call makes use of a series of modules, each pertaining to a specific area of the run time of Linfor3D.

- Initialize MPI (linfor_parallel.f90)
- Initialize the timing features (linfor_timing.f90)
- Initialize UIO (linfor_uio.f90)
- Read input parameters (linfor_input.f90)
- Initialize atomic data (linfor_input.f90)
- Read line data (linfor_input.f90)
- Initialize ionopa2, atmosphere parameters, opacity tables and EOS tables (linfor_io.f90)
- Set constants (linfor_input.f90)
- Set up the angle quadratures (linfor_raybase.f90)
- Read 1DX model data (linfor_rdatm.f90)
- Define and populate the 1DX flowfield (fx) type (linfor_rdatm.f90)
- Read 1DX departure coefficients (linfor_nlte.f90)
- Read 3D model data (linfor_rdatm.f90)
- Recompute model on refined z-grid (linfor_rdatm.f90)
- Define and populate 3D flowfield (f3) type (linfor_rdatm.f90)
- Compute (3D) models based on the 3D model data (linfor_rdatm.f90)
- Define and populate (3D) flowfield (f1) type (linfor_rdatm.f90)
- Read 3D departure coefficients (linfor_nlte.f90)

6.5 F90 Files 35

- Define and populate global (3D) flowfield (fa) type (linfor_rdatm.f90)
- Compute ionopa quantities (pe, kappa, zeta) and monochromatic τ for 1DX input model (linfor_ionopa.f90)
- Compute ionopa quantities (pe, kappa, zeta) and monochromatic τ for $\langle 3D \rangle$ models (linfor_ionopa.f90)
- Compute ionopa quantities (pe, kappa, zeta) and monochromatic τ for 3D models (linfor_ionopa.f90)
- Define 3D spectrum (s3) type (linfor_dort.f90)
- Do radiative transfer calculations for 3D models (linfor_dort.f90)
- Define $\langle 3D \rangle$ spectrum (s1) type (linfor_dort.f90)
- Do radiative transfer calculations for (3D) atmospheres (linfor_dort.f90)
- Define 1DX spectrum (sx) type (linfor_dort.f90)
- Do radiative transfer calculations for 1DX atmosphere (linfor_dort.f90)
- Store results for in output data types (linfor_evaluation.f90)
- Generate output files (linfor_wrdata.f90).

6.5 F90 Files

Table 5 shows a list of all source files necessary to run Linfor3D.

All **F90** versions of Linfor3D require the UIO library to handle the I/O of the CO⁵BOLD files, and versions 6.0.0 require them for ALL I/O done during the program flow.

6 PROGRAM FILES

File name	Type	Description
base:		
linfor_main.F90	P	main program.
var_input.f90	M	contains input data types.
var_charlen.f90	M	sets character string lengths throughout Linfor3D.
debug:		
linfor_debug.f90	P	developer module used to output UIO-formatted data for use with the IDL environment.
eos:		
gasinter_routines.F90	M	responsible for reading in the interpolating the equation-of-state to extract hydrodynamical properties such as temperature and pressure. Taken verbatim from CO ⁵ BOLD.
<pre>gfx: linfor_gfx.f90</pre>	M	Deals with most print-to-screen statements.
io:		1
linfor_flowfield.f90	M	deals with the flowfield allocation and array population for most atmosphere types. In particular for CO ⁵ BOLD models.
linfor_input.f90	M	deals with almost all input data (line, cmd, atom, abufile, etc.).
linfor_io.f90	M	responsible for most of the generic IO done by Linfor3D.
linfor_rd1dx.f90	M	reads in all 1D external model atmospheres.
linfor_rd3d.f90	M	control module that calls the appropriate module to read the particular 3D model.
linfor_rdcobold.f90	M	reads in CO ⁵ BOLD model atmospheres.
linfor_rdstagger.f90	M	reads in STAGGER model atmospheres.
linfor_wrdata.f90	M	writes all output to UIO-formatted files.
var_const.f90	M	contains all constant information and the const data
		type.
var_output.f90	M	contains the output data types.
var_snaps.f90	M	contains data type necessary to read in CO ⁵ BOLD 3D full files.
math:		
linfor_box.f90	M	contains several routines to manipulate various properties of the flowfield.
linfor_functions.f90	M	contains several functions and subroutines to deal with general mathematical procedures and array manipula- tion.
linfor_raybase.f90	M	sets up the angle quadratures.
mpi:		
linfor_parallel.f90	M	sets up and defines the parallelization schemes used by Linfor3D.
var_mpi.f90	M	contains data pertaining to the global parameters and information that is passed on to linfor_parallel.f90.
nlte		
linfor_nlte.f90	M	controls the departure coefficient modules.
linfor_rdxbc.f90	M	reads the xbc and xbc2 formatted departure coefficient modules.

6.5 F90 Files 37

opta		
linfor_ionopa.f90	M	controls every call to ionopa2.f90.
var_xkaroslin.f90	M	contains older versions of the xkaros series of subrou-
		tines that use a linear interpolation scheme.
opta_par_module.f90	M	contains arrays pertaining to opta_routines.F90.
		Taken verbatim from CO ⁵ BOLD.
opta_routines.F90	M	control modules for handling and manipulating data
		from CO ⁵ BOLD opacity tables. Taken verbatim from
		CO ⁵ BOLD.
var_ionopa.f90	M	contains data types and local and global arrays used by
		linfor_ionopa.f90.
rad		
linfor_dort.f90	M	control module that sets up all calls to dort.F90.
linfor_eval.f90	M	evaluates the output data from dort.F90 and allocates
		and populations output data types.
var_dort.f90	M	Contains a data type used by linfor_dort.f90.
time		
linfor_timing.f90	M	deals with all timing aspects of Linfor3D.
uio		
uio_base_module.f90	M	These modules are taken verbatim from CO ⁵ BOLD
		and are responcible for
uio_filedef_module.f90	M	almost all IO throughout a typical Linfor3D execution.
uio_bulk_module.f90	M	
uio_mac_module.F90	M	

Table 5: List of all F90 modules: the table shows the file name, the type (**P**rogram or **M**odule, and its description.

7 Parameter Input: linfor_setcmd.pro (IDL) linfor3d.setcmd (F90)

The input parameters (except for those defined in line.dat, see Sect. 8) are basically specified by editing the routine linfor_setcmd.pro in IDL or linfor3d.sectcmd when using the F90 version of Linfor3D. In this way, the user defines the structure cmd (see Table 3). The order of entries is irrelevant. Parameters which are not required may be omitted and set by default in both codes.

A detailed explanation of the various input parameters and their possible values is given in the following sections. An example of the IDL setcmd file follows in Sect. 7.13 and an example of the F90 setcmd file follows in Sect. 7.14.

7.1 F90 specific flags and settings

While the information below can be pertinant to both versions of the code, and is defined in an identical fashion, the following **optional** input is only considered in the F90 execution when set within linfor3d.setcmd:

7.1.1	outfile		
	function	:	file allocation
	required	:	optional
	type	:	character
	values	:	<pre>'output.uiosave' (default 'Linfor3D.uiosave')</pre>

One sets this parameter to save the entire output to file. By default it is saved as Linfor3D.uiosave. This contains all input and output structures that can be loaded into IDL, Python and Fortran.

7.1.2	printcobol	d	
			execution flag
	required type	:	. *
	• •		0 (default), 1

When set to 1 Linfor3D will print extra information concerning the EOS, opta tables and full files to screen. By default this is set to 0, as this information is usually superfluous to a typical Linfor3D run.

7.1.3	debug		
	function required type	execution flag optional integer	
	• •	0 (default), 1	

This is only used to determine how the parallelization scheme executes on the allocated number of CPUs. When debug=1 no calls to ionopa.f90 or dort.f90 are made. Rather, the parallelization scheme outputs further information on how mpirun -np <NCPU> has been allocated by the parallelization scheme, given the number of CPUs, <NCPU>. This is mostly used for development purposes.

Therefore, it can be ignored in most normal scenarios.

function : execution flag required : optional type : integer values : 0, 1 (default)

This switches off writing the 3x3 model atmospheres.

7.1.5	d1_flag		
	function	:	execution flag
	required	:	optional
	type	:	integer
	values	:	0, 1 (default)

Tells Linfor3D whether it should compute the (3D) models for spectrum synthesis.

7.2 IDL specific flags and settings

There are certain features available in the IDL version that is not available or deprecated in the F90 version, such as the plotting ability.

7.2.1	plt_flag		
	function	:	plotting of bisectors
	required	:	always
	type	:	integer
	values	:	-1, 0, 1

The parameter plt_flag controls if line bisctors should be plotted or not (0: no, 1: yes). If plt_flag is set to -1, all plotting is suppressed.

```
function : free pointers in structures at end of program
required : always
type : integer
values : 0, 1
```

If free_flag = 1, then each run of Linfor3D allocates fresh memory for the structures ff, f1, fx, ss, s1, and sx. In this case the corresponding pointers are removed at the end. If you want to examine the structures after the end of execution, you must have free_flag = 0. If you want to run the program several times in a row with different input parameters, you should set free_flag = 0 in order to avoid additional memory allocation for each run.

7.2.3	ff_path		
	function	:	directory to be used for reading and writing cached flow fields
	required	:	always
	type	:	string
	values	:	e.g. '/data/mst/ffcache/'

7.3 Program execution flags (IDL/F90)

The user can control the program execution by setting the flags run_flag, nlte_flag, cv1_flag, cv2_flag, cv3_flag, maps_flag, cc3d_flag, rdbb_flag, which are explained in more detail below.

function: program mode
required: always
type: integer
values: -3, -2, -1, 0, 1, 2, 3 (usually 3)

This parameter determines the general function of Linfor3D:

IMPORTANT: The F90 version of the code currently only runs using flags = -3, and 3. Flags = 1 or 2 will most likely never be included inside the F90 version.

Setting run_flag = -3 allows you to compute the external 1D atmosphere only. While a snapshot is still required to run Linfor3D correctly, no 3D or $\langle 3D \rangle$ data is computed or written to file. The results are stored in the structure 'linfor_1X.uiosave'. N.B. mode is only available from version 6.1.0 onwards.

Setting run_flag = -2 allows you to compute 3x3 file for the external reference model only.

Setting run_flag = -1 allows you to restore old results, and replace the results of the previous 1D external atmosphere with those of a different 1D external atmosphere.

Setting run_flag = 0 (similar to run_flag = -1) allows you to quickly compare the 3D spectra with another external 1D reference atmosphere. Finally, the results are saved in files 'linfor_3D_1.uiosave' and 'linfor_3D_2.uiosave'. Rarely used setting.

Setting run_flag = 1 is used for plotting the structure of the input model on the original grid. No radiative transfer calculations are done.

Setting run_flag = 2 is used for plotting the structure of the input model on the reduced (refined) grid. No radiative transfer calculations are done.

Setting run_flag = 3 is the usual case. After construction of the 3D atmosphere on the reduced (refined) grid and of the 1D mean atmosphere, the line formation calculations are done, and the results are plotted ('linfor_plot1': spatially and temporally resolved line profiles and bisectors, 'linfor_plot2': surface and time averaged line profiles and bisectors). Finally, the results are saved in files 'linfor_3D_1.uiosave' and 'linfor_3D_2.uiosave'.

run_flag value		control of program flow
-3	:	load 3D models, (compute 1D ref. spectrum), save results
-2	:	compute 1D 3x3 external atmosphere
-1	:	restore results, (compute 1D ref. atmosphere & spectrum),
		save results
0	:	restore results, (compute 1D ref. atmosphere & spectrum),
		plot2, save results
1	:	compute 3D, 1D atmospheres (1), plot01, stop
2	:	compute 3D, 1D atmospheres (1,2), plot02, stop
3	:	compute 3D, 1D atmospheres (1,2), line formation,
		plot1, plot2, save results

```
7.3.2 cv1_flag

function : enforce \langle \rho u_x \rangle = 0
required : always
type : integer
values : 0, 1
```

The parameter cv1_flag controls whether or not the x-component of the velocity field is adjusted to ensure zero mass flux in x-direction. (0: no, 1: yes). Default 0

```
7.3.3 cv2_flag

function : enforce \langle \rho u_y \rangle = 0
required : always
type : integer
values : 0, 1
```

The parameter $cv2_flag$ controls whether or not the *y*-component of the velocity field is adjusted to ensure zero mass flux in *y*-direction. (0: no, 1: yes). Default 0

```
7.3.4 cv3_flag

function : enforce \langle \rho u_z \rangle = 0
required : always
type : integer
values : 0, 1
```

The parameter cv3_flag controls whether or not the z-component of the velocity field is adjusted to ensure zero mass flux in z-direction. (0: no, 1: yes). Default 0

7.3.5	maps_flag			
	function	:	controls output of intensity maps	
	required	:	always	
	type	:	integer	
	values	:	0, 1, 2	

The parameter maps_flag controls the output of intensity maps which are provided in the IDL structure MAPS:

value		meaning
0	:	Continuum images only. Create map ICLAMO.
1	:	Continuum images (ICLAMO) plus images at the centre of the wavelength window
		(ICLAM1), all at wavelength $\lambda = clam$;
2	:	Continuum images (ICLAMO) plus images (ICLAM2) at all wavelengths within the
		wavelength window of width $2 \cdot dlam$ around the central wavelength clam:
		$\lambda_i = clam - dlam + i \cdot ddlam \text{ (see Sect. 8)};$

7.3.6	cc3d_flag		
	function	:	output of 3D contribution function
	required	:	always
	type	:	integer
	values	:	0, 1

The parameter cc3d_flag controls whether the 3D continuum intensity contribution function should be saved in structure contf3d or not (0: no, 1: yes).

7.3.7	nlte_flag		
	function	:	output of 3D contribution function
	required	:	always
	type	:	integer
	values	:	0, 1, 2, 3

The parameter nlte_flag controls whether the line transfer is performed in LTE (nlte_flag=0) or in NLTE (nlte_flag=1, 2, 3). The NLTE options work only for lines with available departure coefficients, which are read from a separate data file (see below).

value		meaning
0	:	Continuum and lines in LTE.
1	:	Continuum in LTE, line source function in LTE, line opacity in NLTE
2	:	Continuum in LTE, line opacity in LTE, line source function in NLTE,
3	:	Continuum in LTE, line opacity and source function in NLTE

7.4 General paths

7.4.1	abupath		
	function	:	directory where '.abu' files and 'atom.dat' are located
	required	:	always
	type	:	string
	values	:	e.g. '/home/mst/ABU/'

If abupath is not specified in the command file, the path is taken from environment variable '\$LINFOR3D_ABU'.

7.5 Model data 43

function : directory with opacity tables (.opta files) required : always type : string values : e.g. '/home/mst/RHD/opa/dat/'

We recommend setting the environment variable \$OPTABLES

7.4.3	gaspath		
	function	:	directory with GAS tables (gas_*.eos files)
	required	:	always
	type	:	string
	values	:	e.g. '/home/mst/RHD/eos/dat/'

7.4.4	eospath		
	function	:	directory with EOS tables (eos_*.eos files)
	required	:	always
	type	:	string
	values	:	e.g. '/home/mst/RHD/eos/dat/'

We recommend setting the environment variable \$EOSTABLES for these two paths.

7.5 Model data

7.5.1	context		
	function	:	source of input model
	required	:	always
	type	:	string
	values	:	e.g. 'cobold'

value		meaning
'cobold'	:	3D CO⁵BOLD
'copenhagen'	:	N&S 3D code
'kiel'	:	Kiel 2D HDW-Code
'muram'	:	MURAM 3D MHD Code
'grey'	:	construct grey 3D ($n_x = n_y = 10$)
	:	hydrostatic atmosphere for test purposes

The τ_{Ross} grid of the grey atmosphere is defined by the parameters cmd.lutau1, cmd.lutau2, cmd.dlutau. The atmospheric parameters must be specified as cmd.Teff and cmd.grav. The opacity table must be specified as cmd.opafile, and the equation of state as cmd.eosfile and cmd.gasfile.

function : directory with 2D/3D model atmospheres (.end, .full files) required : always type : string values : e.g. '/data/mst/model/'

function : name of 2D/3D model file required : always type : string values : e.g. 'gt57g44n66_3Dgz.end'

Note: A list of files can be specified by using wildcards, e.g. 'chro3D04*.full'.

7.5.4	parfs		
			full path to parameter file (rhd.par)
	required	:	CO ⁵ BOLD only
	type	:	string
	values	:	e.g. '/data/mst/model/par/gt57g44n66.par'

7.5.5	xbcpath3	
		: full path to 3D xbc or xbc2 files (*.xbc/*.xbc2)
	type	: optional: string
	values	: e.g. '/data/mst/NLTE3D_data/model/'

7.5.6	xbcpathx		
	function	:	full path to 1DX(external) xbc or xbc2 files (*.xbc/*.xbc2)
	required	:	optional
	type	:	string
	values	:	e.g. '/data/mst/NLTE3D_data/model/'

7.5.7	xbcpath		
	function	:	full path to 3D and 1DX xbc or xbc2 files (*.xbc/*.xbc2)
	required	:	optional
	type	:	string
	values	:	e.g. '/data/mst/NLTE3D_data/model/'

Note: departure files are necessary for NLTE line formation calculations. xbcpath is superseeded by xbcpath3 and xbcpathx.

7.5 Model data 45

7.5.8	abuid		
	function	:	Model abundance mixture to be used in the ionopa (or ionopa2) routine
	required	:	always
	type	:	string
	values	:	'kiel', 'cifist2006', 'special'

abuid identifies the solar abundance mix which is then modified according to dmetal and dalpha (see below). The corresponding tables, kiel.abu, cifist2006.abu, or special.abu must be located in directory abupath. Version 6.2.2 onwards use ionopa2, which requires two abundance mixture files: The model abundance mixture, abuid (above); and the spectrum abundance mixture, abuidx (below).

7.5.9	abuidx		
	function	:	Spectrum abundance mixture to be used in ionopa2 routine
	required	:	always (version 6.2.2 onwards)
	type	:	string
	values	:	'kiel', 'cifist2006', 'special'

Linfor3D has an additional way it computes ionopa quantities (pe, kappa, zeta) and the monochromatic tau scale. When abuid=abuidx (or if abuidx is **not** defined), these quantities are computed as they were in previous versions of Linfor3D. When abuid contains the solar abundance mixture of the CO⁵BOLD model and abuidx contains the desired abundance mixture of the spectrum synthesis then ionopa2 computes the quantities twice to compensate for the change in abundance.

7.5.10	dmetal		
	function	:	metallicity [M/H] (log ₁₀) to be used in ionopa-routines
	required	:	always
	type	:	float
	values	:	e.g. 0.0, -0.5, -2.0

The logarithmic abundance of all elements beyond Li (N > 3) is changed by dmetal.

7.5.11	dalpha		
	function	:	alpha enhancement to be used in ionopa-routines
	required	:	always
	type	:	float
	values	:	e.g. 0.0, +0.4

The logarithmic enhancement factor to be applied to all α -elements.

Linfor3D considers O, Ne, Mg, Si, S, Ar, Ca, and Ti as α -elements.

function : sampling of model in x-direction required : if context='cobold','kiel','muram' type : integer values : 1, 4, 10; -1

If both nx_skip and ny_skip (see Sect. 7.5) are negative, the original data are re-binned from (nx,ny) to (nx/abs(nx_skip), ny/abs(ny_skip)). In the usual case that both nx_skip and ny_skip are positive, the original data are re-sampled, skipping by nx_skip in x, and by ny_skip in y-direction (nx/nx_skip, and ny/ny_skip should preferably be an integer). If nx_skip and ny_skip have different signs, an error message is printed and the program is stopped. The value 1 has no effect.

7.5.13	ny_skip	
		: sampling of model in x-direction: if context='cobold','kiel','muram'
	• I	: integer : 1, 4, 10; -1

For details see description of nx_skip (Sect. 7.5).

7.6 More model information (MOST read from parameter file for CO⁵BOLD data)

The *majority* of parameters in this section are ignored in the case of CO⁵BOLD data and instead read from the specified CO⁵BOLD parameter file. Please read this section carefully to avoid errors in your synthesis.

```
function : name of opacity file (binned opacity tables)
required : not needed if context='cobold'
type : string
values : e.g. 'g2v.opta'
```

7.6.2	gasfile		
	function	:	name of GAS file $(P, T \rightarrow \rho, e,)$
	required	:	not needed if context='cobold'
	type	:	string
	values	:	e.g. 'gas_mm00_l.eos'

7.6.3	eosfile		
	function	:	name of EOS file $(\rho, e \rightarrow P, T,)$
	required	:	not needed if context='cobold'
	type	:	string
	values	:	e.g. 'eos_mm00_1.eos'

function : opacity scale height [cm] at top of 3D model required : always type : float values : e.g. 60.0E5; default = 0.0

A **default value of 0.0** tells Linfor3D to take this parameter from the parameter file (set at sect. 7.5 - parfs - e.g. rhd.par).

7.6.5	qmol		
	function	:	mean molecular weight of neutral gas
	required	:	not needed if context='cobold'
	type	:	float
	values	:	e.g. 1.301855

Important Note: This parameter has been deprecated in Linfor3D version 6.2.6 onwards.

7.6.6	Teff		
	function	:	effective temperature of 3D model
	required	:	not needed if context='cobold'
	type	:	float
	values	:	e.g. 5770.0

7.6.7	grav		
	function	:	surface gravity [cm/s ²] of 3D model
			not needed if context='cobold'
	type	:	float
	values	:	e.g. 27500.0

7.6.8	tsurffac		
	function	:	surface temperature ($\tau = 0$) of 3D model is tsurffac· T_{eff}
	required	:	always
	type	:	float
	values	:	e.g. 0.727903; default = 0.0

A **default value of 0.0** tells Linfor3D to take this parameter from the parameter file (set at sect. 7.5 - parfs - e.g. rhd.par). This only affects **Linfor3D** version 6.2.6 onwards. Versions of Linfor3D older than this do not read this parameter from setcmd if context='colbold'.

7.7 Model data - reading of 'full' files (CO⁵BOLD only)

The parameters in this section are only needed for reading snapshot from $\mathsf{CO}^5\mathsf{BOLD}$ data files.

7.7.1 isnap_full_1

function : first snapshot to be read from full file(s)
required : only needed if context='cobold'

type : integer values : 1

7.7.2 isnap_full_2

function : last snapshot to be read from full file(s)required : only needed if context='cobold'

type : integer values : 1

7.7.3 istep_full

function : step for reading snapshots from full file(s)

required : only needed if context='cobold'

type : integer values : 1

7.8 $\langle 3D \rangle$ mean model

7.8.1	mavg		
	function	:	mode of averaging 3D T-structure on $ au_{ m Ross}$
	required	:	always
	type	:	integer
	values	:	1, 4

value		meaning
1	:	$T_{\langle \text{3D} \rangle}(\tau_{\text{Ross}}) = \langle T_{\text{3D}}(\tau_{\text{Ross}}) \rangle$
4	:	$T_{\langle 3\mathrm{D}\rangle}(\tau_{\mathrm{Ross}}) = \langle T_{\mathrm{3D}}^4(\tau_{\mathrm{Ross}}) \rangle^{1/4}$

7.9 External 1D reference model

7.9.1	atmpath		
	function	:	directory with 1D model atmospheres
	required	:	always
	type	:	string
	values	:	e.g. '/home/mst/atm/'

7.9.2	atmfile		
	function	:	name of 1D reference model
	required	:	always
	type	:	string
	values	:	e.g. 'NONE', 'dxgt57g44n59.150', 'falc.at9', 'falc.mod', '<3D>'

Note: No external 1D reference atmosphere will be used if atmfile='NONE'. In this case the parameter atmpath has no meaning. If atmfile='<3D>' the external model atmosphere is replaced by a global $\langle 3D \rangle$ model atmosphere constructed by averaging the individual $\langle 3D \rangle$ snapshots.

Linfor3D has the capability to read in several types of external 1D model atmospheres. The way it determines the type of model atmosphere is with the file extension. For example, '.150' is determined as an LHD model atmosphere. This is determined at the linfor_rdxatm.pro routine level. The result of that will invoke one of several routines to properly read the model atmosphere. Here is a list of 1D model atmospheres accepted by Linfor3D, the routine name that reads the model, and what the external model atmosphere file extension should be:

Model atmosphere		Invoked routine		File extension
LHD	:	rdl50.pro	:	'.15 0 '
Kiel ATMOS	:	<pre>linfor_rdatmos.pro</pre>	:	'.atm'
ATLAS9	:	linfor_rdatlas9.pro	:	'.at9' or 'a12'
MARCS	:	linfor_rdmarcs.pro	:	'.mod'
FAL*	:	<pre>linfor_rdfalmod.pro</pre>	:	'.fal'

^{*}Fontenla, Avrett, Loeser models (1993, ApJ 406, 319)

Finally, should you wish to compute a $\langle 3D \rangle$ model again, for different parameters, such as microturbulence, the routine d3a21dx.pro will convert a standard $\langle 3D \rangle$ model (which is saved as an idlsave) to a properly formatted ATLAS9 model accepted by Linfor3D. However, this model is only compatable with Linfor3D and the routine is only available with Linfor3D version 6.2.6 onwards.

7.10 Line data and radiative transfer

7.10.1 linfs

function : name of line data file

required : always type : string

values : e.g. 'Li67.line'

Note: If linfs is not specified, the default value 'line.dat' is assumed.

7.10.2 lutau1

function : smallest $\log \tau_{\text{Ross}}$ covered by sub-model (refined z-grid)

required : always type : float values : e.g. -7.0*D*0

7.10.3 lutau2

function : largest $\log \tau_{\text{Ross}}$ covered by sub-model (refined z-grid

required : always type : float values : e.g. 2.0*D*0

7.10.4 dlutau

function : z-spacing of sub-model corresponds roughly to $\Delta \log \tau_{Ross}$ =dlutau

required : always type : float

values : e.g. 8.0D - 2

7.10.5 lctau1

function : smallest $\log \tau_{\rm cont}$ used for RT integration

required : always type : float

values : e.g. -7.0D0, ≥ 1 utau1

7.10.6 lctau2

function : largest $\log \tau_{\rm cont}$ used for RT integration

required : always type : float

values : e.g. 2.0D0, ≤ 1 utau2

7.10.7 dlctau

function : resolution in $\log \tau_{\rm cont}$ used for RT integration

required : always type : float

values : e.g. 8.0D - 2

function : controls broadening of hydrogen lines required : always type : integer values : 0, 1, 2, 3, 4

value		meaning
0	:	Cayrel & Traving (1960), default
1	:	Resonance broadening: AG, Stark broadening: G
2	:	Resonance broadening: BPO, Stark broadening: G
3	:	Resonance broadening: A08, Stark broadening: G
4	:	Resonance broadening: A08 , Stark broadening: SH

AG: Ali & Griem (1966, Phys. Rev. 144, 366),

BPO: Barklem, Piskunov and O'Mara (2000, A&A 363, 1091),

A08: Allard et al. (2008, A&A 480, 581),

G: Griem (1960, ApJ 132, 883), with corrections to approximate the Vidal, Cooper & Smith (1973,

ApJS 25, 37) profiles.

SH: Stehlé & Hutcheon (1999 A&AS, 140, 93)

Note 1: option Hbrd = 2 has an effect only on $\mathbf{H}\alpha$, $\mathbf{H}\beta$, and $\mathbf{H}\gamma$, and Hbrd = 3 affects only $\mathbf{H}\alpha$; all other hydrogen lines are treated according to option Hbrd = 1, unless Hbrd = 0.

Note 2: option Hbrd = 4 is not currently working (as of version 6.2.4 – check the readme file in the later versions of Linfor3D for updates on this).

7.10.9	vsini		
	function	:	Sets $v \sin i$ value for all spectra in linfor_plot2.pro only
	required	:	always
	type	:	float
	values	:	e.g. 1.0

7.10.10 ximicx		
function	:	isotropic Gaussian microturbulence velocity [km/s] for external
		1D reference model (added quadratically to thermal velocity)
required	:	always
type	:	float
values	:	e.g. 1.0

7.10.11	ximic1		
	function	:	isotropic Gaussian microturbulence velocity $[km/s]$ for $\langle 3D \rangle$
			mean models (added quadratically to thermal velocity)
	required	:	always
	type	:	float
	values	:	e.g. 1.0

values

e.g. 1.0

function : isotropic Gaussian microturbulence velocity [km/s] for 2D/3D models (added quadratically to thermal flow velocity)
required : always
type : float

function : Isotropic Gaussian macroturbulence velocity [km/s] for external
1D reference model (additional line broadening after line formation)
required : always
type : float
values : e.g. 1.6

function : Isoptropic Gaussian macroturbulence velocity [km/s] for (3D) mean models (additional line broadening after line formation)
required : always
type : float
values : e.g. 1.6

function: Isotropic Gaussian macroturbulence velocity [km/s] for 2D/3D models (additional line broadening after line formation)
required: always
type: float
values: e.g. 1.6

function : the x-component of the hydrodynamical velocity field of the 2D/3D models is multiplied by this factor required : always type : float values : e.g. 0.0, 1.0

function : the y-component of the hydrodynamical velocity field of the 2D/3D models is multiplied by this factor required : always type : float values : e.g. 0.0, 1.0

function : the z-component of the hydrodynamical velocity field of the 2D/3D models is multiplied by this factor required : always type : float values : e.g. 0.0, 1.0

7.10.19 micro		
function	:	controls microturbulence in 1D Curve-of-Growth
required	:	always
type values		integer 0, 1

Determines whether or not different microturbulence values should be used when computing the 1D Curve-of-Growth. 0: only one value, given by ximicx and ximic1, respectively; 1: sequence of microturbulence values defined by parameters xi_a, xi_b, xi_d (see below).

7.10.20 xi_a		
function	:	determines start value for microturbulence sequence
required	:	always
type	:	float
values	:	e.g. 0.0, default: 0.5

7.10.21 xi_b		
function	:	determines end value for microturbulence sequence
required	:	always
type	:	float
values	:	e.g. 2.0, default: 1.5

7.10.22 xi_d					
function	:	determines intervals of microturbulence sequence			
required	:	always			
type	:	float			
values	:	e.g. 0.1, default: 0.125			

The microturbulence sequence is computed as $xi(i) = xi0 * (xi_a + i * xi_d)$, i=0 .. im, where xi0 is ximicx and ximic1, respectively, and $im=(xi_b - xi_a)/xi_d$.

function : determines the variation of the continuum required : always type : float values : e.g. 20.0, default: 0

if dclam=0, the continuum is treated as constant (default). Otherwise, the continuum is computed at 3 wavelength points, clam-dclam, clam, clam+dclam, where clam is the central wavelength (in Å) of the computed spectral range (see Sect. 8), and dclam is half the width of the specified spectral range (in Å). The continuum is computed by parabolic interpolation inside the spectral window. If the spectral range of the specified synthetic spectrum (which is defined by the parameters of the line file (see Sect. 8) exceeds a few Å, dclam should be set to match half the total spectral range.

7.10.24 intmode				
required type	: :	•		

Determines the mode of integration in routines ms_int_tau and ms_int_exp, which can be linear (0) or monotonic and cubic (1, standard).

7.10.25 intline		
function	:	mode of integrating the line transfer equation
required	:	always
type	:	integer
values	:	1, 2, -1, -2

Determines the method of integrating the line transfer equation (see Section 3 for details). Default value is intline=1.

value		meaning
1	:	Line depression on fixed $\log \tau$ scale (Eq. 41)
2	:	Line depression on monochromatic τ scale (Eq. 36)
-1	:	Line intensity on fixed $\log \tau$ scale (Eq. 25)
-2	:	Line intensity on monochromatic τ scale (Eq. 26)

7.10.26 r	nchunk		
fu	nction	:	rad.transfer is done in n_chunk "slices"
rec	quired	:	always
tyı	pe	:	integer
va	lues	:	e.g. 2

Default is nchunk = 1, i.e. the whole model is processed as one block. For large models, it may be necessary to split the computation into several 'chunks' to save memory.

7.11 Angle quadrature schemes

By default, Linfor3D requires the following information to compute the transfer equation over several ray angles.

7.11.1 **ntheta**function: number of θ -angles for which spectrum is computed required: always type: integer values: 0, 1, 2, 3, (-3), 4, 6, 8

0: Intensity spectrum, > 0: Intensity and flux spectrum;

7.11.2 **nphi**function: number of ϕ -angles for integration of flux spectrum required: always type: integer values: no restriction, typically 4

7.11.3 mu0

function: view angle $\mu = \cos \theta$ required: always
type: float
values: $0.0 \dots 1.0$

If the parameter ntheta=0, then the spectrum and intensity maps are computed for inclination angle mu0 (= $\cos \theta_0$).

mu0= 1.0 corresponds to vertical rays, i.e. disk center view.

mu0= 0.0 corresponds to the very limb, but a value of mu0=0.0 will clearly not work.

7.11.4 kphi

function: view angle
required: always
type: integer
values: 0, 1, 2, 3

The parameter kphi determines the direction from which the model is viewed:

value		meaning
0	:	rays emerge parallel to the x-axis, i.e. the model is viewed somewhere
		on the 'equator' between the left limb and disk center.
1	:	rays emerge parallel to the y-axis, i.e. the model is viewed somewhere
		on the 'meridian' between the lower limb and disk center.
2	:	rays emerge anti-parallel to the x-axis, i.e. the model is viewed somewhere
		on the 'equator' between the right limb and disk center.
3	:	rays emerge anti-parallel to the y-axis, i.e. the model is viewed somewhere
		on the 'meridian' between the upper limb and disk center.

Other (integer) values of kphi are allowed, but give no new results; increasing kphi by one in-

creases phi by $\pi/2$.

However, since the release of Linfor3D version 6.3.0, several new schemes have been introduced for the user to select:

Name		meaning
Lobatto	:	quadrature through routine linfor_setwts_lobatto.pro
Double Gauss	:	<pre>quadrature through routine linfor_setwts_dblgaus.pro</pre>
Double Gauss-Radau	:	<pre>quadrature through routine linfor_setwts_dblrdau.pro</pre>
Custom-made	:	<pre>quadrature through routine linfor_setwts_special.pro</pre>

These new quadrature schemes can be used by selecting them in the setcmd:

7.11.5	raybase		
	function	:	quadrature scheme
	required	:	always
	type	:	string
	values	:	'lobatto', 'dblgaus', 'dblrdau', and 'special'

If the raybase option is missing from the setcmd then the default lobatto is selected. For the user, little has changed. One must still select the number of μ and ϕ angles to use, like before. The only exception to this, is when the user elects to use a custom angle quadrature scheme.

To use the special case, a file called 'special.xmu' that contains the list of mu-angles and corresponding weights must be made available in the working directory. Examples of this file can be found in the Data subdirectory of the Linfor3D directory tree.

7.12 Curve-of-Growth computations

As standard, Linfor3D computes a Curve-of-Growth (CoG) for the 1D external and $\langle 3D \rangle$ model atmospheres. The range in abundance, and the sampling of the range were fixed within Linfor3D. Version 6.2.5 onwards now includes the option to tailor the Curve-of-Growth, or deactivate the computations.

7.12.1	cog		
	required type	:	Tailors the Curve-of-Growth computations always integer -1, 0, 1

Default is cog = 1. cog = 0 deactivates the CoG computations (speeds up computations of large line lists). cog = -1 activates a tailored CoG. Requires the three following parameters, otherwise Linfor3D computes a standard CoG (like cog = 1).

7.12.2	icg	
		sets index from default to user defined yes, if cog=-1
	type values	integer e.g. 51, 101

7.12.3 gflgmin function: sets minimum $\Delta \log gf$ value over which to perform CoG computations required: yes, if $\cos = -1$ type: float values: e.g. -3.0

7.12.4 gflgmax function: sets maximum $\Delta \log gf$ value over which to perform CoG computations required: yes, if cog=-1 type: float values: e.g. +2.5

If these properties are not included in $linfor_setcmd$, the default settings are invoked; icg=51, gflgmin=-1.0, gflgmax=+1.5.

All of the options defined in Sect. 7 are checked by linfor_checkcmd.pro and are set to default values in the event that they are missing from setcmd.

7.13 IDL Example

```
pro linfor_setcmd
common linfordata
```

```
cmd = $
:-----
; Program execution flags:
                              ; 0 / 1 / 2 / 3: LTE or NLTE for lines with xb
nlte flag: 0. $
 run_flag: 3, $
                              ; execution mode: -3, -2, -1, 0, 1, 2, 3
 cv1_flag: 1, $
                              ; 0 / 1: enforce <rho*v1>(z)=0 off / on
 cv2_flag: 1, $
                              ; 0 / 1: enforce < rho*v2>(z)=0 off / on
 cv3_flag: 0, $
                              ; 0 / 1: enforce <rho*v3>(z)=0 off / on
 plt_flag: 1, $
                              ; -1 / 0 / 1: plotting off / bisectors off / on
                              ; create maps ICLAMO .. ICLAMm, m=map_flag
maps_flag: 1, $
                              ; 0 / 1: output of CC3(nx,ny,nx) off / on
cc3d_flag: 0, $
rdbb_flag: 0, $
                              ; 0 / 1: Read magnetic field, write SIR output
                              ; free pointers in structures at end of program
free_flag: 0, $
:-----
; General paths:
abupath: getenv('LINFOR3D_ABU'), $
         ; Path to abu files and atom.dat
         ; if not set, abupath is read from environment variable LINFOR3D_ABU
                                    ; directory with cached flow fields
ff_path: 'NONE', $
                                    'NONE': do not use cached flow fields
opapath: getenv('OPTABLES'), $ ; directory with opacity tables
gaspath: getenv('EOSTABLES'), $ ; directory with GAS tables
eospath: getenv('EOSTABLES'), $ ; directory with EOS tables
; Model data:
context: 'cobold', $
rhdpath: '/data/models/d3gt57g44n59/bigsel/', $ ; directory with model data
modelid: 'd3gt57g44n59.*.full', $ ; data file name
parfs: '/data/models/d3gt57g44n59/rhd.par', $ ; parameter file
xbcpath: '/data/models/d3gt57g44n59/NLTE3D/', $ ; directory of
                                                      departure coefficients
abuid: 'cifist2006', $ ; model abundance mixture, e.g. 'cifist2006' abuidx: 'special', $ ; spectrum abundance mixture, e.g. 'special' dmetal: 0.0, $ ; log10 scaling for metal abundances (Z>3)
dmetal: 0.0, $ dalpha: 0.0, $
                            ; log10 scaling for alpha elements
                                    (0, Ne, Mg, Si, S, Ar, Ca, Ti)
nx_skip: 5, ny_skip: 5, $ ; sampling in x, y (kiel, cobold only)
; more information (all read from parameter file for CO5BOLD)
opafile: 'undefined', $
gasfile: 'undefined', $
eosfile: 'undefined', $
teff: 5770.0, grav: 27500.0, $; grey, copenhagen, muram only
:-----
htau0: 0.0E0, $
                                  ; tau scale height; special 0 and negative
tsurffac: 0.0E0, $ ; Surface temperature = tsurffac*Teff
tsurffac: 0.0E0, $
; Reading of 'full' files (CO5BOLD only):
                   ; first snapshot to be read from full file(s)
isnap_full_1: 1, $
isnap_full_2: 9, $ ; last snapshot to be read from full file(s)
istep_full: 2, $ ; step for reading snapshots from full file(s)
```

7.13 IDL Example 59

```
; <3D> mean model:
mavg: 4, $; 1: T-average, 4: T^4-average for defining <3D> atmosphere
:-----
; External 1D reference model:
atmpath: '/data/models/d3gt57g44n59/lhdmodels/', $; directory of 1D
                                               reference model
atmfile: 'dxgt57g44n59.150', $
                                             ; name of reference model
                                               'NONE': no reference model
; Line data / radiative transfer:
linfs: 'line.dat', $ ; File with line data
lutau1: -7.0D0, lutau2: 2.0D0, dlutau: 8.0D-2, $ ; tau scale defining vertical
                                             model extent and resolution
lctau1: -7.0D0, lctau2: 2.0D0, dlctau: 8.0D-2, $; universal tau scale for
                                             integration of RT equation
ntheta: 3, nphi: 4, $ ; number of theta and phi angles mu0: 0.40, kphi: 0, $ ; view angle if ntheta=0 (cos theta,kphi*pi/2) n_chunk: 1, $ ; RT is done in n_chunk "slices"
; Curve-of-Growth control
       1,   ; -1 /   0 / 1: Custom CoG / CoG off / default CoG calculations
         51, \$ ; number of points to compute COG over (used when cog = -1)
icg:
gflgmin: -1.0, $ ; minimum delta log(gf) (used when cog = -1)
gflgmax: +1.5, $ ; maximum delta log(gf) (used when cog = -1)
;-----
; Balmer line computation control
Hbrd: 3,$
                            ; option for H line broadening
                            ; 0 - (default)
                            ; Cayrel&Traving (self res.) + Griem (Stark)
                            ; 1 - Ali-Griem (self res.) + Griem (Stark)
                            ; 2 - BPO (self res.) + Griem (Stark)
                             ; 3 - Allard 08 (self res.) + Griem (Stark)
                             ; 4 - Allard 08 (self res.) + Stehle (Stark)
                               using properly convolved tabulated profiles
                            ;
:-----
                           ; v sini (plot2); same for all spectra
vsini: 1.80, $
ximicx: 1.00, $
                            ; microturbulence [km/s], 1D-REF atmosphere
ximic1: 1.00, $
                            ; microturbulence [km/s], 1D-AVG atmosphere
ximic3: 0.00, $
                            ; microturbulence [km/s], 3D-RHD atmosphere
                            ; macroturbulence [km/s], 1D-REF atmosphere
ximacx: 1.60, $
ximac1: 1.60, $
                             ; macroturbulence [km/s], 1D-AVG atmosphere
                             ; macroturbulence [km/s], 3D-RHD atmosphere
ximac3: 0.00, $
                            ; fudge factor for 3D x-velocity
vfacx: 1.00, $
vfacy: 1.00, $
                            ; fudge factor for 3D y-velocity
vfacz: 1.00, $
                            ; fudge factor for 3D z-velocity
micro: 0, $
                             ; compute microturbulence sequence (0/1)
xi_a: 0.0, $
                             : microturbulence sequence start [km/s]
                             ; microturbulence sequence stop [km/s]
xi_b: 2.0,
           $
                             ; microturbulence delta sequence [km/s]
xi_d: 0.1,
            $
dclam: 0.0, $
                  ; variation of continuum from clam-dclam .. clam+dclam [A]
intmode: 1, $
                             ; integration mode (linfor_msint)
intline: 1 $
                             ; line integration: depth (1,2) / I (-1,-2)
end
```

7.14 F90 Example

```
; Linfor3D Fortran 90 only variables
; Output filename (optional)
outfile = 'linfor3D.uiosave'
; Printing options for UIO print outputs
                ; 0 UIO print out is supressed
printcobold = 0
                         ; 1 UIO if fully output
; Debug mode
debug
         = 0
                         ; (0 / 1) debugging model (off / on)
                         ; Used for parallelization scheme debugging
                         ; No serious computations are done.
    -----
; Program execution flag
; -3 - Compute the external 1D model atmosphere only
             ; -2 - Generate a 3x3 file for the external model atmosphere only
             ; -1 - Restore old results and compare with new 1D external model
                   (IDL-version only -- PLOTTING)
               0 - Restore old results, replace 1D external model
                   (IDL-version only)
               1 - Plotting input model structure on original vertical grid
                   (IDL-version only -- PLOTTING)
               2 - Plotting input model structure on refined vertical grid
                  (IDL-version only -- PLOTTING)
               3 - Compute RT for 3D, <3D>, and 1DX model atmospheres
                   (Default)
;------
; NLTE execution flag
;============
nlte_flag = 1 ; read XBC file departure coefficients
            ; 0 - No XBC files read. Everything is computed in LTE
                 (Default)
            ; 1 - Continuum & source function are LTE, line opacities are \mathtt{NLTE}
            ; 2 - Continuum & line opacities are LTE, source function is NLTE
            ; 3 - Continuum, source function & line opacities are NLTE
; Other program execution flags
wr3x3_flag = 1 ; (0 / 1) write the 1DX and global <3D> 3x3 models
wrtst_flag = 0 ; (0 / 1) write linfor_timing.txt
  d1_flag = 1; (0 / 1) create <3D> & global <3D> models for dort
 cv1_flag = 1; (0 / 1) enforce <rho*v1>(z)=0 off / on
 cv2_flag = 1; (0 / 1) enforce <rho*v2>(z)=0 off / on
 cv3_flag = 1 ; (0 / 1) enforce <rho*v3>(z)=0 off / on
             ;
                     create maps ICLAMO .. ICLAMm, m=map_flag
maps_flag = 1
cc3d_flag = 1; (0 / 1) Output of CC3(nx,ny,nx) off / on
rdbb_flag = 0 ; (0 - 2) Read magnetic field, write SIR output
```

7.14 F90 Example 61

```
;-----
; General paths
; Path to abu files and atom.dat
abupath = './' ; directory containing the .abu file
                     ; if 'LINFOR3D_ABU' then linfor3d looks at the shell
                      ; variable $LINFOR3D_ABU
opapath = 'OPTABLES'
                    ; directory with opacity tables
gaspath = 'EOSTABLES' ; directory with GAS tables
eospath = 'EOSTABLES' ; directory with EOS tables
; === IMPORTANT ===
; if the above paths are not set, they are read from system environments.
; Not set means missing or
; = 'OPTABLES', = 'EOSTABLES', = 'LINFOR3D_ABU', = 'NONE', = ''
; Input data
;========
context = 'cobold'
/ Shaps/usgts/g44n59/bigsel/'
modelid = 'd3gt57g44n59.*.full'
parfs = '~'cnan-'d2-'--
                                         ; directory with model data
                                              ; data file name(s)
parfs = '~/snaps/d3gt57g44n59/scripts/rhd.par'
                                              ; parameter file
xbcpath = '~/snaps/d3gt57g44n59/xbc/'
                                              ; directory of matching
                                              ; departure coefficients
abuid = 'cifist2006'
                      ; model abundance mixture 1 (Atmosphere abundances)
abuidx = 'special'
                        ; model abundance mixture 2 (Synthesis abundances)
dmetal = 0.0
                        ; log10 scaling for metal abundances (Z>3)
dalpha = 0.0
                         ; log10 scaling for alpha elements
                         ; (0, Ne, Mg, Si, S, Ar, Ca, Ti)
nx_skip = 5
ny_skip = 5
                      ; sampling in x, y (kiel, cobold only)
                         ; > 1 samples, < -1 interpolates
                         ; = 0,1 does nothing
; more information (all read from parameter file for CO5BOLD)
opafile = 'undefined'
gasfile = 'undefined'
eosfile = 'undefined'
teff = 5770.0
grav = 27500.0
                       ; grey, copenhagen, muram only
htau0 = 0.0E0
                        ; tau scale height; special 0 and negative
tsurffac = 0.0E0
                        ; Surface temperature = tsurffac*Teff
; <3D> mean model
;==========
           ; 1 - T-average, 4 - T^4-average for defining <3D> atmosphere
;-----
; External 1D reference model
```

```
atmpath = '~/snaps/d3gt57g44n59/lhdmodels/'
                                       ; directory of 1D
                                        ; reference model
atmfile = 't5780g44mm00ml3a10ob12_marcs.150' ; name of reference model
                                        ; 'NONE' - no reference model
; Line data / radiative transfer
linfs = 'line.dat' ; File with line data
lutau1 = -7.0D+0
lutau2 = 2.0D+0
dlutau = 8.0D-2
                      ; tau scale defining vertical
; model extent and resolution
lctau1 = -7.0D+0
1ctau2 = 2.0D+0
dlctau = 8.0D-2; universal tau scale for integration of RT equation
ntheta = 3
nphi = 4
                  ; number of theta and phi angles
     = 1.00
mu0
kphi = 0
                  ; view angle if ntheta=0 (cos theta,kphi*pi/2)
                  ; RT is done in n_chunk "slices"
n_{chunk} = 1
raybase = 'lobatto' ; mu-quadrature method
; Curve-of-Growth control
= 1 ; (-1 / 0 / 1) Custom CoG / CoG off / default CoG calculations
    = 51 ; number of points to compute COG over (used when cog = -1)
gflgmin = -1.0 ; minimum delta log(gf) (used when cog = -1)
gflgmax = +1.5; maximum delta log(gf) (used when cog = -1)
; Balmer line computation control
Hbrd = 3 ; Option for H line broadening
         ; 0 - (default) Cayrel & Traving (self res.) + Griem (Stark)
                Ali-Griem (self res.) + Griem (Stark)
         ; 1 -
                    BPO
         ; 2 -
                                   (self res.) + Griem (Stark)
                    Allard 08
                                 (self res.) + Griem (Stark)
(self res.) + Stehle (Stark)
         ; 3 -
                    Allard 08
         : 4 -
                                   using properly convolved tabulated
                                    profiles
; RT controls
:=========
             ; microturbulence [km/s], 1D-REF atmosphere
ximicx = 1.00
            ; microturbulence [km/s], 1D-AVG atmosphere
; microturbulence [km/s], 3D-RHD atmosphere
ximic1 = 1.00
ximic3 = 0.00
```

7.14 F90 Example 63

8 Line Data File: line.dat

There are several different formats (for historical reasons) to specify line data which are described in Sect. 8.2.

Note that all formats were extended in version 1.5.0 and now do have to contain the two lines

```
clam gfscale 2000.0 1.0
```

at the end. These parameters are explained in Sect. 8.1. Some helpful remarks concerning the conversion of line broadening parameters are given in Sect. 8.3.

A basic IDL program for creating a properly formatted line can be found in linfor_wrline.pro, within the Routines sub-directory within the Linfor3D directory tree.

8.1 Parameters in Line Data File

8.1.1 clam function : continuum wavelength in Å, also center of wavelength window required : always type : float values : e.g., 2000.0

clam defines the wavelength where the continuum opacities are computed, and also defines the center of the window for which spectrum synthesis is done. The window extends from λ =clam-dlam to λ =clam+dlam, depending on the value of dlam specified for the particular line.

From Version 3.1.2, a **negative** clam indicates that the continuum source function is to be set to the wavelength-integrated Planck-Function, $S = \sigma T^4/\pi$, and the continuum opacity is set to the Rosseland mean opacity, $\kappa_{\rm cont} = \kappa_{\rm Ross}$..

```
8.1.2 gfscale

function: global scaling factor for oscillator strengths
required: always
type: float
values: e.g., 1.0
```

Note: The value 1 has no effect. Useful when line.dat contains more than one transition.

8.2 Line Data Formats

8.2.1 Continuum only

It is possible to do pure continuum calculations. In this case, the line.dat file looks like this.

Example:

```
Some text header
1 1
Continuum, 2000 A
1 -1
clam gfscale
2000.0 1.0
```

8.2 Line Data Formats 65

Description of entries:

```
Row 1: Header (identifies the meaning of the columns for data in row 5)
Row 2: Two integers, kline and ktotal; both of them must be 1
Row 3: String, identifier of the continuum calculation
```

Row 4: Two integers, nbl = 1, incode = -1

Row 5: Description for data in row 6

Row 6: clam and gfscale (see Sect.8.1)

All the line parameters remain undefined.

8.2.2 Single line calculations, line data format '0'

For a **single unblended line**, the simplest form of the 'line.dat' file looks like this.

Example:

```
dlgC6
                                                      drrca1 dlam
                                                                     ddlam
Mult
       namj
                  ei
                          alam
                                    gflg
Fe I, 5500 A, 0.00 eV
0000
                 0.000
                          5500.0
                                                              5.5D-1 5.5D-3
       2600
                                    -6.000
                                                      10.0
                                             1.0
clam
         gfscale
2000.0
```

Description of entries:

```
Row 1: Header (identifies the meaning of the columns for data in row 5)
```

Row 2: Two integers, kline and ktotal

kline: number of line calculations requested in this file

ktotal: is the total number of spectral lines including blends

in this case kline = 1, ktotal = 1

Row 3: String, identifier of the (first) line calculation

Row 4: Integer *nbl*, integer array *incode*(*nbl*)

nb: number of blend components for this line calculation (= 1)

incode: integer array identifying the input format for each of the blend components (= 0)

Row 5: Line data in format '0' (7 + 2 columns):

C1: Multiplet number (for information only)

C2: Identifier of atom or ion (e.g. 2601 mean FeII)

C3: Excitation potential of lower level in [eV]

C4: Central wavelength of blend component

C5: $\log gf$ value of blend component

C6: $\Delta \log C_6$: Enhancement factor for van der Waals line broadening

C7: $\Delta \overline{r^2}/a_0^2$: Difference of mean square electron orbital radii

C8: $\Delta \lambda$ [Å]: Line profile is computed from $\lambda_0 - \Delta \lambda$ to $\lambda_0 + \Delta \lambda$

C9: $\delta\lambda$ [Å]: Spacing of wavelength points for spectrum synthesis

(C10: W_0 [mÅ]: total equivalent width of this blend, see below)

Row 6: Description for data in row 6

Row 7: clam and gfscale (see Sect.8.1)

In this case, the Stark broadening (due to collisions with electrons) is neglected ($C_4 = 0$). Radiative damping (γ_{rad}) is treated in the classical approximation.

In the case of a **single blended line** the 'line.dat' file looks as follows:

Example:

```
dlgC6
                                                       drrca1 dlam
                                                                        ddlam
Mult
       namj
                  ei
                           alam
                                     gflg
1
    2
Fe I, 0.00 eV + Fe II, 3.00 eV, 2000 A
2
    0 0
9999
       2600
                  0.000
                           2000.0
                                     -6.441
                                               1.0
                                                        10.0
                  3.000
                           2000.0
                                     -4.550
                                                        10.0
9999
       2601
                                               1.0
                                                                1.5D-1 1.5D-3
          gfscale
clam
2000.0
          1.0
```

Note that it is not necessary that the blend components belong to the same ion. Here kline = 1, ktotal = 2, nbl = 2, incode = [0, 0]. Note that only the last of the rows describing the blend need entries C8 and C9.

With a slight modification, it is possible to enter an **equivalent width** $(W_0 \text{ in } [\text{mÅ}])$ in column C10. For this purpose, nbl must be negative, with |nbl| being the number of blend components. The gf value producing this equivalent width W_0 is returned in result.gflg01 (average 3D atmosphere) and result.gflg0x (1D reference atmosphere).

Example unblended line:

```
Mult
      namj chik
                     alam
                               gflg
                                        dlgC6 drrca1 dlam
                                                                ddlam
                                                                            M0
 1 1
 N I Fictitious Line 1: /
                              0.000
                                       5500.0
                                                               10.00
                                                                       75.00 /
                                               -7.6914 1.00
-1 0
9999
       700
             0.000
                     5500.0 -7.6914
                                      1.00
                                              10.00 3.00E-01
                                                               3.00E-03
                                                                           75.00
clam
         qfscale
2000.0
         1.0
```

Example blended line:

```
Mult
                                        dlgC6 drrca1 dlam
                                                                            W0
       namj chik
                     alam
                                gflg
                                                                 ddlam
  1 2
Fe I, 0.00 eV + Fe II, 3.00 eV, 2000 A
 -2 0 0
9999
       2600
            0.000
                     2000.0
                               -6.441
                                        1.0
                                               10.0
9999
       2601 3.000
                     2000.0
                               -4.550
                                        1.0
                                               10.0
                                                    1.50D-1
                                                                1.50D-03
                                                                         100.00
         gfscale
clam
2000.0
         1.0
```

8.2.3 Single line calculations, line data format '1'

For a **single unblended line**, the this form of the 'line.dat' file looks like this.

Example:

```
Mult
                       alam
                                qflq
                                         dlqC6 lu diu lo
                                                             dio
                                                                  dlam
                                                                         ddlam
       namj
              ei
1
    1
O I ApJ Line 2: 92 6300.30
                              0.000 - 9.773
  92
       800
               0.000
                      6300.30 -9.773
                                               1
                                                   0.0
                                                       2
                                                             0.0 4.D-1 4.D-3
                                         1.0
clam
         gfscale
2000.0
         1.0
```

Description of entries:

8.2 Line Data Formats 67

```
Row 1: Header (identifies the meaning of the columns for data in row 5)
Row 2: Two integers, kline and ktotal
        kline: number of line calculations requested in this file
        ktotal: is the total number of spectral lines including blends
        in this case kline = 1, ktotal = 1
Row 3: String, identifier of the (first) line calculation
Row 4: Integer nbl, integer array incode(nbl)
        nb: number of blend components for this line calculation (= 1)
        incode: integer array identifying the input format for each of the blend components (= 1)
Row 5: Line data in format '1' (10 + 2 \text{ columns}):
        C1: Multiplet number (for information only)
        C2: Identifier of atom or ion (e.g. 2601 mean FeII)
        C3: Excitation potential of lower level in [eV]
        C4: Central wavelength of blend component
        C5: \log gf value of blend component
        C6: \Delta \log C_6: Enhancement factor for van der Waals line broadening
        C7: LU: Orbital quantum number of valence electron of lower level
        C8: DIU: excitation energy [eV] of parent term for lower level
        C9: LO: Orbital quantum number of valence electron of upper level
        C10: DIO: excitation energy [eV] of parent term for upper level
        C11: \Delta \lambda [Å]: Line profile is computed from \lambda_0 - \Delta \lambda to \lambda_0 + \Delta \lambda
        C12: \delta\lambda [Å]: Spacing of wavelength points for spectrum synthesis
        (C13: W_0 [mÅ]: total equivalent width of this blend, see below)
Row 6: Description for data in row 6
Row 7: clam and gfscale (see Sect.8.1)
```

In this case, $\Delta \overline{r^2}/a_0^2$ is computed from LU, DIU, LO, DIO (Function rrca). As before, the Stark broadening (due to collisions with electrons) is neglected ($C_4 = 0$). Radiative damping (γ_{rad}) is treated in the classical approximation.

In the case of a single blended line the 'line.dat' file looks as follows:

Example:

```
Mult
       namj
              ei
                      alam
                                gflg
                                         dlgC6 lu diu lo
                                                            dio
                                                                  dlam
                                                                          ddlam
O I ApJ Line 1: 67 6158.17 10.741 -1.140
    1 1 1
  67
       800
              10.741
                      6158.15
                               -1.985
              10.741
       800
                      6158.17
                               -1.140
                                         1.0
  67
              10.741
                      6158.19
                               -0.553
                                                                  4.D-1 4.D-3
         gfscale
clam
2000.0
```

Here kline = 1, ktotal = 3, nbl = 3, incode = [1, 1, 1]. Note that only the last of the rows describing the blend need entries C11 and C12.

As in the case of format '0', it is possible to enter an **equivalent width** $(W_0 \text{ in } [m\text{Å}])$ in column C13. For this purpose, nbl must be negative, with |nbl| being the number of blend components. The gf value producing this equivalent width W_0 is returned in result.gflg01 (average 3D atmosphere) and result.gflg0x (1D reference atmosphere).

Example unblended line:

```
Mult
       namj
            ei
                    alam
                             gflg
                                     dlgC6 lu diu lo
                                                        dio
                                                             dlam ddlam W0
 1 1
O I ApJ Line 2: 92
                    6300.30
                             0.000 - 9.773
  92
       800
             0.000
                    6300.30
                             -9.773 1.0
                                           1
                                               0.0
                                                    2
                                                             4.D-1 4.D-3 7.00
clam
         gfscale
2000.0
         1.0
```

Example blended line:

```
dlgC6 lu diu lo dio dlam ddlam W0
Mult
       namj
              ei
                    alam
                              gflg
    3
 1
O I ApJ Line 1: 67
                    6158.17 10.741 -1.140
   1 1 1
                             -1.985 1.0
       800
            10.741
                    6158.15
                                               0.0
                                                         0.0
  67
                                                    2
                                               0.0
  67
       800
            10.741
                    6158.17
                             -1.140 1.0
                                           1
                                                    2
                                                         0.0
  67
            10.741
                    6158.19
                             -0.5531.0
                                           1
                                               0.0
                                                    2
                                                         0.0
                                                              4.D-1 4.D-3 10.00
         gfscale
clam
2000.0
         1.0
```

8.2.4 Single line calculations, complete line data format '2'

For a **single unblended line**, the this form of the 'line.dat' file looks like this.

Example:

```
Mult
                                       dlgC6 drrca1 dlgC4 C4lg
                      alam
                                gflg
                                                                    dlggr Crad
                                                                                dlam
                                                                                        ddl am
       nami
              ei
    1
Si I AA Line 5: 16
                     5948.540
                               5.0823
                                       -1.130
                                                390.03
                                                          11.80
    2
   16
       1400
              5.0823
                      5948.540 -1.130 1.0
                                              390.03 0.0
                                                             11.80 0.0
                                                                           -1.0 5.D-1 5.D-3
clam
         gfscale
2000.0
         1.0
```

Description of entries:

```
Row 1: Header (identifies the meaning of the columns for data in row 5)
```

Row 2: Two integers, kline and ktotal

kline: number of line calculations requested in this file

ktotal: is the total number of spectral lines including blends

in this case kline = 1, ktotal = 1

Row 3: String, identifier of the (first) line calculation

Row 4: Integer *nbl*, integer array *incode*(*nbl*)

nb: number of blend components for this line calculation (= 1)

incode: integer array identifying the input format for each of the blend components (= 2)

Row 5: Line data in format '2' (11 + 2 columns):

C1: Multiplet number (for information only)

C2: Identifier of atom or ion (e.g. 2601 mean FeII)

C3: Excitation potential of lower level in [eV]

C4: Central wavelength of blend component

C5: log gf value of blend component

C6: $\Delta \log C_6$: Enhancement factor for van der Waals line broadening

C7: $\Delta r^2/a_0^2$: Difference of mean square electron orbital radii

C8: $\Delta \log C_4$: Enhancement factor for Stark line broadening

C9: $-\log C_4$: Stark broadening constant.

8.2 Line Data Formats 69

```
if -\log C_4 = 0, then use Griem (Phys. Rev. 165, 258, 1968) and Cowley (Obs. 91, 139, 1971) approximation if -\log C_4 < 0 (typically -\log C_4 = -1.0), then C_4 = 0 C10: \Delta\log\gamma_{\rm rad}: Enhancement factor for natural line broadening C11: C_{\rm rad}: Natural line broadening (10^{-8}\gamma_{\rm rad}) if C_{\rm rad} < 0, use classical formula (\gamma_{\rm rad} = 2.22 \cdot 10^{15}/\lambda^2) [rad/s], where \lambda is in Å. C12: \Delta\lambda [Å]: Line profile is computed from \lambda_0 - \Delta\lambda to \lambda_0 + \Delta\lambda C13: \delta\lambda [Å]: Spacing of wavelength points for spectrum synthesis (C14: W_0 [mÅ]: total equivalent width of this blend, see below) Row 6: Description for data in row 6 Row 7: clam and gfscale (see Sect.8.1)
```

In the case of a **single blended line** the 'line.dat' file looks as follows:

Example:

```
dlgC6 drrca1 dlgC4 C4lg
                                                                                       ddlam
Mult
       namj
              ei
                      alam
                               gflg
                                                                   dlggr Crad dlam
Si I / Si II blend: 16
                         5948.540 5.0823 -1.130 390.03
                                                             11.80
                                                                   -1
                      5948.540 -1.130
                                             390.03
   16 1400
                                       1.0
                                                     0.0
                                                            11.80
                                                                   0.0
                                                                          -1.0
              5.0823
              0.0823 5948.530 -3.130
                                              90.00
                                                            13.80
                                                                          -1.0
                                                                               5.D-1 5.D-3
   16
      1401
                                       1.0
                                                     0.0
clam.
         gfscale
2000.0
```

Here kline = 1, ktotal = 2, nbl = 2, incode = [2, 2, 2]. Note that only the last of the rows describing the blend need entries C12 and C13.

As in the cases of format '0' and '1', it is possible to enter an **equivalent width** $(W_0 \text{ in } [mÅ])$ in column C14. For this purpose, nbl must be negative, with |nbl| being the number of blend components. The gf value producing this equivalent width W_0 is returned in result.gflg01 (average 3D atmosphere) and result.gflg0x (1D reference atmosphere). No examples are given since the necessary modification the data format should be obvious.

8.2.5 Single line calculations, complete line data format '3'

This data format has a maximum of 17 columns. It differs from format '2' only in the way the van der Waals broadening parameters are specified. Columns C7 with $\Delta r^2/a_0^2$ is replaced by the four columns:

```
C7: LU: Orbital quantum number of valence electron of lower level C8: DIU: excitation energy [eV] of parent term for lower level C9: LO: Orbital quantum number of valence electron of upper level C10: DIO: excitation energy [eV] of parent term for upper level
```

as in format '1'. The remaining columns are as in format '2', but shifted by +3:

```
C11: Δ log C<sub>4</sub>: Enhancement factor for Stark line broadening
C12: -log C<sub>4</sub>: Stark broadening constant.

if log C<sub>4</sub> = 0, then use Griem (Phys. Rev. 165, 258, 1968)

and Cowley (Obs. 91, 139, 1971) approximation

if -log C<sub>4</sub> < 0 (typically -log C<sub>4</sub> = -1.0), then C<sub>4</sub> = 0
C13: Δ log γ<sub>rad</sub>: Enhancement factor for natural line broadening
C14: C<sub>rad</sub>: Natural line broadening (10<sup>-8</sup> γ<sub>rad</sub>)

if C<sub>rad</sub> < 0, use classical formula (γ<sub>rad</sub> = 2.22 · 10<sup>15</sup>/λ²) [rad/s], where λ is in Å.
```

C15: $\Delta\lambda$ [Å]: Line profile is computed from $\lambda_0 - \Delta\lambda$ to $\lambda_0 + \Delta\lambda$ C16: $\delta\lambda$ [Å]: Spacing of wavelength points for spectrum synthesis (C17: W_0 [mÅ]: total equivalent width of this blend, see below)

As in the cases of format '0', '1', and '2' it is also possible to enter an **equivalent width** (W_0 in [mÅ]), now in column C17. For this purpose, nbl must be negative, with |nbl| being the number of blend components. The gf value producing this equivalent width W_0 is returned in result.gflg01 (average 3D atmosphere) and result.gflg0x (1D reference atmosphere).

8.2.6 Single line calculations, complete line data format '4'

This data format has a maximum of 14 columns. It differs from format '2' only in the way the van der Waals broadening parameter is specified. Column C7 with $\Delta \overline{r^2}/a_0^2$ is replaced by the parameter – log C_6 .

C7: $-\log C_6$: negative logarithmic van der Waals broadening parameter C_6

The remaining columns are as in format '2'.

```
C8: \Delta \log C_4: Enhancement factor for Stark line broadening C9: -\log C_4: Stark broadening constant. if \log C_4 = 0, then use Griem (Phys. Rev. 165, 258, 1968) and Cowley (Obs. 91, 139, 1971) approximation if -\log C_4 < 0 (typically -\log C_4 = -1.0), then C_4 = 0 (no Stark broadening) C10: \Delta \log \gamma_{\rm rad}: Enhancement factor for natural line broadening C11: C_{\rm rad}: Natural line broadening (10^{-8}\gamma_{\rm rad}) if C_{\rm rad} < 0, use classical formula (\gamma_{\rm rad} = 2.22 \cdot 10^{15}/\lambda^2) [rad/s], where \lambda is in Å. C12: \Delta \lambda [Å]: Line profile is computed from \lambda_0 - \Delta \lambda to \lambda_0 + \Delta \lambda C13: \delta \lambda [Å]: Spacing of wavelength points for spectrum synthesis (C14: W_0 [mÅ]: total equivalent width of this blend, see above)
```

Example:

6707.840

5.0119

```
ei
                        alam
                                                dlgC6 C6log
                                                                                   dlggr Crad
                                                                                                         dd]
Mult
                                     gflg
                                                                 dlgC4 C4log
                                                                                               dlam
       namj
1 12
Li7, 6 components Li6, 6 components: glog=-0.427905 .. -0.831310
   4 4 4 4 4 4 4 4 4 4 4 4
9999
       0300.7
                        6707.7560
                                    -0.427905
                                                0.84
                                                       31.3843
                                                                 0.0
                0.00
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.7
                                    -0.206158
                                                        31.3843
                                                                         14.1505
                                                                                         -1.0
                0.00
                        6707.7680
                                                0.84
                                                                 0.0
                                                                                   0.0
9999
       0300.7
                0.00
                        6707.9070
                                    -0.808148
                                                0.84
                                                       31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.7
                0.00
                        6707.9080
                                    -1.507150
                                                0.84
                                                       31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.7
                0.00
                        6707.9190
                                    -0.808148
                                                0.84
                                                       31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.7
                        6707.9200
                                    -0.808148
                                                0.84
                                                        31.3844
                                                                         14.1505
                0.00
                                                                 0.0
                                                                                   0.0
                                                                                         -1.0
9999
       0300.6
                0.00
                        6707.9200
                                    -0.478953
                                                0.84
                                                        31.3844
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
                                                                 0.0
9999
       0300.6
                0.00
                        6707.9230
                                    -0.178176
                                                0.84
                                                       31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.6
                0.00
                        6708.0690
                                    -0.831310
                                                0.84
                                                       31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
       0300.6
                0.00
                        6708.0700
                                    -1.734310
                                                0.84
                                                        31.3844
                                                                 0.0
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
9999
                0.00
                        6708.0740
                                    -0.734310
                                                0.84
                                                        31.3844
                                                                         14.1505
       0300.6
                                                                 0.0
                                                                                   0.0
                                                                                         -1.0
9999
                0.00
                        6708.0750
                                   -0.831310
                                               0.84
                                                        31.3844
                                                                         14.1505
                                                                                   0.0
                                                                                         -1.0
                                                                                                10.D-1
       0300.6
                                                                 0.0
clam
         gfscale
```

8.2 Line Data Formats 71

8.2.7 Single line calculations, complete line data format '5'

This data format has a maximum of 15 columns. It differs substantially form format '4': (i) an extra column is inserted that allows the specification of $\log gf$ offsets; (ii) the van der Waals broadening is specified by $\log \gamma_6$ instead of $-\log C_6$; (iii) the Stark broadening is specified by $\log \gamma_4$ instead of $-\log C_4$; (iv) the natural broadening is specified by $\log \gamma_{\rm rad}$ instead of $\gamma_{\rm rad}/10^8$. More precisely, column C5-C15 have the following meaning in format '5':

```
C5: \Delta \log gf: Correction factor for the line's \log gf value
```

C6: $\log qf$: the line's logarithmic qf value

C7: $\Delta \log \gamma_6$: Enhancement factor for van der Waals γ parameter

C8: $\log \left(\frac{\gamma_6 (T=10^4)}{N_{\rm H}} \right)$: logarithmic van der Waals broadening parameter $\gamma_6/N_{\rm H}$ at $T=10^4$ K.

C9: $\Delta \log \gamma_4$: Enhancement factor for Stark γ parameter

C10: $\log \left(\frac{\gamma_4 (T=10^4)}{N_e} \right)$: logarithmic Stark broadening parameter γ_4/N_e at $T=10^4$ K. if $\log \gamma_4/N_e \ge 0$, then use Griem (Phys. Rev. 165, 258, 1968) and Cowley (Obs. 91, 139, 1971) approximation

C11: $\Delta \log \gamma_{\rm rad}$: Enhancement factor for the natural line broadening

C12: $\log \gamma_{\text{rad}}$: Natural line broadening ($\log \gamma_{\text{rad}}$ [rad/s])

if $\log \gamma_{\rm rad} \ge 99.0$, use classical formula $(\gamma_{\rm rad} = 2.22 \cdot 10^{15}/\lambda^2)$ [rad/s], where λ is in Å.

C13: $\Delta\lambda$ [Å]: Line profile is computed from $\lambda_0 - \Delta\lambda$ to $\lambda_0 + \Delta\lambda$

C14: $\delta\lambda$ [Å]: Spacing of wavelength points for spectrum synthesis

(C15: W_0 [mÅ]: total equivalent width of this blend, see above)

Example:

```
Mult
              ei
                     alam
                                dlggf gflg
                                                 dlgg6
                                                        g6log
                                                                dlgg4
                                                                        g4log
                                                                                 dlggr grlog dlam
                                                                                                     ddlam
1 12
Li7, 6 components Li6, 6 components: glog=-0.427905 .. -0.831310
12 5 5 5 5 5 5 5 5 5 5 5 5
                                                                                       99.0
9999
      0300.7
              0.00
                     6707.7560
                                0.00 -0.427905 2.10 -7.94973
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
9999
      0300.7 0.00
                     6707.7680 0.00 -0.206158 2.10 -7.94974
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
9999
      0300.7
                     6707.9070 0.00 -0.808148 2.10 -7.94975
                                                                       -5.7800
                                                                                       99.0
              0.00
                                                                0.00
                                                                                 0.0
9999
      0300.7 0.00
                     6707.9080 0.00 -1.507150 2.10 -7.94975
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
9999
      0300.7
              0.00
                     6707.9190 0.00 -0.808148 2.10 -7.94975
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
                     6707.9200 0.00 -0.808148 2.10
9999
      0300.7
              0.00
                                                      -7.94975
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
9999
      0300.6
             0.00
                     6707.9200 0.00 -0.478953 2.10
                                                      -7.94975
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
9999
      0300.6 0.00
                     6707.9230 0.00 -0.178176 2.10 -7.94975
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
                                                                0.00
9999
      0300.6 0.00
                     6708.0690 0.00 -0.831310 2.10 -7.94976
                                                                       -5.7800
                                                                                 0.0
                                                                                       99.0
                                                                                 0.0
9999
      0300.6 0.00
                     6708.0700 0.00 -1.734310 2.10 -7.94976
                                                                0.00
                                                                       -5.7800
                                                                                       99.0
                     6708.0740 0.00 -0.734310 2.10 -7.94976
                                                                                       99 0
9999
      0300.6 0.00
                                                                0.00
                                                                       -5.7800
                                                                                 0.0
                     6708.0750 0.00 -0.831310 2.10 -7.94976
                                                                       -5.7800
                                                                                       99.0 10.D-1 5.D-3
      0300.6 0.00
                                                                0.00
                                                                                 0.0
9999
        gfscale
clam
6707.840 5.0119
```

8.2.8 Single line calculations, complete line data format '6'

This data format also has a maximum of 15 columns. It differs from format '5' only in the way the van der Waals broadening parameters are specified. In format '6', column C7–C8 have the following meaning:

C7: σ_{ABO} : van der Waals broadening cross section in atomic units at $v_0 = 10$ km/s according ABO theory C8: α_{ABO} : α parameter of ABO theory defining the velocity (temperature) dependence of the cross section σ .

The remaining columns C9-C15 are as in format '5'. Note that:

• no enhancement factor for van der Waals broadening is foreseen in this line data format.

• the temperature dependence of the broadening cross section is correctly taken into account according to the ABO theory when this line data format is used.

Example:

```
Mult
                                   dlggf gflg
                                                                                            dlggr grlog dlam
                                                                                                                 ddla
       nami
                       alam
                                                     s_abo
                                                                a_abo
                                                                         dlgg4
                                                                                  g4log
1 12
Li7, 6 components Li6, 6 components: glog=-0.427905 .. -0.831310
12 6 6 6 6 6 6 6 6 6 6 6
                                                                                                  99.0
9999
       0300.7 0.00
                       6707.7560
                                   0.00
                                         -0.427905
                                                     355.909
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                           0.0
       0300.7
                                                                                                  99.0
9999
               0.00
                       6707.7680
                                         -0.206158
                                                     355.900
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                   0.00
                                                                                           0.0
9999
       0300.7
               0.00
                       6707.9070
                                         -0.808148
                                                                0.40000
                                                                                 -5.7800
                                                                                                  99.0
                                   0.00
                                                     355.892
                                                                         0.00
                                                                                           0.0
9999
       0300.7
               0.00
                       6707.9080
                                         -1.507150
                                                     355.892
                                                                                                  99.0
                                   0.00
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                           0.0
9999
       0300.7
               0.00
                       6707.9190
                                   0.00
                                         -0.808148
                                                     355.892
                                                                0.40000
                                                                         0.00
                                                                                                  99.0
                                                                                 -5.7800
                                                                                           0.0
9999
       0300.7
               0.00
                       6707.9200
                                   0.00
                                         -0.808148
                                                     355.892
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                           0.0
                                                                                                  99.0
9999
       0300.6
               0.00
                       6707.9200
                                   0.00
                                         -0.478953
                                                     355.892
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                            0.0
                                                                                                  99.0
9999
       0300.6
               0.00
                       6707.9230
                                   0.00
                                         -0.178176
                                                     355.892
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                            0.0
                                                                                                  99.0
9999
       0300.6
               0.00
                       6708.0690
                                   0.00
                                         -0.831310
                                                     355.894
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                            0.0
                                                                                                  99.0
9999
       0300.6
               0.00
                       6708.0700
                                   0.00
                                         -1.734310
                                                     355.894
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                           0.0
                                                                                                  99.0
9999
       0300.6
               0.00
                       6708.0740
                                   0.00
                                         -0.734310
                                                     355.894
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                           0.0
                                                                                                  99.0
9999
                       6708.0750
                                                     355.894
                                                                0.40000
                                                                         0.00
                                                                                 -5.7800
                                                                                                  99.0
                                                                                                        10.D-1 5.D-
       0300.6
               0.00
                                   0.00
                                         -0.831310
                                                                                           0.0
clam
         gfscale
6707.840 5.0119
```

8.2.9 Single line calculations, complete line data format '7'

This data format was designed for simple test calculations where the line profile is fixed, i.e. the line parameters are depth-independent (see also Sect. 3.5). This format has a maximum of 7 columns:

Description of entries:

```
Row 1: Header (identifies the meaning of the columns for data in row 5)
Row 2: Two integers, kline and ktotal
        kline: number of line calculations requested in this file
        ktotal: is the total number of spectral lines including blends
        in this case kline = 1, ktotal = 1
Row 3: String, identifier of the line calculation
Row 4: Integer nbl, integer array incode(nbl)
        nb: number of blend components for this line calculation (= 1)
        incode: integer array identifying the input format for each of the blend components (= 7)
Row 5: C1: Central wavelength of blend component [Å]
        C2: Doppler broadening in units of c, v_D/c
        C3: \eta_0 = \kappa_{\text{line}}/\kappa_{\text{cont}} at line center
        C4: \alpha-parameter for Voigt profile, \alpha = \gamma/2/\Delta\omega_D
             (ratio of half half width of dispersion profile and Doppler widths of Gaussian).
        C5: \Delta \lambda [Å]: Line profile is computed from \lambda_0 - \Delta \lambda to \lambda_0 + \Delta \lambda
        C6: \delta\lambda [Å]: Spacing of wavelength points for spectrum synthesis
        (C7: W_0 [mÅ]: total equivalent width of this blend, see above)
Row 6: Description for data in row 6
```

Example:

```
alam Vdop eta0 avgt dlam ddlam
1 1
Test grey sf Vdop=2.D-5, eta0=1.0D0, avgt=1.D-2
1 7
```

Row 7: clam and gfscale (see Sect.8.1)

8.2 Line Data Formats 73

```
4000.000 2.0D-5 1.0D0 1.0D-2 0.90D0 0.90D-2 clam gfscale -4000.000 1.0
```

8.2.10 Multiple Line Calculations

It is also possible to process a whole set of lines in a single run. The requirement is, however, that all lines have the same central wavelength (continuum wavelength). This mode was designed for parameter studies, e.g. investigating the "granulation abundance corrections" as a function of line excitation potential.

Example, 8 unblended N I lines of different excitation potential:

```
Mult
                                               drrca1 dlam
                                                                  ddlam
                                                                             W0
       namj chik
                      alam
                                gflg
                                        dlgC6
  8
 N I Fictitious Line
                       1: /
                               0.000
                                        5500.0
                                                -7.6914
                                                         1.00
                                                                 10.00
                                                                         75.00 /
 -1
9999
             0.000
                      5500.0
                              -7.6914
                                               10.00 3.00E-01
       700
                                       1.00
                                                                 3.00E-03
                                                                            75.00
 N I Fictitious Line
                       2: /
                               2.000
                                        5500.0
                                                -5.7282
                                                         1.00
                                                                 10.00
                                                                         75.00 /
 -1
9999
       700
             2.000
                      5500.0
                              -5.7282
                                        1.00
                                               10.00 3.00E-01
                                                                 3.00E-03
                                                                            75.00
                                               -3.8298
                                                                         75.00 /
 N I Fictitious Line
                       3: /
                               4.000
                                        5500.0
                                                        1.00
                                                                 10.00
 -1
9999
       700
             4.000
                      5500.0
                              -3.8298
                                        1.00
                                               10.00 3.00E-01
                                                                 3.00E-03
                                                                            75.00
 N I Fictitious Line 4: /
                               6.000
                                        5500.0
                                                -1.9876
                                                                 10.00
                                                                         75.00 /
                                                         1.00
 -1
9999
       700
             6.000
                      5500.0
                              -1.9876
                                        1.00
                                               10.00 3.00E-01
                                                                 3.00E-03
                                                                            75.00
 N I Fictitious Line
                               8.000
                                        5500.0
                                                -0.1961
                        5: /
                                                         1.00
                                                                 10.00
                                                                         75.00 /
 -1
9999
       700
             8.000
                      5500.0
                              -0.1961
                                               10.00 3.00E-01
                                                                 3.00E-03
                                                                            75.00
                                        1.00
 N I Fictitious Line
                       6: /
                              10.000
                                        5500.0
                                                 1.5485
                                                         1.00
                                                                 10.00
                                                                         75.00 /
 -1
9999
       700 10.000
                      5500.0
                               1.5485
                                        1.00
                                               10.00
                                                     3.00E-01
                                                                            75.00
                                                                 3.00E-03
                              11.000
 N I Fictitious Line
                       7: /
                                        5500.0
                                                 2.4046
                                                         1.00
                                                                 10.00
                                                                         75.00 /
 -1 0
9999
                      5500.0
                               2.4046
                                               10.00
                                                      3.00E-01
                                                                            75.00
       700 11.000
                                        1.00
                                                                 3.00E-03
                              12.000
                                                                         75.00 /
 N I Fictitious Line 8: /
                                        5500.0
                                                 3.2510
                                                         1.00
                                                                 10.00
 -1
9999
       700 12.000
                      5500.0
                               3.2510
                                       1.00
                                               10.00
                                                     3.00E-01 3.00E-03
                                                                            75.00
clam
         gfscale
2000.0
         1.0
```

Note that now kline = 8, and ktotal = 8, since all lines have one blend component only.

8.3 Conversion of line broadening parameters

The line broadening can be specified in different ways, e.g. as $-\log C_4$ for quadratic Stark broadening. The required data is, however, not always available and must be converted from other broadening parameters, e.g. γ_4 . In the particular case of the *Vienna Atomic Line Database* the broadening is provided as $\log(\gamma_4/N_e)$ for a temperature of $T = 10^4$ K.

Please note that here and in Linfor3D in general, the parameters C_n (n = 4, 6) are defined via

$$\Delta\omega = \frac{C_n}{r^n} \tag{79}$$

whereas the definition by Unsöld is

$$\Delta\omega = 2\pi \frac{C_n}{r^n}. (80)$$

The Linfor parameters C_n are thus a factor 2π larger than in the definition by Unsöld.

Note that γ_{rad} , γ_4 , γ_6 measure the **full** width at half maximum of the Lorentzian profile in units of rad/s.

8.3.1 Quadratic Stark effect

The broadening parameter γ_4 for the quadratic Stark effect can be written as

$$\gamma_4 = 11.37 C_4^{2/3} v_{\text{rel}}^{1/3} N_e ,$$
 (81)

where $v_{\rm rel}$ is the relative velocity between the regarded atom and the perturber, i.e. the colliding particle:

$$v_{\rm rel}^2 = \frac{8 k T}{\pi m_{\rm H}} \cdot (\frac{1}{A_1} + \frac{1}{A_2}) \ .$$
 (82)

 A_1 and A_2 are the atomic weights in atomic mass units, e.g., $A_2 = 1$ for a colliding hydrogen atom and $A_1 \approx 56$ for iron atoms and $A_2 = 1/1837 = m_e/m_H$ for electrons. For Stark broadening with electrons as perturbers the following good approximation can be made:

$$A_1 >> A_2 \Rightarrow \frac{1}{A_1} + \frac{1}{A_2} \approx \frac{1}{A_2} = 1837 = m_{\rm H}/m_{\rm e}$$
 (83)

With this Eq. 81 can be written as

$$\log \frac{\gamma_4}{N_2} = \log 11.37 + \log C_4^{2/3} + \log v_{\text{rel}}^{1/3}$$
 (84)

$$= 1.056 + \frac{2}{3}\log C_4 + \frac{1}{6}\log \frac{8kT}{\pi m_e}$$
 (85)

$$= 1.056 + \frac{2}{3}\log C_4 + 1.931 + \frac{1}{6}\log T \tag{86}$$

$$= 1.056 + \frac{2}{3}\log C_4 + 1.931 + \frac{1}{6}\log 10^4 + \frac{1}{6}\log \frac{T}{10^4 \text{ K}}$$
 (87)

(88)

With $T = 10^4$ K, which is assumed for data in VALD, we derive

$$\log \frac{\gamma_4}{N_e} = 3.654 + \frac{2}{3} \log C_4 \tag{89}$$

and finally the conversion formula:

$$\log C_4 = 1.5 \log \frac{\gamma_4}{N_e} - 5.4805 \tag{90}$$

For instance a value of -5.491 from VALD gives $\log C_4 = -13.717$. The parameter C41g is thus set to 13.717.

8.3.2 Van der Waals broadening

The broadening parameter γ_6 for the van der Waals effect can be written as

$$\gamma_6 = 8.08 C_6^{2/5} v_{\rm rel}^{3/5} N_{\rm H} . \tag{91}$$

The perturbing particles are mostly hydrogen atoms with $A_2 = 1$. We now make the approximation

$$A_1 > A_2 \Rightarrow \frac{1}{A_1} + \frac{1}{A_2} \approx \frac{1}{A_2} = 1$$
 (92)

With this the relative velocity of the particles (Eq. 82) reduces to

$$v_{\rm rel}^2 = \frac{8 k T}{\pi m_{\rm H}}.$$
 (93)

We can thus rewrite Eq. 91:

$$\log \frac{\gamma_6}{N_{\rm H}} = \log 8.08 + \log C_6^{2/5} + \log v_{\rm rel}^{3/5} \tag{94}$$

$$= 0.907 + \frac{2}{5}\log C_6 + \frac{3}{10}\log \frac{8kT}{\pi m_{\rm H}}$$
 (95)

$$= 0.907 + \frac{2}{5}\log C_6 + 2.497 + \frac{3}{10}\log T \tag{96}$$

$$= 0.907 + \frac{2}{5}\log C_6 + 2.497 + \frac{3}{10}\log 10^4 + \frac{3}{10}\log \frac{T}{10^4 \,\mathrm{K}}$$
 (97)

(98)

With $T = 10^4$ K, which is assumed for data in VALD, we derive

$$\log \frac{\gamma_6}{N_{\rm H}} = 4.604 + \frac{2}{5} \log C_6 \tag{99}$$

and finally the conversion formula:

$$\log C_6 = 2.5 \log \frac{\gamma_6}{N_{\rm H}} - 11.510 \tag{100}$$

For instance a value of -7.619 from VALD gives $\log C_6 = -30.558$. Before Linfor3D Version 6.5.0, neither the parameter γ_6 nor the parameter C6log= $-\log C_6$ could be specified in the line data file directly. Instead the van der Waals broadening had to be specified via the difference of mean square electron orbital radii $\Delta r^2/a_0^2$, where a_0 is the Bohr radius:

$$\log\left(\Delta \overline{r^2}/a_0^2\right) = \log C_6 + 32.3867 \ . \tag{101}$$

The necessary relation for the conversion between $(\Delta \overline{r^2}/a_0^2)$ and γ_6 is:

$$\Delta \overline{r^2}/a_0^2 = 10^{20.877 + 2.5 \log \frac{\gamma_6}{N_{\rm H}}} . \tag{102}$$

The exemplary value of -7.619 from VALD thus gives 67.437 for the parameter drrca1. In addition dlgC6 should be set to 0 unless you want to apply an additional enhancement of the broadening.

Since Linfor3D Version 6.5.0, line data format '4' and '5' allows to enter directly the parameter C6log or $\gamma_6/N_{\rm H}$, respectively.

8.3.3 ABO van der Waals broadening formalism

In the van der Waals broadening formalism of Anstee, Barklem, and O'Mara, γ_6 is computed as

$$\frac{w}{N_{\rm H}} = \frac{\gamma_6}{2N_{\rm H}} = \sigma_{\rm ABO} a_0^2 \left(\frac{4}{\pi}\right)^{\alpha_{\rm ABO}/2} \Gamma(2 - \alpha_{\rm ABO}/2) v_0 \left(\frac{v_{\rm rel}}{v_0}\right)^{1 - \alpha_{\rm ABO}} , \tag{103}$$

where w is the **half** half width in rad s⁻¹, σ_{ABO} and α_{ABO} are the two tabulated quantities of the ABO line broadening theory, Γ denotes the mathematical Γ -function. The parameter σ_{ABO} is the broadening cross section at relative velocity $v_0 = 10 \, \text{km/s}$ between the perturbing hydrogen atom and the atom of interest in atomic units. The factor a_0^2 (a_0 is the Bohr radius) converts the cross section to units of cm². v_{rel} is the mean relative velocity averaged over the Maxwellian velocity distribution as given by Eq. 82.

The parameter α_{ABO} describes the velocity dependence of the broadening cross section

$$\sigma_{\text{ABO}}(v) = \sigma_{\text{ABO}}(v_0) \left(\frac{v}{v_0}\right)^{-\alpha_{\text{ABO}}}$$
 (104)

For details see, e.g., Barklem, Anstee and O'Mara, Publ. Astron. Soc. Aust., 1998, 15, 336–8. Numerically, we obtain

$$\log \frac{\gamma_6}{N_{\rm H}} = \log \sigma_{\rm ABO} + 0.052455\alpha_{\rm ABO} + \log \Gamma (2 - \alpha_{\rm ABO}/2) + (1 - \alpha_{\rm ABO}) \log \left(\frac{v_{\rm rel}}{v_0}\right) - 10.25177. \quad (105)$$

This relation may be compared to the classical van der Waals formula (Eq.94) which may be rewritten as

$$\log \frac{\gamma_6}{N_{\rm H}} = 0.4 \log C_6 + 0.6 \log \left(\frac{v_{\rm rel}}{v_0}\right) + 4.5074114. \tag{106}$$

We can convert the ABO parameters σ_{ABO} and α_{ABO} to C_6 by requiring the two expressions (105) and (106) to yield identical results for $\gamma_6(v_{\rm rel} = v_0) = \gamma_6(T \approx 4760 \, {\rm K})$:

$$\log C_6 = 2.5 \log \sigma_{ABO} + 0.1311376 \alpha_{ABO} + 2.5 \log \Gamma (2 - \alpha_{ABO}/2) - 36.89795. \tag{107}$$

For $\sigma_{ABO} = 530$, $\alpha_{ABO} = 0.277$, we obtain $\log C_6 = -30.1076$.

If we choose a different reference velocity, v^* , for matching both expressions, we obtain

$$\log C_6 = 2.5 \log \sigma_{\text{ABO}} + 0.1311376 \alpha_{\text{ABO}} + 2.5 \log \Gamma (2 - \alpha_{\text{ABO}}/2) + \left(1 - \frac{5}{2} \alpha_{\text{ABO}}\right) \log \frac{v^*}{v_0} - 36.89795.$$
(108)

This relation shows that, for $\alpha_{ABO}=2/5$, ABO and Linfor3D can be matched to give identical γ_6 for arbitrary temperatures. In Linfor3D we choose $v^*=14.495$ km/s, corresponding to $T\approx 10^4$ K. Then $\log(v^*/v_0)=0.1612$.

On the other hand, any C_6 can be uniquely converted to σ_{ABO} and α_{ABO} :

$$\log \sigma_{ABO} = 0.4 \log C_6 + 14.76906834$$
 , $\alpha_{ABO} = 2/5$. (109)

For example, $\log C_6 = -30.1076$ implies $\log \sigma_{ABO} = 2.7260324$ or $\sigma_{ABO} = 532.15$.

For use in Linfor3D, we rewrite Eq. (105) as

$$\log \frac{\gamma_6}{10^8} = \log \sigma_{ABO} + \frac{1 + \alpha_{ABO}}{2} \log \theta + \log P_{H} + F(\alpha_{ABO}), \tag{110}$$

where $\theta = 5039.67/T$, $P_{\rm H} = N_{\rm H} k T$ is the partial pressure of neutral hydogen atoms, and

$$F(\alpha_{ABO}) = c_1 \alpha_{ABO} + \log \Gamma (2 - \alpha_{ABO}/2) - (1 - \alpha_{ABO}) \log v_0 + \frac{1 - \alpha_{ABO}}{2} c_2 - \frac{1 + \alpha_{ABO}}{2} c_3 + c_4,$$
(111)

or

$$F(\alpha_{ABO}) = \log \Gamma (2 - \alpha_{ABO}/2) + f_1 \alpha_{ABO} + f_2, \qquad (112)$$

with the constants

$$v_0 = 10^6 \text{ [cm/s]},$$
 (113)

$$a_0 = 5.2917725 \, 10^{-09}$$
, Bohr radius [cm], (114)

$$c_1 = \frac{1}{2} \log \left(\frac{4}{\pi} \right) = 0.052455,$$
 (115)

$$c_2 = \log\left(\frac{8}{\pi m_{\rm H}}\right) = 24.182288\,,$$
 (116)

$$c_3 = \log(k5039.67) = -12.15750,$$
 (117)

$$c_4 = \log\left(\frac{2v_0 a_0^2}{10^8}\right) = -18.25177,$$
 (118)

$$f_1 = c_1 - (c_2 + c_3)/2 + \log(v_0) = 0.040060295,$$
 (119)

$$f_2 = (c_2 - c_3)/2 + c_4 - \log(v_0) = -6.0818740$$
. (120)

For $\alpha_{ABO} = 2/5$ we obtain

$$\log \frac{\gamma_6}{10^8} = \log \sigma_{ABO} + \frac{7}{10} \log \theta + \log P_{H} - 6.0967212, \tag{121}$$

and with Eq. (109) we get

$$\log \frac{\gamma_6}{10^8} = \frac{2}{5} \log C_6 + \frac{7}{10} \log \theta + \log P_{\rm H} + 8.6723475, \tag{122}$$

which is the standard formula used in Linfor3D for decades.

8.3.4 Natural line broadening

The broadening parameter γ_{rad} can be converted like this:

$$C_{\rm rad} = 10^{\log \gamma_{\rm rad} - 8.0} \tag{123}$$

For instance, $\log \gamma_{\rm rad} = 7.877$ would give $C_{\rm rad} = 0.753$. In line data formats '0' - '4', the parameter Crad is thus set to 0.753, and dlggr is set to 0.0. In line data formats '5' - '6', the parameter grlog is set to 7.887.

9 Departure Coefficients

Linfor3D is able to read departure coefficients from statistical equilibrium computations and incorporate how they affect the source function, and hence the line depression and the over all line profile in a normalised spectrum.

Until early 2022, Linfor3D was only able to read departure coefficients from the 3D statistical equilibrium code, NLTE3D. These files are formatted according to the UIO standard, and are often called xbc files.

Since then, modifications were made to Linfor3D that made it possible for it to read a new type of file – an xbc2 file. Like this file's predecessor, it is written using the UIO package, but the contents of these files differs. These files are created with the counterpart 1.5D statistical equilibrium wrapper, NLTE15D. This code is an MPI wrapper that can be adapted for most 1D statistical equilibrium codes, such as MULTI or DETAIL.

Linfor3D is capable — with some effort — of reading most formats containing departure coefficients. To add new formats, a new module should be added to nlte/ and those considerations should be added to linfor_nlte.f90. In fact linfor_nlte.f90 was designed so that one could easily add new modules that deal with NLTE departures.

The contents of the xbc and xbc2 files are now explained.

9.1 The xbc file

Add a table of the inputs

Description of entries:

Description	or er	itries:
Z-Structure:		
M10	:	First index of first horizontal dimension
N10	:	Last index of first horizontal dimension
M20	:	First index of second horizontal dimension
N20	:	Last index of second horizontal dimension
M30	:	First index of the vertical dimension
N30	:	Last index of the vertical dimension
K1SKIP	:	Skipping value of the first horizontal dimension
K2SKIP	:	Skipping value of the second horizontal dimension
K3BOT	K3BOT : Bottom boundary grid point considered for statistical equilibrium computatio	
		from NLTE3D
K3TOP	:	Top boundary grid point considered for statistical equilibrium computations from
		NLTE3D
NLEVEL	:	Number of levels stored in departure file
GSTLEV	:	Statistical weights of each level
EEVLEV	EEVLEV : Energies of each level in electron volts	
XC3	:	Vertical grid points in centimetres
TEMP	TEMP : Temperature values at every grid point of the 3D cube in Kelvin	
DNE0	: Electron number density values at every grid point of the 3D cube	
DNH0	DNH0 : Hydrogen number density values at every grid point of the 3D cube	
XBCOEF	:	Departure coefficients, $n_{\text{NLTE}}/n_{\text{LTE}}$, for each level at every grid point of the 3D
		cube

9.2 The xbc2 file 79

9.2 The xbc2 file

Description of entries:

FILETYPE : File type. Set to "xbc2" in files generated by NLTE15D

Z-Structure:

ID : Element ID ANAM : Element code ID

M10 : First index of first horizontal dimension
 N10 : Last index of first horizontal dimension
 M20 : First index of second horizontal dimension
 N20 : Last index of second horizontal dimension
 M30 : First index of the vertical dimension
 N30 : Last index of the vertical dimension

NLAM : Number of transition wavelengths stored in departure file

NLEVEL : Number of levels stored in departure file

K1SKIP : Skipping value of the first horizontal dimensionK2SKIP : Skipping value of the second horizontal dimension

ZSHIFT : First geometrical depth point over which departures are computed

ILEVEL : Corresponding departure indexes in xbcoef for each level

GSTLEV : Statistical weights of each level

EEVLEV : Energies of each level in electron volts

CLAM : Central wavelength of every transition considered in departure file

LEVIJ : Corresponding lower (first index) and upper (second index) departure indexes for

each transition

XC1 : First horizontal grid points in centimetresXC2 : Second horizontal grid points in centimetres

XC3 : Vertical grid points in centimetres

TEMP : Temperature values at every grid point of the 3D cube in Kelvin LTAUV : Monochromatic optical depth scale evaluated in base 10 logarithm LTAUR : Rosseland optical depth scale evaluated in base 10 logarithm

XBCOEF : Departure coefficients, $n_{\text{NLTE}}/n_{\text{LTE}}$, for each level at every grid point of the 3D

cube

80 10 OUTPUT FILES

10 Output files

Linfor3D generates the following output files in the Linfor3D working directory:

name		content	
linfor_3D_1.uiosave :		UIO formatted structures:	
		ABU, ATOM, CMD, CONST, INFO, LINE (see Sect. 11.1 for	
		details).	
linfor_3D_2.uiosave	:	UIO formatted structures:	
		CONTF, IMUPHI, MAPS, RESULT (see Sect. 11.2 for details).	
linfor_3D_3.uiosave	:	UIO formatted structure:	
		CONTF3D - written to file if cc3d flag is set to 1 in CMD (see	
		Sect. 11.3 for details).	
linfor_1X.uiosave :		UIO formatted structures:	
		ABU, ATOM, CMD, CONST, INFO, LINE, CONTF, IMUPHI,	
		RESULT – writen to file if run flag is set to -3 in CMD (See	
		Sect. 11.4 for details).	
linfor_timing.txt	:	Timing statistics (see Sect. 13).	
linfor_3D_1.ps	:	Postscript file: local line profiles plus average.	
linfor_3D_2.ps	:	Postscript file: line profiles for 1D reference atmospheres and	
		time-averaged 1D and 3D spectra; granulation abundance correc-	
		tion	
<pre><lhd_model_name>_150.3x3 : The 1D LHD model written as a 3X3 RHD box in UIO for</lhd_model_name></pre>		The 1D LHD model written as a 3X3 RHD box in UIO format	
<3D_model_name>_avg.3x3	:	The $\langle 3D \rangle$ model written as a 3X3 RHD box in UIO format	

The latest versions of Linfor3D (version 6.0.0 onwards) are compatible with the CVS versions of GNU data language (GDL)⁵. To make this possible, two new routines were written to replace the intrinsic IDL I/O routines, SAVE/RESTORE, previously used by Linfor3D. Both these new routines, written by A. J. Gallagher, were written to exploit the Universal Input Output (UIO) routines, which were designed by B. Freytag for handling I/O in CO⁵BOLD.

10.1 uio_save

The uio_save.pro routine is rather complex, but is nevertheless designed to work as a viable replacement to the intrinsic IDL routine, SAVE. Therefore its call is simple. At the current time, the maximum number of variables uio_save can save is 15. This can be extended when necessary by adding further variables into the routine, but for the purposes of Linfor3D it was not required.

It saves a binary file, which is commonly given the file format name uiosave. A typical call for this routine is as follows:

```
uio_save, FILE = '<filename>', variable1, variable2, variableN [, /verbose]
```

where <filename> is a string of the exact file name to be used; variable1 – variableN are the variable names to be saved.

The uio_save.pro routine can save scalars, arrays and structures. However, at present, the UIO routines do not work with IDL pointers.

The switch verbose can be used to output several useful checks to screen, including the results of an error check, which is performed by the UIO routines throughout the save procedure. This is particularly

⁵The tarball can be downloaded at http://gnudatalanguage.cvs.sourceforge.net/ and the GDL manual can be found at http://gnudatalanguage.sourceforge.net

10.1 uio_save 81

useful for error checking one's own coding. As a simple example, the uio_save routine is used to save a scaler, two arrays and a structure and then uio_restore (see Sect. 10.2) is used to open the saved file below:

```
IDL> a = 45L \& b = findgen(100) \& c = dblarr(50, 100, /nozero)
IDL> d = \{a:a, b:b, c:c\}
IDL> uio_save, FILE = 'example.uiosave', a, b, c, d, /verbose
% UIO_SAVE: Writing A vector to file
% UIO_SAVE: Write of A successful
% UIO_SAVE: Writing B vector to file
% UIO_SAVE: Write of B successful
% UIO_SAVE: Writing C vector to file
% UIO_SAVE: Write of C successful
% UIO_SAVE: Writing D structure to file
% UIO_SAVE: Write of D successful
% UIO_SAVE: Closing file and checking...
% UIO_SAVE: Data has been successfully written to file
% UIO SAVE: Write status: done
IDL> .reset ; reset the session and delete variable(s)
IDL> uio_restore, 'example.uiosave', /verbose
% UIO_RESTORE: Restoring structure A
% UIO_RESTORE: Restoring structure B
% UIO_RESTORE: Restoring structure C
% UIO_RESTORE: Restoring structure D
IDL> help
% At $MAIN$
                                 45
Α
              LONG
В
              FLOAT
                      = Array[100]
C
             DOUBLE = Array[50, 100]
D
                      = -> <Anonymous> Array[1]
              STRUCT
```

The routine calls upon the following sub-routines from the UIO database directly:

Routine		Description
uio_filedefinc.pro	:	Parameter definitions for standard file descriptors and labels
uio_uionaminc.pro	:	Common block that contains parameters for UIO initialisation routines
uio_init.pro	:	Initialisation procedure for UIO routine package.
uio_wr.pro	:	Writes scalar or array data to file.
uio_wrlabl.pro	:	Writes a label for structures or datasets.
uio_openwr.pro	:	Opens a file for writing and writes the data block header.
uio_closwr.pro	:	Closes a file after writing.

Each of these sub-routines call on several other sub-routines within the UIO routine package.

A very simple example of how to use these sub-routines to write a basic structure to file in IDL or GDL (without using uio_save.pro) is given with step-by-step annotations:

Create a structure, C, with arrays A and B:

```
IDL> a = findgen(100) & b = fltarr(20, 50) & c = {a:a, b:b}
Initialise the UIO procedures and common blocks:
IDL> @uio_filedefinc
IDL> @uio_uionaminc
IDL> uio_init, progrm = 'example_save'
```

82 10 OUTPUT FILES

Open a binary file (form = 'unformatted') called test.uiosave and use the default conversion type (conv = 'ieee_4'):

```
IDL> uio_openwr, nc, 'test.uiosave', outstr, ierr, $
IDL> form = 'unformatted', conv = 'ieee_4', prog = 'example_save'
```

Write the name of the dataset to file for the binary file header using special definition dataset_ident:

```
IDL> uio_wrlabl, nc, dataset_ident, outstr, ierr, date = 'now', $
IDL> name = 'test.uiosave'
```

Write the structure name, C, to file using special definition box_ident:

```
IDL> uio_wrlabl, nc, box_ident, outstr, ierr, date = 'now', name = 'c'
```

Begin the write of the C structure to file by declaring the box ID name as C using special definition box_id_ident:

```
IDL> uio_wr, nc, 'C', box_id_ident, name = 'C structure'
```

Write the contents of structure C to file:

```
IDL> uio_wr, nc, c.a, 'A', outstr, ierr, name = 'c.A'
IDL> uio_wr, nc, c.b, 'B', outstr, ierr, name = 'c.B'
```

Declare the end of the structure write using special definition endbox_ident:

```
IDL> uio_wrlabl, nc, endbox_ident, outstr, ierr
```

Declare the end of the dataset write using special definition enddataset_ident:

```
IDL> uio_wrlabl, nc, enddataset_ident, outstr, ierr
```

Close the file for writing

```
IDL> uio_closwr, nc, outstr, ierr
```

The uio_save.pro routine and other sub-routines within the Linfor3D routine list use this basic principle to write structures to file. A similar (though not as complex) set of procedures are used when writing arrays or scalars to file:

Create two arrays, A and B, and a scalar, C:

```
IDL> a = findgen(100) \& b = fltarr(20, 50) \& c = 55L
```

Initialise the UIO procedures and common blocks:

```
IDL> @uio_filedefinc
IDL> @uio_uionaminc
IDL> uio_init, progrm = 'example_save'
```

Open a binary file (form = 'unformatted') called test.uiosave and use the default conversion type (conv = 'ieee_4'):

```
IDL> uio_openwr, nc, 'test.uiosave', outstr, ierr, $
IDL> form = 'unformatted', conv = 'ieee_4', prog = 'example_save'
```

Write the name of the dataset to file for the binary file header using special definition dataset_ident:

```
IDL> uio_wrlabl, nc, dataset_ident, outstr, ierr, date = 'now', $
IDL> name = 'test.uiosave'
```

Write the arrays/scalars to file:

```
IDL> uio_wr, nc, a, 'A', outstr, ierr, name = 'A'
IDL> uio_wr, nc, b, 'B', outstr, ierr, name = 'B'
IDL> uio_wr, nc, c, 'C', outstr, ierr, name = 'C'
```

10.2 uio_restore 83

Declare the end of the dataset write using special definition enddataset_ident:

```
IDL> uio_wrlabl, nc, enddataset_ident, outstr, ierr
Close the file for writing
IDL> uio_closwr, nc, outstr, ierr
```

10.2 uio restore

The uio_restore.pro routine is a wrapper designed around the high level IDL function uio_dataset_rd.pro to read a UIO formatted binary or ASCII file and return the output to the call level within IDL or GDL. The call procedure for this wrapper is identical to that of the intrinsic RESTORE procedure in IDL, i.e.:

```
uio_restore, '<filename>' [, variable1, variable2, ..., variableN [, /verbose]]
```

where variables 1-N are optional, but useful where computer memory is limited. An example of its use:

```
IDL> uio_restore, 'linfor_3D_1.uiosave', /verbose
% UIO_RESTORE: Restoring structure ABU
% UIO_RESTORE: Restoring structure ATOM
% UIO_RESTORE: Restoring structure CMD
% UIO_RESTORE: Restoring structure CONST
% UIO_RESTORE: Restoring structure LINE
% UIO_RESTORE: Restoring structure INFO
IDL> help
% At $MAIN$
ABU
              STRUCT
                      = -> <Anonymous> Array[1]
ATOM
              STRUCT
                      = -> <Anonymous> Array[1]
CMD
              STRUCT
                      = -> <Anonymous> Array[1]
                      = -> <Anonymous> Array[1]
CONST
              STRUCT
INFO
              STRUCT
                      = -> <Anonymous> Array[1]
                      = -> <Anonymous> Array[1]
LINE
              STRUCT
```

The user can specify what data should be restored by adding additional command(s) to the call:

Additionally, this routine will open all CO⁵BOLD model atmospheres and is useful when a single piece of information (e.g. the model time) is required. It also means that for the first time, the user has a choice of computer languages (Fortran/IDL/GDL) to do their analysis without the need for any conversion of the output file. Further details of the routine's use can be found in the header of uio_restore.pro, which is located in the Routines sub-directory of Linfor3D.

10.3 Useful UIO information

The UIO routines allow the user to restore arrays with up to four dimensions, as modifying the UIO routines for use with Fortran so that more than four dimensions can be read is not a trivial matter. In its current form, the UIO routines will successfully save an array with more than four dimensions:

84 10 OUTPUT FILES

```
IDL> a = fltarr(10, 10, 10, 10, 10, 10, /nozero)
IDL> uio_save, file = 'example.uiosave', a, /verbose
% UIO_SAVE: Writing A vector to file
% UIO_SAVE: Write of A successful
% UIO_SAVE: Closing file and checking...
% UIO_SAVE: Data has been successfully written to file
% UIO_SAVE: Write status: done
however, the routines will not allow you to open the file afterwards:
IDL> uio_restore, 'example.uiosave'
% Attempt to subscript SARR with NDIM is out of range.
% Execution halted at: UIO_ST2DIM
  /data/Linfor/uio/uio_st2dim.pro
%
                    UIO_RD
                                     140
  /data/Linfor/uio/uio_rd.pro
%
                    UIO_STRUCT_RD
                                    333
  /data/Linfor/uio/uio_struct_rd.pro
%
                    UIO_DATASET_RD 150
  /data/Linfor/uio/uio_dataset_rd.pro
%
                    UIO_RESTORE
                                     134
  /data/Linfor/Linfor_6_0_2/Routines/uio_restore.pro
%
                     $MAIN$
```

It is shown that the restore procedure fails during the uio_st2dim.pro sub-routine call. If one only wishes to work in IDL or GDL, and has little interest in working under Fortran, there is a very simple modification that can be added to the UIO routines so that an array with more than four dimensions can be saved and successfully restored under the UIO convention. At line 69 in the routine uio_st2dim.pro, the following is seen sarr=strarr(2,4), where 4 represents the maximum number of dimensions that the UIO routines (in IDL and GDL) can load. The user can simply replace 4 with a higher number so that larger dimension arrays can be successfully restored using the UIO routines. However, it must be stressed that any alteration to this routine will only affect any file opened in IDL and GDL, not in Fortran. Indeed, any attempt to open these larger dimension arrays in Fortran will result in a read failure.

For further details on the UIO repository, as well as some other examples, please consult the CO⁵BOLD manual⁶, (Sect. 4).

⁶Downloadable at http://www.astro.uu.se/~bf/co5bold_main.html.

11.1 linfor_3D_1.uiosave 85

11 Output file structures

The binary files saved by Linfor3D contain several structures. In this section, a brief description of each array in every output structure is given.

11.1 linfor_3D_1.uiosave

The UIO formatted output file linfor_3D_1.uiosave contains the following structures:

11.1.1 ABU

The ABU structure contains information on the input file, <ABUFILE>.abu, found in the Data sub-directory of Linfor3D, where <ABUFILE> is either kiel, cifist2006 or special. It is created after the successful initialisation of the routine ionopa.pro.

Description of entries:

	-	
NAMI	:	Column 1 from abuid.
ABUI	:	Column 2 from abuid.
NAMIX	:	Column 1 from abuidx (version 6.2.2 onwards). See Sect. 7.5
ABUIX	:	Column 2 from abuidx (version 6.2.2 onwards). See Sect. 7.5

11.1.2 ATOM

The ATOM structure contains information on the input file, atom.dat, found in the Data sub-directory of Linfor3D, e.g. 1201.24 corresponds to Mg II 24, 1201.25 corresponds to Mg II 25, etc.

Description of entries:

2 cscrip.	Description of charles.			
NIONS	:	Number of species included in atom.dat		
ANAM	:	Linfor3D formatted atoms, ions and molecules. (Column 1 of atom.dat)		
WTJ	:	Corresponding baryon masses of ANAM. (Column 2 of atom.dat)		
CHIJ	:	Corresponding χ (eV) energies of ANAM (Column 3 of atom.dat)		
FISO	:	Corresponding isotope fractions of ANAM. Usually = 1.0, unless the isotopes are		
		considered. (Column 4 of atom.dat)		

This file can be edited before running Linfor3D to alter, for example, isotope fractions. However 'line.dat' should be properly formatted to reflect the changes.

11.1.3 CMD

This structure contains inputs defined by the user in the linfor_setcmd.pro routine (plus additional parameters defined by linfor_checkcmd.pro). See Sect. 7 for details.

This input structure routine can be defined and compiled in IDL/GDL before running Linfor3D by writing a BASH/TCSH script to produce this file using the native EOS procedure. This is usually done to run Linfor3D when several sessions need to be computed at the same time.

11.1.4 CONST

This structure contains a set of constants used by Linfor3D throughout the synthesis.

Description of entries:

AVMEOS : Average mass of heavy particles in EOS.

AVMION : Average mass of heavy particles in IONDIS of the model.

EPSHE : Helium number density of the model. FRACH : Hydrogen mass fraction of the model.

AVMIONX : Average mass of heavy particles in IONDIS of the spectrum.

EPSHEX : Helium number density of the spectrum. FRACHX : Hydrogen mass fraction of the spectrum.

LUTAU1 : Smallest $\log \tau_{ROSS}$ covered by sub-model (refined z-grid) – set by user in

linfor_setcmd.pro

LUTAU2 : Largest $\log \tau_{ROSS}$ covered by sub-model (refined z-grid) – set by user in

linfor_setcmd.pro

LUTAU : Array of $\log \tau_{ROSS}$ values covered by sub-model (refined z-grid) UTAU : Array of τ_{ROSS} values covered by sub-model (refined z-grid)

NUTAU : Number of points in LUTAU

LCTAU1 : Smallest $\log \tau_0$ used for RT integration – set by user in linfor_setcmd.pro LCTAU2 : Largest $\log \tau_0$ used for RT integration – set by user in linfor_setcmd.pro

LCTAU : Array of $\log \tau_0$ points used for the RT integration CTAU : Array of τ_0 points used for the RT integration

NCTAU : Number of points in LCTAU

ICG : Index number of points over which the Curve-of-Growth is computed. Default:

51. Can be set in CMD structure by user.

DLGF_CG : $\Delta \log gf$ index used to compute the Curve-of-Growth. By default this is set at 51

points between $-0.5 \le \Delta \log gf \le +1.0$, but the user can extend this if the CoG

control parameters are set in the CMD structure (see CMD.COG).

IMT : The index number of microturbulence values over which to compute the Curve-

of-Growth. If CMD.MICRO = 0 then IMT = 1.

XIMC_MTX : The range of microturbulence values over which to compute the Curve-of-Growth

using the 1D external atmosphere.

XIMC_MT1 : The range of microturbulence values over which to compute the Curve-of-Growth

using the average 3D atmosphere.

MLIST : String array of CO5BOLD full files used during the spectrum synthesis run.

NFILE : Number of model files for which the spectrum synthesis was done NDATA : Number of snapshots for which spectrum synthesis was done

WALFAO : Switch for the ALFA parameter, which is related to the upper boundary condition

(0/1). ALFA = $H_{\rm P_0}/H_{\tau_0}$ – 1, where $H_{\rm P_0}$ and H_{τ_0} is the pressure scale height and the optical depth scale height, respectively, at the upper boundary. If WALFA0 =

1, $H_{\tau_0} = f \times H_{P_0}$, where f is $-H_{\tau_0}$ (if $-10 < H_{\tau_0} < 0$).

WALFA1 : Switch for the ALFA parameter, which is related to the upper boundary condition

(0/1). ALFA = $H_{P_0}/H_{\tau_0} - 1$, where H_{P_0} and H_{τ_0} is the pressure scale height and the optical depth scale height, respectively, at the upper boundary. If WALFA1 =

1, $H_{\tau_0} = f \times H_{P_0}$, where f is $-H_{\tau_0}$ (if $H_{\tau_0} > 0$).

WALFA2 : Switch for the ALFA parameter, which is related to the upper boundary condition

(0/1). ALFA = H_{P_0}/H_{τ_0} – 1, where H_{P_0} and H_{τ_0} is the pressure scale height and the optical depth scale height, respectively, at the upper boundary. If WALFA2 =

1, $H_{\tau_0} = f \times H_{P_0}$, where f is $-H_{\tau_0}$ (if $H_{\tau_0} \le -10$).

YR1 : Plot ranges used by linfor_plot0.pro.
YR2 : Plot ranges used by linfor_plot0.pro.
YR3 : Plot ranges used by linfor_plot0.pro.
YR4 : Plot ranges used by linfor_plot0.pro.
YR5 : Plot ranges used by linfor_plot0.pro.
YR6 : Plot ranges used by linfor_plot0.pro.

11.1.5 INFO

The INFO structure contains information about the machine that Linfor3D was run on.

Description of entries:

VERSION : Version of Linfor3D used for synthesis run

DATE : Date of synthesis run

MACHINE : Machine used for synthesis run (Sometimes missing from INFO structure)

11.1.6 LINE

The LINE structure contains wavelength information and line parameters on the synthesis. This structure is typically used to reconstruct the equivalent wavelength array for use with the RESULT and IMUPHI structures.

Description of entries:

KLINE	:	Number of line calculations done by the synthesis
KTOTAL	•	Total number of spectral lines including blends

K1 : Array containing corresponding index numbers of each line or blend in kline

NBLEND : Array containing number of blends for each line synthesis

CLAM : Central wavelength, λ_0 , and continuum wavelength in Å, set in line file

DLAM : Line profile, $\Delta \lambda$, in Å computed from $\lambda_0 - \Delta \lambda$ to $\lambda_0 + \Delta \lambda$ DDLAM : Spacing of wavelength points for spectrum synthesis

WLAMO : Requested equivalent width from line file. (set to '0' unless user includes W0 in

line.dat, see Sect. 8.2.2).

LINEID : Header from the line file

LFLAG : Control string set to 'cont' (continuum synthesis) or 'line' (line synthesis) by con-

tents of line file.

MULT : Integer array identifying the multiplet number of the lines synthesised ANAM : The atomic number of lines included in the synthesis (multiplied by 100)

WTJ : Array of baryon masses for every transition considered during spectrum synthesis

(taken from atom.dat).

CHIJ : Array of χ values of lower energy in eV for every transition considered during

synthesis (taken from [cifist2006, special, kiel].abu input file).

FISO : Array of isotope fractions for every transition considered during spectrum synthe-

sis (taken from atom.dat).

CHIK Array containing χ values of upper energy in eV Central wavelength of line or blend component **ALAM GFLG** Array containing $\log gf$ values of lines synthesised Array containing $\log C_6$ values of lines synthesised C6LOG Array containing $\Delta \log C_6$ values of lines synthesised DLGC6 Difference of mean square electron orbital radii, $\Delta r^2/a_0^2$ DRRCA1 C4LOG Array containing $\log C_4$ values of lines synthesised Array containing $\Delta \log C_4$ values of lines synthesised DLGC4 Natural line broadening parameter, γ_{rad} of KLINE. GRAD8

DLGGR : Array of mean square electron orbital radii differences $(\Delta r^2/a_0^2)$

VDOP : Doppler width in units of the speed of light.

ETA0 $\eta_0 = \kappa_l/\kappa_c$. See Sect. 3.5 and Fig. 1 **AVGT** Damping parameter "a" for Voigt profile.

: Lower level index from NLTE departure files (XBC) ILOWER[3,X] IUPPER[3,X] : Upper level index from NLTE departure files (XBC)

XBCFIL3 String array containing XBC information for the 3D synthesis (set to "LTE" if no

XBC is used)

XBCFILX : String array containing XBC information for the 1D synthesis (set to "LTE" if no

XBC is used)

XCFLAG Set to 'grey': Continuum source funtion was set to wavelength-integrated Planck-

Function, $S = \sigma T^4/\pi$ and continuum opacity is set to Rosseland mean opacity,

 $\kappa_0 = \kappa_{ROSS}$. Set to 'mono': spectrum synthesis was computed as normal.

11.2 linfor_3D_2.uiosave

The UIO formatted output file linfor_3D_2.uiosave contains the following:

11.2.1 CONTF

The arrays found in this structure relate to the contribution functions calculated by Linfor3D. See Sect. 3.4 for the formal derivations.

Description	n o	f entries:
NZX	:	Array containing resultant sampling considered during external 1D model synthesis,
		redefined by lctau1 and lctau2 set in linfor_setcmd.pro
ZZX	:	Vertical geometrical ray scale for the 1D external model.
CCX	:	Continuum intensity contribution functions of the external 1D model for "vertical"
		rays on the geometrical scale, ZZX.
NZ1	:	Array containing resultant sampling considered during $\langle 3D \rangle \log \tau_{ROSS}$ synthesis, re-
		defined by lctau1 and lctau2 set in linfor_setcmd.pro
ZZ1	:	Vertical geometrical ray scale for the $\langle 3D \rangle$ model.
CC1	:	Continuum intensity contribution functions of the (3D) model for "vertical" rays on
		the geometrical scale, ZZ1.
NZ3	:	Array containing resultant sampling considered during 3D synthesis, redefined by
		<pre>lctau1 and lctau2 set in linfor_setcmd.pro</pre>
ZZ3	:	Vertical geometrical ray scale for the 3D model.
CC3	:	Continuum intensity contribution functions of the 3D model for "vertical" rays on
		the geometrical scale, ZZ3.
LTAUC	:	Array of $\log \tau_0$ (continuum optical depth) points
ITALIDY		Array of 1D log 7 (Posseland optical donth) points

Array of 1D log τ_{ROSS} (Rosseland optical depth) points LTAURX

DTRTCX : $d \log \tau_{ROSS}/d \log \tau_0$ for the external 1D model used by linfor_cf2cr.pro.

Array of $\langle 3D \rangle \log \tau_{ROSS}$ points. LTAUR1

DTRTC1 $d \log \tau_{ROSS}/d \log \tau_0$ for the $\langle 3D \rangle$ model used by linfor_cf2cr.pro.

LTAUR3 Array of 3D $\log \tau_{ROSS}$ points

 $d \log \tau_{\text{ROSS}}/d \log \tau_0$ for the 3D model used by linfor_cf2cr.pro. DTRTC3

CFCXI Array containing the 1D Continuum Intensity Contribution Function, C_I^c , evaluated

over a $\log \tau_0$ scale

CFC1I : Array containing the $\langle 3D \rangle$ Continuum Intensity Contribution Function, C_I^c , evaluated

over a $\log \tau_0$ scale

CFC3I Array containing the 3D Continuum Intensity Contribution Function, C_I^c , evaluated

over a $\log \tau_0$ scale, see Eq. (42).

CFLXI : Array containing the 1D *Line Intensity Contribution Function*, C_I^l , evaluated over a $\log \tau_0$ scale

CFL1I : Array containing the $\langle 3D \rangle$ *Line Intensity Contribution Function, C*^l_I, evaluated over a $\log \tau_0$ scale

CFL3I : Array containing the 3D *Line Intensity Contribution Function*, C_I^l , evaluated over a $\log \tau_0$ scale, see Eq. (46).

CFDXI : Array containing the 1D Line Intensity Depression Contribution Function, $\tilde{C}_I^D = C_I^c - C_I^l$, evaluated over a log τ_0 scale

CFD1I : Array containing the $\langle 3D \rangle$ Line Intensity Depression Contribution Function, $\tilde{C}_I^D = C_I^c - C_I^l$, evaluated over a log τ_0 scale

CFD3I : Array containing the 3D Line Intensity Depression Contribution Function, $\tilde{C}_I^D = C_I^c - C_I^l$, evaluated over a log τ_0 scale, see Eq. (50).

CFWXI : Array containing the 1D Equivalent Width Intensity Contribution Function, C_I^W , evaluated over a $\log \tau_0$ scale

CFW1I : Array containing the $\langle 3D \rangle$ Equivalent Width Intensity Contribution Function, C_I^W , evaluated over a $\log \tau_0$ scale

CFW3I : Array containing the 3D Equivalent Width Intensity Contribution Function, C_I^W , evaluated over a log τ_{cont} scale, see Eq. (56).

CFCXF : Array containing the 1D Continuum Flux Contribution Function, C_F^c , evaluated over a $\log \tau_0$ scale

CFC1F : Array containing the $\langle 3D \rangle$ Continuum Flux Contribution Function, C_F^c , evaluated over a $\log \tau_0$ scale

CFC3F : Array containing the 3D Continuum Flux Contribution Function, C_F^c , evaluated over a log τ_0 scale, see Eq. (44).

CFLXF : Array containing the 1D $Line\ Flux\ Contribution\ Function,\ C_F^l,$ evaluated over a $\log\tau_0$ scale

CFL1F : Array containing the $\langle 3D \rangle$ *Line Flux Contribution Function,* C_F^l , evaluated over a $\log \tau_0$ scale

CFL3F : Array containing the 3D *Line Flux Contribution Function*, C_F^l , evaluated over a log τ_0 scale, see Eq. (48).

CFDXF : Array containing the 1D *Line Flux Depression Contribution Function*, C_F^D , evaluated over a log τ_0 scale

CFD1F : Array containing the $\langle 3D \rangle$ Line Flux Depression Contribution Function, C_F^D , evaluated over a $\log \tau_0$ scale

CFD3F : Array containing the 3D *Line Flux Depression Contribution Function*, C_F^D , evaluated over a log τ_0 scale, see Eq. (53).

CFWXF : Array containing the 1D Equivalent Width Flux Contribution Function, C_F^W , evaluated over a log τ_0 scale

CFW1F : Array containing the $\langle 3D \rangle$ Equivalent Width Flux Contribution Function, C_F^W , evaluated over a log τ_0 scale

CFW3F : Array containing the 3D Equivalent Width Flux Contribution Function, C_F^W , evaluated over a log τ_{cont} scale, see Eq. (59).

CRCXI : Array containing the 1D Continuum Intensity Contribution Function, C_I^c , evaluated over a log τ_{ROSS} scale

CRC1I : Array containing the $\langle 3D \rangle$ Continuum Intensity Contribution Function, C_I^c , evaluated over a log τ_{ROSS} scale

CRC3I : Array containing the 3D Continuum Intensity Contribution Function, C_I^c , evaluated over a log τ_{ROSS} scale, see Eq. (42).

CRLXI : Array containing the 1D *Line Intensity Contribution Function*, C_I^l , evaluated over a $\log \tau_{\rm ROSS}$ scale

CRL1I : Array containing the $\langle 3D \rangle$ *Line Intensity Contribution Function, C_I^l*, evaluated over a $\log \tau_{ROSS}$ scale

Array containing the 3D Line Intensity Contribution Function, C_{I}^{l} , evaluated over a CRL3I $\log \tau_{\text{ROSS}}$ scale, see Eq. (46).

CRDXI : Array containing the 1D Line Intensity Depression Contribution Function, \tilde{C}_{I}^{D} = $C_I^c - C_I^l$, evaluated over a log τ_{ROSS} scale

Array containing the $\langle 3D \rangle$ Line Intensity Depression Contribution Function, $\tilde{C}_I^D =$ CRD1I $C_I^c - C_I^l$, evaluated over a log τ_{ROSS} scale

CRD3I Array containing the 3D Line Intensity Depression Contribution Function, \tilde{C}_{I}^{D} = $C_I^c - C_I^l$, evaluated over a log τ_{ROSS} scale, see Eq. (50).

Array containing the 1D Equivalent Width Intensity Contribution Function, C_I^W , eval-**CRWXI** uated over a $\log \tau_{ROSS}$ scale

Array containing the $\langle 3D \rangle$ Equivalent Width Intensity Contribution Function, C_I^W , CRW1I evaluated over a log τ_{ROSS} scale

CRW3I Array containing the 3D Equivalent Width Intensity Contribution Function, C_I^W , evaluated over a log τ_{ROSS} scale, see Eq. (56).

CRCXF Array containing the 1D Continuum Flux Contribution Function, C_F^c , evaluated over a $\log \tau_{ROSS}$ scale

Array containing the $\langle 3D \rangle$ Continuum Flux Contribution Function, C_F^c , evaluated CRC1F over a $\log \tau_{ROSS}$ scale

CRC3F Array containing the 3D Continuum Flux Contribution Function, C_F^c , evaluated over a log τ_{ROSS} scale, see Eq. (44).

Array containing the 1D Line Flux Contribution Function, C_F^l , evaluated over a **CRLXF** $\log au_{
m ROSS}$ scale

CRL1F Array containing the $\langle 3D \rangle$ Line Flux Contribution Function, C_E^l , evaluated over a $\log \tau_{\rm ROSS}$ scale

CRL3F Array containing the 3D Line Flux Contribution Function, C_F^l , evaluated over a $\log \tau_{\text{ROSS}}$ scale, see Eq. (48).

Array containing the 1D Line Flux Depression Contribution Function, C_E^D , evaluated **CRDXF** over a $\log \tau_{ROSS}$ scale

Array containing the $\langle 3D \rangle$ Line Flux Depression Contribution Function, C_E^D , evalu-CRD1F ated over a $\log \tau_{ROSS}$ scale

CRD3F Array containing the 3D Line Flux Depression Contribution Function, C_E^D , evaluated over a $\log \tau_{ROSS}$ scale, see Eq. (53).

CRWXF Array containing the 1D Equivalent Width Flux Contribution Function, C_E^W , evaluated over a $\log \tau_{ROSS}$ scale

CRW1F Array containing the $\langle 3D \rangle$ Equivalent Width Flux Contribution Function, C_E^W , evaluated over a $\log \tau_{ROSS}$ scale

Array containing the 3D Equivalent Width Flux Contribution Function, C_E^W , evalu-CRW3F

ated over a log τ_{ROSS} scale, see Eq. (59).

11.2.2 IMUPHI

This structure contains selective information from the RESULT structure (as well as information on ray angles). This structure is used in conjunction with several post-processing routines, such as linfor_rotate.pro.

Description of entries:

NDATA Number of snapshots for which spectrum synthesis was done KLINE Number of lines for which spectrum synthesis was done

Total number of wavelength and flux points in calculated in the synthesis NLAMX

NMUPHI Number of μ and ϕ angles used in the synthesis

MODELIDX	:	Name of the external 1D model atmosphere		
MODELID3	:	String array containing the name of snapshot, the x and y sampling and snapshot time in seconds		
MODELID1	:	String array containing the name of average model snapshot and snapshot time in seconds		
DV3	:	Array containing a velocity-spaced wavelengths, $\left(\frac{\lambda-\lambda_0}{\lambda_0}\right)c_0$		
MU	:	Array containing ray inclination angles, $\mu = \cos \theta$		
PHI	:	Array containing azimuthal angles, ϕ		
XMU	:	An extended array of inclination angles, conformal with NMUPHI dimension of		
		other arrays – allows for a simple way to perform the flux integration; $\int I3\mu d\mu =$		
		$\sum (I3 * XMU * WTS)$		
XPHI	:	An extended array of azimuthal angles, conformal with NMUPHI dimension of		
		other arrays – allows for a simple way to perform the flux integration; $\int I3\phi d\phi =$		
		$\sum (I3 * XPHI * WTS)$		
WTS	:	Weightings used for μ and ϕ angle quadratures		
I1	:	Array of (3D) fluxes evaluated over NMUPHI angles: [NLAMX, NMUPHI,		
		NDATA, KLINE]		
D1	:	Array of (3D) line depression fluxes evaluated over NMUPHI angles: [NLAMX, NMUPHI, NDATA, KLINE]		
I3	:	Array of 3D fluxes evaluated over NMUPHI angles: [NLAMX, NMUPHI, NDATA,		
		KLINE]		
D3	:	Array of 3D line depression fluxes evaluated over NMUPHI angles: [NLAMX,		
		NMUPHI, NDATA, KLINE]		
IX	:	Array of 1D fluxes evaluated over NMUPHI angles: [NLAMX, NMUPHI, NDATA,		
		KLINE]		
DX	:	Array of 1D line depression fluxes evaluated over NMUPHI angles: [NLAMX		
		NMUPHI, NDATA, KLINE]		

11.2.3 MAPS

The output file linfor_3D_2.uiosave contains a structure MAPS. An example of this structure is:

**	Structure	<83027f4>, 11	tags, length=11289820,	data	length=11289820,	refs=1:
	NX	LONG	140			
	NY	LONG	140			
	NDATA	INT	12			
	KLINE	INT	1			
	NLAM	LONG	11			
	MODELID	STRING	Array[12]			
	MU0	FLOAT	1.00000			
	PHI0	FLOAT	0.00000			
	CLAM	FLOAT	3966.34			
	LINEID	STRING	Array[1]			
	DV3	FLOAT	Array[11]			
	ICLAM0	FLOAT	Array[140, 140, 12]			
	ICLAM2	FLOAT	Array[140, 140, 11,	1, 12]		

Depending on the value of the control parameter maps_flag (see Sect. 7.3), there might be a tag named ICLAM1

ICLAM1 FLOAT Array[140, 140, 12, 1]

instead of ICLAM2 or even both might be missing if maps_flag = 0.

Description of entries:

nx, ny : x,y dimensions of the 2D images

ndata : number of models for which spectrum synthesis was donekline : number of lines for which spectrum synthesis was done

clam : central continuum wavelength for all maps

modelid : model identifier (0:ndata-1)
lineid : line identifier (0:kline-1)

ICLAMO : continuum intensity maps for all models (at clam),

dimensions: nx, ny

(see Sect. 8)

ICLAM1 : emergent intensity maps for all models and lines,

including line absorption at clam (window center);

dimensions: nx, ny, ndata, kline;
only present if maps_flag = 1

(see Sect. 8)

ICLAM2 : emergent intensity maps for all models and lines,

including line absorption at all wavelengths within the wavelength window

of width $2 \cdot dlam$ around the central wavelength clam: $\lambda_i = clam - dlam + i \cdot ddlam$, where clam = alam + dclam,

alam is the wavelength of the main blend component as defined in line.dat;

dimensions: nx, ny, nlam, kline, ndata;

only present if $maps_flag = 2$

(see Sect. 8)

W3LAM : equivalent width maps for all models and lines

Note:

- Intensities are given in units of $[erg cm^{-2} s^{-1} sr^{-1} Å^{-1}]$.
- The file formerly called "linfor_3D.idlsave" was renamed to "linfor_3D_1.idlsave".

Note that the maps include foreshortening effects. A model with a quadratic cross section becomes a rectangle when viewed off-center.

If ntheta≠ 0, the flux spectrum is computed as before, and the intensity maps show the vertical view, as before.

Keyword view added to plotting routine linfor_plot3. If given, the intensity and equivalent width maps show the foreshortened view.

11.2.4 **RESULT**

This structure contains all results from the radiative transfer done by Linfor3D, as well as some other useful information.

Description of entries:

NDATA : Number of snapshots for which spectrum synthesis was done
 KLINE : Number of lines for which spectrum synthesis was done
 KTOTAL : The total number of spectral lines including blends

NLAMX : Total number of wavelength and flux points in calculated in the synthesis

MU0 : Scalar containing first μ angle PHI0 : Scalar containing first ϕ angle

STRMU0 : String of MU0

MODELIDX : Name of the LHD model atmosphere

MODELID3 : String array containing the name of snapshot, the x and y sampling and snapshot

time in seconds

MODELID1 : String array containing the name of average model snapshot and snapshot time in

seconds

GRIDID : String array containing the sampling size of the synthesis

LINEID : String array containing the headers in the line file

LFLAG : Control string set to 'cont' (continuum synthesis) or 'line' (line synthesis) by con-

tents of line file.

VFACX : The x-component of the hydrodynamical velocity field of the 2D/3D models is

multiplied by this factor. Set in CMD.

VFACY : The y-component of the hydrodynamical velocity field of the 2D/3D models is

multiplied by this factor. Set in CMD.

VFACZ : The z-component of the hydrodynamical velocity field of the 2D/3D models is

multiplied by this factor. Set in CMD.

NL3 : Number of wavelength and flux points used for every line synthesised

DV3 : Array containing a velocity-spaced wavelengths

XIMICX : Array containing the microturbulences of the 1D synthesis
 XIMIC1 : Array containing the microturbulences of the ⟨3D⟩ synthesis
 XIMIC3 : Array containing the microturbulences of the 3D synthesis

GFLGOX : If the user sets an equivalent width 'WO' (stored in LINE.WLAMO) in the line file

(see Sects. 8.2.2 & 8.2.3) then this array will contain the resulting $\log gf$ value(s) necessary to compute the line or blend of that set strength from the given external

1D model atmosphere.

GFLG01 : If the user sets an equivalent width value in the line file (see Sects. 8.2.2 & 8.2.3)

then this array will contain the resulting $\log gf$ value(s) necessary to compute the

line or blend of that set strength from the $\langle 3D \rangle$ model atmosphere.

FX : Structure containing arrays of 1D fluxes fluxes (F) and intensities (I)

DX : Structure containing arrays of 1D line depression fluxes (F) and intensities (I) WX : Structure containing arrays of 1D equivalent widths for the absolute line depres-

sion (D) and intensity (I)

F1 : Structure containing arrays of (3D) fluxes fluxes (F) and intensities (I)

D1 : Structure containing arrays of ⟨3D⟩ line depression fluxes (F) and intensities (I)
 W1 : Structure containing arrays of ⟨3D⟩ equivalent widths for the absolute line depression

sion (D) and intensity (I)

F3 : Structure containing arrays of 3D fluxes fluxes (F) and intensities (I)

D3 : Structure containing arrays of 3D line depression fluxes (F) and intensities (I) W3 : Structure containing arrays of 3D equivalent widths for the absolute line depres-

sion (D) and intensity (I)

AC1 : Structure containing arrays of (3D) abundance corrections required to replicate

the equivalent 3D profiles for absolute line depression (D) and intensity (I)

ACX : Structure containing arrays of 1D abundance corrections required to replicate the

equivalent 3D profiles for absolute line depression (D) and intensity (I)

FCG1 : Contains the (3D) continuum intensity (I) and continuum flux (F). They are con-

stant, not changing with $\log qf$ or the line along the CoG.

WCG1 : Structure containing arrays of (3D) Curve-of-Growth equivalent width fluxes (F)

and intensities (I).

FCGX : Contains the external 1D continuum intensity (I) and continuum flux (F). They

are constant, not changing with $\log qf$ or the line along the CoG.

WCGX : Structure containing arrays of Curve-of-Growth equivalent width fluxes (F) and intensities (I) computed from the 1D external model atmospheres.

11.3 linfor_3D_3.uiosave

The UIO formatted output file linfor_3D_3.uiosave contains the following:

11.3.1 **CONTF3D**

The CONTF structure contains information relating to the 3D contribution functions. When the cc3d flag is set, this structure is saved and contains extended information from that stored in the CONTF structure.

Description of entries:

NX3 : Resultant sampling points considered in synthesis, redefined by nx_skip set in linfor_setcmd.pro

NY3 : Resultant sampling points considered in synthesis, redefined by nx_skip set in

NY3 : Resultant sampling points considered in synthesis, redefined by ny_skip set in linfor_setcmd.pro

NZ3 : Array containing resultant sampling considered during synthesis, redefined by lctau1 and lctau2 set in linfor_setcmd.pro

ZZ3 : Vertical geometrical ray scale for the 3D model.

CC3 : Continuum intensity contribution functions of the 3D model on the geometrical scale, ZZ3.

11.4 linfor_1X.uiosave

This is a special output file, only written when Linfor3D performs synthesis under run_flag = -3. While most of the structures given in this file contain most of the same sub-structures and arrays that are found in linfor_3D_1.uiosave and linfor_3D_2.uiosave, the MAPS structure is not written and several sub-structures or arrays pertaining to the 3D or $\langle 3D \rangle$ synthesis. The only exception to this is the inclusion of the I3, D3, I1 and D1 arrays in the structure IMUPHI. This is so that certain post-synthesis routines, such as linfor_rotate.pro, still work without error. While these arrays exist, they only contain zeros.

12 Plotting output

In this section we briefly present examples of how you can manipulate the output detailed in Sect. 11 and plot them in IDL or GDL.

12.1 Plotting the synthesis

Linfor3D has several routines that can quickly process the raw data from the uiosaves output after the synthesis has completed. The first of these is linfor_rotate.pro. The call procedure for this routine is:

```
A = linfor_rotate(IMUPHI, itime, kline, vsini [, /normalize, modid = modid])
```

where IMUPHI is the imuphi structure found in linfor_3D_2.uiosave; itime is the snapshot number (0-N-1) or the averaged time (-1); i_kline is the kline index; and vsini is the $v \sin i$ value of star in km s⁻¹. The switch, /normalize, is used to normalise the spectrum and keyword modid is used to select which synthesis to process $(1 = 1D, 2 = \langle 3D \rangle)$ and 3 = 3D.

The other useful routine is linfor_convol.pro. This routine is used to convolve a Gaussian profile with the synthesis. The call for this routine is:

```
linfor_convol, lambda, input_flux, output_flux, xi
```

where lambda is a 1D array containing the wavelength points; input_flux is a 1D array containing the corresponding unbroadened flux; output_flux is the 1D output array containing the broadened flux; and xi is a float/double scalar turbulence parameter in absolute units $-\xi = \sigma \sqrt{2} = \text{FWHM}/(\sigma \sqrt{2})$. Using both these routines will produce an array of flux points that can be plotted. The following step-by-step procedures can be used to successfully load and plot the synthesis.

After loading the two uiosaves, linfor_3D_1.uiosave and linfor_3D_2.uiosave, create a wavelength array for the number of lines synthesised (kline) and data points (nlamx):

```
IDL> lambda = fltarr(imuphi.nlamx, imuphi.kline)

IDL> for i = 0, imuphi.kline - 1 do begin &$

IDL> lambda[*, i] = (line.clam - line.dlam[i]) + $

IDL> findgen(1. + 2. * line.dlam[i] / line.ddlam[i]) * line.ddlam[i] &$

IDL> endfor

Create the corresponding flux arrays for the 3D, \langle 3D \rangle and 1D fluxes:

IDL> flux3 = fltarr(imuphi.nlamx, imuphi.kline) ; 3D flux array

IDL> flux1 = fltarr(imuphi.nlamx, imuphi.kline) ; <3D> flux array

IDL> fluxx = fltarr(imuphi.nlamx, imuphi.kline) ; 1D flux array

Set a v sin i value. For this example, we will set v sin i = 5 km/s:
```

```
IDL> vsini = 5.
```

Use the routine linfor_rotate.pro to produce the normalised flux for the 3D, \langle 3D \rangle (averaged over all snapshots):

```
IDL> for i = 0, imuphi.kline - 1 do begin &$
IDL> flux3[*, i] = linfor_rotate(imuphi, -1, i, vsini, /normalize, modid = 3) &$
IDL> flux1[*, i] = linfor_rotate(imuphi, -1, i, vsini, /normalize, modid = 2) &$
IDL> fluxx[*, i] = linfor_rotate(imuphi, -1, i, vsini, /normalize, modid = 1) &$
IDL> endfor
```

From this procedure, the 3D, $\langle 3D \rangle$ and 1D synthesis can be plotted in IDL or GDL using the plot command. However, if one wishes to include an instrumental broadening term in the synthesis, the

96 12 PLOTTING OUTPUT

following demonstrates how to do this using the linfor_convol.pro.

Set up three new arrays for the convolved 3D, \langle 3D \rangle and 1D flux profiles:

```
IDL> f3_inst = make_array([size(flux3, /dimensions)])
IDL> f1_inst = make_array([size(flux1, /dimensions)])
IDL> fx_inst = make_array([size(fluxx, /dimensions)])
```

Set the instrumental broadening in km/s:

```
IDL> v inst = 10.0
```

and the speed of light in km/s:

```
IDL> c = 2.9979246D+5
```

Calculate the equivalent instrumental broadening value in absolute units:

```
IDL> inst = (v_inst * line.clam / c) / (2 * sqrt(alog(2)))
```

Using linfor_convol.pro to broaden flux3, flux1 and fluxx with a Gaussian of FWHM v_inst:

```
IDL> for i = 0, imuphi.kline - 1 do begin &$
IDL> linfor_convol, lambda[*, i], flux3[*, i], f3_inst[*, i], inst &$
IDL> linfor_convol, lambda[*, i], flux1[*, i], f1_inst[*, i], inst &$
IDL> linfor_convol, lambda[*, i], fluxx[*, i], fx_inst[*, i], inst &$
IDL> endfor
```

12.2 Plotting contribution functions

Linfor3D also contains information on contribution functions. This section explains how to plot one type of contribution function, the equivalent width contribution functions (crw[3,1,X]f see Sect. 11.2.1), which are derived by integrating the line-depth contribution functions (Magain 1986, A&A, 135) over all wavelength points considered by Linfor3D during the synthesis run. In this example, we will average over all snapshots computed during the synthesis as well. The crw[3,1,X]f has the following dimensions: [CONST.NCTAU, RESULT.NDATA, RESULT.KLINE]. Create the arrays and set some variables:

IDL> crw3f[*, j] = ln10 * avg(contf.crw3f[*, *, j], 1) * tauc / avg(f3[*, j]) &\$ IDL> crw1f[*, j] = ln10 * avg(contf.crw1f[*, *, j], 1) * tauc / avg(f1[*, j]) &\$

```
IDL> crw3f = fltarr(const.nctau, result.kline)
IDL> crw1f = fltarr(const.nctau, result.kline)
IDL> crwxf = fltarr(const.nctau, result.kline)
         = fltarr(result.nlamx, result.kline)
IDL> f3
IDL> f1 = fltarr(result.nlamx, result.kline)
IDL> fx = fltarr(result.nlamx, result.kline)
IDL> ltauc = contf.ltauc
IDL> tauc = 10.0^ltauc
IDL > ln10 = alog(10)
Fill the flux arrays:
IDL> for i = 0, result.kline - 1 do begin &$
IDL> f3[*, i] = avg(result.f3.f[*, *, i], 1) &
IDL> f1[*, i] = avg(result.f1.f[*, *, i], 1) &
IDL> fx[*, i] = result.fx.f[*, i] &
IDL> endfor
Convert the contribution functions from Eq. (59) to a \log \tau_{ROSS} scale:
```

IDL> for j = 0, result.kline - 1 do begin &\$

```
IDL> crwxf[*, j] = ln10 * avg(contf.crwxf[*, *, j], 1) * tauc / avg(fx[*, j]) &$ IDL> endfor
```

Finally, plot the contribution functions:

```
IDL> plot, ltauc,crwxf[*, 0], linestyle = 5
IDL> oplot, ltauc,crw3f[*, 0]
IDL> oplot, ltauc,crw1f[*, 0], linestyle = 4
```

The conversion just performed means that the plot depicts $dW/d \log \tau_{ROSS}$ (in mÅ) as a function of $\log \tau_{ROSS}$, where W is the equivalent width and $\log \tau_{ROSS}$ is the logarithm of the optical depth evaluated over a Rosseland scale. As such, $\int (dW/d \log \tau_{ROSS}) d \log \tau_{ROSS}$ reproduces the equivalent width in mÅ.

12.3 Plotting the Curve-of-Growth

The Curve-of-Growth (CoG) information is contained in three arrays within the RESULT, ABU and CONST structures CONST.dlgf_cg, RESULT.wcgx, RESULT.wcg1, ABU.abui and ABU.abuix, see Sect. 11 for information. The wcgx and wcg1 are four dimensional arrays formatted according to the number of snapshots considered during the spectrum synthesis, RESULT.ndata; the number of lines synthesised, RESULT/LINE.kline; the number of microturbulences to be evaluated, CONST.imt; and the number of index points to compute the CoG, CMD/CONST.icg.

To plot a traditional Curve-of-Growth (i.e. log(W) as a function of A(X)) the correct abundance should be known. This is usually given in ABU. abui (or ABU. abuix in version 6.2.2 onwards), if their corresponding abundance files are edited and input into Linfor3D. Otherwise, this value should be input manually. In this example, we assume the former is accurate. First, let's define A(X), in this case we will work with lithium, A(Li):

```
IDL> N = 3
IDL> logA = abu.abui[N] + const.dlgf_cg
```

Next, let's define $\log(W)$, and average out the snapshot information:

```
IDL> logWX = fltarr(line.kline, const.imt, const.icg)
IDL> logW1 = fltarr(line.kline, const.imt, const.icg)
IDL> for k = 0, line.kline - 1 do begin &$
IDL> for i = 0, const.imt - 1 do begin &$
IDL> logWX[k, i, *] = alog10(avg(result.wcgx.f[*, k, i, *], 0)) &$
IDL> logW1[k, i, *] = alog10(avg(result.wcg1.f[*, k, i, *], 0)) &$
IDL> endfor &$
IDL> endfor
```

Finally, let's plot the first line for all microturbulence values:

```
IDL> plot, logA, logWX[0, 0, *]
IDL> for i = 1, const.imt - 1 do $
IDL> oplot, logA, logWX[0, i, *], linestyle = i
IDL> for i = 0, const.imt - 1 do $
IDL> oplot, logA, logW1[0, i, *], linestyle = i, color = 255
```

98 13 TIMING STATISTICS

13 Timing statistics

At the end of a run of Linfor3D timing statistics are presented which are also saved to the file linfor_timing.txt in the current working directory. The file will look like this:

```
TIMING STATISTICS
Routine linfor_find_ff.....(total ): 10.36 s ( 0.00 %)
Restoring structure FF.....
                                :
                                         ---
0.02\%
                                                   0.00 %)
                                        24.30 s (
                          (0):
                                                    0.00 %)
                          (
                                1):
                                         5.17 s (
                                                    0.00 %)
                          (
                                2):
                                          5.57 s (
                                                    0.00 %)
                          (
                                          5.05 s (
                               3):
                                                    0.00 %)
                          (
                              4) :
                                          5.74 s (
                                                    0.00 %)
                              5):
6):
7):
8):
                          (
                                          5.76 s (
                                                    0.00 %)
                          (
                                         4.87 s (
                                                    0.00 %)
                                          5.14 s (
                          (
                                                    0.00 %)
                                          5.41 s (
                          (
                                                    0.00 %)
                               9):
                          (
                                          5.13 s (
                                                    0.00 %)
                          (
                              10) :
                                          5.41 s (
                                                    0.00 %)
                                                    0.00 %)
                                          5.85 s (
                          (
                              11) :
                                          5.05 s (
                                                    0.00 %)
                              12) :
                          (
                              13) :
                                          4.76 s (
                                                    0.00 %)
                          (
                              14) :
                                         5.06 s (
                                                    0.00\%
                          (
                              15):
                                         4.74 s (
                                                    0.00 %)
                              16):
                                          4.72 s (
                                                    0.00 %)
                               17) :
                                          5.10 s (
                          (
                                                    0.00 %)
                                         4.93 s (
                              18) :
                                                    0.00 %)
                          (
                              19) :
                                         4.91 s (
                                                    0.00 %)
Routine linfor_ionopa_3d.....(total ):
                                        736.01 s (
                                                    0.12 %)
                                         36.80 s (
                         (average):
                                                    0.01 %)
                                0):
                                         38.12 s (
                          (
                                                    0.01 %)
                          (
                                         37.65 s (
                                1) :
                                                    0.01 %)
                          (
                                2):
                                          35.50 s (
                                                    0.01 %)
                          (
                                3):
                                         40.03 s (
                                                    0.01 %)
                          (
                               4) :
                                         38.03 s (
                                                    0.01 %)
                          (
                               5):
                                         38.49 s (
                                                    0.01 %)
                          (
                               6):
                                         37.90 s (
                                                    0.01 %)
                          (
                               7):
                                         36.29 s (
                                                    0.01 %)
                               8):
                                         36.88 s (
                          (
                                                    0.01 %)
                          (
                               9):
                                         37.29 s (
                                                    0.01 %)
                          (
                               10):
                                          37.04 s
                                                (
                                                    0.01 %)
                          (
                               11) :
                                         37.64 s (
                                                    0.01 %)
                              12) :
                          (
                                         36.05 s (
                                                    0.01 %)
                              13) :
                                         33.74 s (
                                                    0.01 %)
                          (
                                         35.52 s (
                                                    0.01 %)
                              14) :
                          (
                              15):
                                         35.83 s (
                                                    0.01 %)
                                         35.51 s (
                          (
                              16):
                                                    0.01 %)
                          (
                               17) :
                                          36.46 s (
                                                    0.01 %)
                             18) :
19) :
                                          36.14 s (
                                                    0.01 %)
                          (
                                         35.90 s (
                          (
                                                    0.01 %)
Saving structure FF.....
Rad. transfer for 3D model....(total ): 594678.33 s ( 97.40 % )
                                      29733.92 s ( 4.87 %)
                          (average):
                              0):
                                      31170.96 s ( 5.11 %)
```

```
1):
                                                31021.06 s (
                                                                5.08 %)
                               (
                                       2) :
                                                29445.84 s (
                                                                4.82 %)
                               (
                                       3):
                                                30393.73 s (
                                                                4.98 %)
                                                30423.26 s
                                                                4.98 %)
                               (
                                       4):
                                                           (
                                       5):
                                                29654.40 s
                                                           (
                                                                4.86 %)
                                                                4.77 %)
                               (
                                       6):
                                                29151.41 s
                                                           (
                                                                4.82 %)
                               (
                                       7):
                                                29403.00 s
                                                           (
                                                29536.25 s
                                                                4.84 %)
                                       8):
                                                           (
                               (
                                       9):
                                                29749.70 s
                                                                4.87 %)
                                                            (
                               (
                                      10):
                                                33397.79 s
                                                                5.47 %)
                                                            (
                               (
                                      11) :
                                                30029.57 s
                                                                4.92 %)
                                                            (
                                                29955.88 s
                                                                4.91 %)
                                      12) :
                               (
                                      13) :
                                                28652.31 s
                                                            (
                                                                4.69 %)
                                      14) :
                                                28731.89 s
                                                                4.71 %)
                               (
                                                           (
                                                29166.00 s
                                                                4.78 %)
                                      15):
                               (
                                                           (
                                                28685.49 s
                                                                4.70 %)
                                      16):
                                                           (
                                                28832.02 s (
                                                                4.72 %)
                                      17) :
                                      18):
                                                28688.46 s
                                                           (
                                                                4.70 %)
                                                28589.31 s
                                                                4.68 %)
                                      19) :
                                                           (
Rad. transfer for <3D> model....(total
                                        ) :
                                                14236.35 s
                                                            (
                                                                2.33 %)
                               (average):
                                                  711.82 s
                                                                0.12 %)
                                                            (
                               (
                                       0):
                                                  755.84 s
                                                           (
                                                                0.12 %)
                                                                0.12 %)
                               (
                                       1) :
                                                  716.50 s
                                                           (
                               (
                                       2):
                                                  715.40 s
                                                                0.12 %)
                               (
                                                  721.79 s
                                                                0.12 %)
                                       3):
                                                            (
                                                  717.25 s
                                                                0.12 %)
                               (
                                       4):
                                                  715.77 s
                               (
                                       5):
                                                                0.12 %)
                                                            (
                               (
                                       6):
                                                  702.42 s
                                                            (
                                                                0.12 %)
                               (
                                       7):
                                                  717.40 s
                                                           (
                                                                0.12 %)
                                                  707.86 s
                                                                0.12 %)
                               (
                                       8):
                                                           (
                                                                0.12 %)
                                       9):
                                                  703.97 s
                               (
                                                           (
                                      10):
                                                  746.35 s
                                                           (
                                                                0.12 %)
                               (
                                      11) :
                                                  707.23 s
                                                           (
                                                                0.12 %)
                                                  695.03 s
                                                                0.11 %)
                               (
                                      12) :
                                                           (
                                                  691.42 s
                                                                0.11 %)
                               (
                                      13) :
                                                            (
                               (
                                      14) :
                                                  690.57 s
                                                            (
                                                                0.11 %)
                               (
                                      15):
                                                  736.33 s
                                                           (
                                                                0.12 %)
                                                  698.71 s
                                                                0.11 %)
                               (
                                      16):
                                                           (
                                      17) :
                                                  698.63 s
                                                           (
                                                                0.11 %)
                                      18):
                                                  701.31 s
                                                                0.11 %)
                                                            (
                                      19):
                                                  696.56 s
                                                                0.11 %)
                               (
                                                            (
Rad. transfer for 1D model....(total
                                                  577.25 s
                                                                0.09 %)
                                        ) :
                                                            (
Total.....(total
                                        ) :
                                               610549.27 s
                                                           (100.00\%)
```

The file is also saved during a running Linfor3D process. Thus, time statistics are available even after aborting the process. The statistics show the system time needed for individual computation steps/routines of Linfor3D and their contribution to the total time in percent. For the case that the same operation is performed several times, e.g., doing the radiative transfer for more than one model snap shot, the total of all calls, the average time, and the duration for each individual step is given (see example above).

100 14 IONDIS

14 IONDIS

IONDIS is responsible for computing all information on requested atomic and molecular species requested in the line.dat file. As stated in Sect. 2, IONDIS is run under Fortran. In this section, we will briefly outline the considerations made by IONDIS, and a full list of the limited number of atomic and molecular species IONDIS currently takes into account.

14.1 Atoms

Linfor3D does not at present include the **complete** atomic data information used by CO⁵BOLD. Rather, a number of selected atoms are properly treated by IONDIS. Additions to IONDIS.f are welcome and will be integrated, after proper testing. However, we ask that **FULL** considerations are taken to the entire program flow of Linfor3D before submitting them to us.

At present (version 6.2.5) there are 61 atomic species considered by IONDIS. You can change the atomic abundances considered during spectrum synthesis by changing the abuid (or abuidx in versions 6.2.2 onwards) and putting your changes in special.abu. Depending on how you want to run Linfor3D (see Sect. 7.5), abuid and abuidx can be equal or different. If they are different, cifist2006.abu is treated as the model abundance file (and is loaded into abuid) and special.abu is treated as the spectrum abundance file (and is loaded into abuidx). A full list of the atoms (and ionisation states, isotopes) are given below.

Table 19: List of atomic species currently considered by IONDIS

Species	Considered	Considered
_	ionisation states	isotopes
Н	I	
Не	I, II	
Li	I, II	6, 7
Be	I, II	
C	I, II	
N	I, II	
O	I, II	
F	I, II	
Ne	I, II	
Na	I, II	
Mg	I, II	24, 25, 26
Al	I, II	
Si	I, II	
P	I, II	
S	I, II	
Cl	I, II	35, 37
Ar	I, II	
K	I, II	
Ca	I, II	
Sc	I, II	
Ti	I, II	
V	I, II	
Cr	I, II	
Mn	I, II	
Fe	I, II	
Co	I, II	

14.2 Molecules

Ni	I, II	
Cu	I, II	63, 65
Zn	I, II	
As	I, II	
Rb	I, II, III	
Sr	I, II	
Y	I, II	
Zr	I, II	
Nb	I, II	
Mo	I, II	
Ru	I, II	
Rh	I, II	
Pd	I, II	
Ag	I, II	
Ba	I, II	134, 135, 136, 137, 138
La	I, II	
Ce	I, II	
Pr	I, II	
Nd	I, II	
Sm	I, II	
Eu	I, II	
Gd	I, II	152, 154, 155, 156, 157, 158, 160
Dy	I, II	
Er	I, II	162, 164, 166, 167, 168, 170
Tm	I, II	
Yb	I, II	168, 170, 171, 172, 173, 174, 176
Lu	I, II	175, 176
Hf	I, II	
Ta	I, II	
W	I, II	
Os	I, II	
Pb	I, II	
Th	I, II	
U	I, II	

14.2 Molecules

Linfor3D also considers a *limited* number of molecules. At present they are only diatomic/bimetallic molecules. We welcome new integrations into IONDIS, and will include them into the general realise, after they are properly tested. However, we ask that **FULL** considerations are taken to the entire program flow of Linfor3D before submitting them to us.

Table 20: Small molecular network: 5 atoms, 8 molecules

	Н	С	N	О	Mg
Н	H_2	СН	NH	ОН	MgH
C	CH	C_2	CN	CO	_
N	NH	CN	_	_	_
0	OH	CO	_	_	_
Mg	MgH	_	_	_	_

102 14 IONDIS

	Н	Li	С	N	О	F	Mg	Ti	Cr	Fe
Н	H_2	LiH	СН	NH	ОН	FH	MgH		CrH	FeH
Li	LiH	_	_	_	LiO	_		_		
C	CH	_	C_2	CN	CO	_		_		
N	NH	_	CN	_	_	_		_		
0	OH	LiO	CO	_	_	_		TiO		
F	FH	_	_	_	_	_		_	_	_
Mg	MgH	_	_	_	_	_		_		
Ti	_	_	_	_	TiO	_		_		
Cr	CrH	_	_	_	_	_		_	_	_
Fe	FeH		_	_	_	_				

Table 21: Large molecular network: 10 atoms, 14 molecules

14.2.1 Some definitions

 N_i Total number density of nuclei of element i, including nuclei bound in diatomic molecules

 \tilde{N}_i Number density of nuclei of element i not bound in diatomic molecules

 $\tilde{N}_{i,0}$ Number density of neutral nuclei of element i not bound in diatomic molecules

 $N_{i,k}$ Total number density of diatomic molecules made up of one

nucleus of element i, and one nucleus of element k

 N_e Total electron number density.

 $N_{\text{Kern}} = \sum_{i} N_{i}$ Total number density of nuclei of all elements, diatomic molecules counting as 2 nuclei

 $P_e = N_e kT$ Electron pressure.

 $f_i = N_i/N_{\text{Kern}}$ Fractional abundance of element *i* (constant)

 $x_i = \tilde{N}_i / N_{\text{Kern}}$ Fractional abundance of free nuclei of element *i*.

 $x_i = f_i = const.$ for elements not involved in molecule formation $(i \notin \{i_{mol}\})$.

For elements forming molecules $(i \in \{i_{mol}\})$, x_i is the variable to be iterated.

 $x_{i,k} = N_{i,k}/N_{\text{Kern}}$ Fractional abundance of molecule (i, k).

 $x_e = N_e/N_{\rm Kern}$ Fractional abundance of free electrons (iterated quantity).

14.2.2 Equations

The Saha equation provides the relation between $\tilde{N}_{i,0}$ and \tilde{N}_{i} :

$$\tilde{N}_{i,0} = S_{i,0} \, \tilde{N}_i \tag{124}$$

where the Saha factor $S_{i,0}$ depends on temperature and electron pressure (and on the ionization potentials and the partition functions of the different ionization stages).

Molecule partial pressures are given by the relation

$$P_{i,k} = \frac{P_i P_k}{K_{i,k}} \tag{125}$$

where $K_{i,k}$ is the dissociation constant for the (neutral) diatomic molecule (ik), composed of one nucleus of elements i and k each. P_i and P_k are the partial pressures of the **neutral** atoms of elements i and k, respectively. Since P = N kT, molecule densities are

$$N_{i,k} = \frac{kT \, \tilde{N}_{i,0} \, \tilde{N}_{k,0}}{K_{i,k}} \tag{126}$$

14.2 Molecules 103

Dividing by N_{Kern} , we obtain the fractional molecule abundance

$$x_{i,k} = \frac{N_{i,k}}{N_{\text{Kern}}} = \frac{N_{\text{Kern}} kT \ x_i S_{i,0} \ x_k S_{k,0}}{K_{i,k}} = \frac{P_e \ x_i S_{i,0} \ x_k S_{k,0}}{K_{i,k} \ x_e} = D_{i,k} \frac{x_i \ x_k}{x_e}$$
(127)

where we have defined

$$D_{i,k} = P_e \, \frac{S_{i,0} \, S_{k,0}}{K_{i,k}}.\tag{128}$$

We note that $D_{i,k}$ depends only on T and P_e , but not on absolute number densities, and hence is constant during the iteration.

For all elements i involved in molecule formation, $i \in \{i_{mol}\}$, we have the following conservation equation

$$f_i = x_i + \sum_k x_{i,k} (1 + \delta_{i,k})$$
 (129)

or

$$x_i + \sum_{k} D_{i,k} \frac{x_i \ x_k}{x_e} (1 + \delta_{i,k}) = f_i$$
 (130)

where $\delta_{i,k}$ is the Kronecker symbol, accounting for the correct counting of atoms in molecules with two identical components.

The electron density is given by

$$N_e = \sum_{i} \tilde{N}_i \overline{Z}_i = \sum_{i \in \{i_{mol}\}} \tilde{N}_i \overline{Z}_i + \sum_{i \notin \{i_{mol}\}} \tilde{N}_i \overline{Z}_i$$
 (131)

where the mean degree of ionization of element i, \overline{Z}_i is defined as

$$\overline{Z}_{i} = \sum_{j=-1,3} j \, \tilde{N}_{i,j} / \sum_{j=-1,3} \tilde{N}_{i,j} = \frac{1}{\tilde{N}_{i}} \sum_{j=-1,3} j \, \tilde{N}_{i,j} = \sum_{j=-1,3} j \, \tilde{S}_{i,j} = \sum_{j=1,3} j \, \tilde{S}_{i,j} - \tilde{S}_{i,-1}.$$
 (132)

Here index j runs over the 4 ionization stages j = 0...3 of element i. For elements forming negative ions, the sum includes the negative ion, j = -1. For such elements, \overline{Z}_i may become negative! Note that \overline{Z}_i depends only on T and P_e , but not on the degree of molecule formation. Dividing Eq.(131) by N_{Kern} , we obtain

$$x_e = \sum_i x_i \overline{Z}_i = \sum_{i \in \{i_{mol}\}} x_i \overline{Z}_i + \sum_{i \notin \{i_{mol}\}} x_i \overline{Z}_i$$
(133)

Defining

$$f_e = \sum_{i \neq \{i,\dots,j\}} x_i \, \overline{Z}_i = \sum_{i \neq \{i,\dots,j\}} f_i \, \overline{Z}_i = const. \tag{134}$$

we have finally

$$x_e - \sum_{i \in \{i_{mol}\}} x_i \, \overline{Z}_i = f_e \tag{135}$$

Combining Eq.(130) and (135), we have the following vector equation

$$\vec{X} + \vec{F}(\vec{X}) = \vec{R} \tag{136}$$

where

$$\vec{X} = \{x_1, x_2, \dots x_N, x_e\},\tag{137}$$

is the vector of unknown number fractions, and

$$\vec{R} = \{f_1, f_2, \dots f_N, f_e\} = const.,$$
 (138)

is the known (constant) right-hand side. N is the number of chemical elements included in the molecular network. Equation (136) is a system of N + 1 nonlinear algebraic equations which can be solved for \vec{X} by Newton-Raphson iteration.

104 14 IONDIS

The first step it to find a suitable starting vector for the iteration, \vec{X}_0 . This is done as described below. The correction $\delta \vec{X}$ giving the next improved estimate of \vec{X} is computed as follows. Assume after n iterations we have

$$\vec{X}_n + \vec{F}(\vec{X}_n) = \vec{R}_n. \tag{139}$$

Then we require that

$$\vec{X}_n + \delta \vec{X} + \vec{F}(\vec{X}_n + \delta \vec{X}) = \vec{R} \tag{140}$$

or

$$\vec{X}_n + \delta \vec{X} + \vec{F}(\vec{X}_n) + \mathcal{J} \cdot \delta \vec{X} = \vec{R}, \tag{141}$$

hence

$$(\mathcal{J}+1)\cdot\delta\vec{X}=\vec{R}-\vec{R_n}. \tag{142}$$

The elements of the Jacobian $\mathcal J$ are defined as

$$\mathcal{J}_{i,j} = \frac{\partial F_i}{\partial x_j}.\tag{143}$$

Since we know that

$$F_i(\vec{X}) = \frac{x_i}{x_e} \sum_{k=1,N} D_{i,k} x_k (1 + \delta_{i,k}) \quad \text{for } i = 1, N$$
 (144)

and

$$F_{N+1}(\vec{X}) = -\sum_{i=1,N} x_i \, \overline{Z}_i,\tag{145}$$

we can readily evaluate $\mathcal{J}_{i,j}$.

We find from Eqs.(144) and (145)

$$\mathcal{J}_{i,j} = \frac{\partial F_i}{\partial x_i} = D_{i,j} \frac{x_i}{x_e} \quad \text{for } i = 1, N \text{ and } i \neq j$$
 (146)

$$\mathcal{J}_{i,i} = \frac{\partial F_i}{\partial x_i} = \sum_{k \neq i} D_{i,k} \frac{x_k}{x_e} + 4 D_{i,i} \frac{x_i}{x_e} = \sum_{k = 1, N} D_{i,k} \frac{x_k}{x_e} + 3 D_{i,i} \frac{x_i}{x_e} \quad \text{for } i = 1, N$$
 (147)

$$\mathcal{J}_{i,N+1} = \frac{\partial F_i}{\partial x_e} = -\frac{x_i}{x_e^2} \sum_{k=1,N} D_{i,k} x_k (1 + \delta_{i,k}) \quad \text{for } i = 1, N$$
(148)

$$\mathcal{J}_{N+1,j} = \frac{\partial F_{N+1}}{\partial x_j} = -\overline{Z}_i \quad \text{for } j = 1, N$$
 (149)

$$\mathcal{J}_{N+1,N+1} = \frac{\partial F_{N+1}}{\partial x_e} = 0 \tag{150}$$

With this information, we can solve Eq.(142) for $\delta \vec{X}$, and obtain the next estimate

$$\vec{X}_{n+1} = \vec{X}_n + \delta \vec{X} \tag{151}$$

Once the iteration has converged, the molecule densities can be computed from Eq.(127).

14.2.3 Criterion for convergence

The criterion for convergence is currently:

$$|x_i^{(n+1)} - x_i^{(n)}| \le 1 \cdot 10^{-4} f_i \tag{152}$$

and

$$|x_i^{(n)} + \sum_{k} D_{i,k} \frac{x_i^{(n)} x_k^{(n)}}{x_e^{(n)}} (1 + \delta_{i,k}) - f_i| \le 1 \cdot 10^{-4} f_i$$
(153)

for all elements i. The maximum number of iterations is 15.

14.2 Molecules 105

14.2.4 Initial guess

The initial concentrations of free atoms and ions of elements involved in molecule formation, x_i , are computed as follows.

First, we assume that no molecules are formed and so the initial x_i are set to f_i ,

$$x_{i,0} = f_i \tag{154}$$

for all elements. From this, the electron fraction x_e is computed as

$$x_{e,0} = \max \left\{ x_{e,\min}, \ f_e + \sum_{i \in \{i_{mol}\}} x_i \, \overline{Z}_i \right\},$$
 (155)

where $x_{e,\min} = 1 \cdot 10^{-10}$. Using this value for x_e , we compute the molecule concentrations $x_{i,k}$ according to Eq.(127). If the resulting

$$x_{i,k} \le 1 \cdot 10^{-5} \min\{x_i, x_k\},$$
 (156)

the formation of this molecule is considered negligible, and no correction of x_i , x_k and $x_{i,k}$ is necessary. If

$$1 \cdot 10^{-5} \min\{x_i, x_k\} < x_{i,k} \le \min\{x_i, x_k\},\tag{157}$$

molecule formation is no longer negligible, but also not exhaustive. In this case, the molecule concentrations must be iterated, but the initial guesses for $x_{i,k}$, x_i and x_k need not be changed. Finally, if

$$x_{i,k} > \min\left\{x_i, x_k\right\},\tag{158}$$

then molecule formation is exhaustive, and the initial guesses for $x_{i,k}$, x_i and x_k are changed. We compute x_i and x_k as the equilibrium values that would result if only this particular molecule was present. If the molecule consists of two atoms of the same element, the condition is (see Eq.(130))

$$2D_{i,i}\frac{x_i^2}{x_i} + x_i - f_i = 0 ag{159}$$

which has the solution

$$x_{i,0} = \frac{2 f_i}{1 + \sqrt{1 + 8 f_i D_{i,i} / x_{e,0}}}.$$
 (160)

If the molecule consists of two different atoms, we have two conditions, namely (see Eq.(130))

$$D_{i,k} \frac{x_i x_k}{x_e} + x_i - f_i = 0$$

$$D_{i,k} \frac{x_i x_k}{x_e} + x_k - f_k = 0$$
(161)

From this we see that

$$x_i - x_k = f_i - f_k \equiv \Delta. \tag{162}$$

Then we have

$$D_{i,k} \frac{(x_k + \Delta) x_k}{x_a} + x_k - f_k = 0$$
 (163)

or

$$\frac{D_{i,k}}{x_e} x_k^2 + \left(1 + \Delta \frac{D_{i,k}}{x_e}\right) x_k - f_k = 0.$$
 (164)

Assuming that $f_i \ge f_k$, and hence $\Delta \ge 0$, the solution for x_k can be written as

$$x_{k,0} = \frac{2 f_k}{(1 + \Delta D_{i,k}/x_{e,0}) + \sqrt{(1 + \Delta D_{i,k}/x_{e,0})^2 + 4 f_i D_{i,k}/x_{e,0}}},$$
(165)

106 14 IONDIS

and for x_i we simply have

$$x_{i,0} = x_{k,0} + \Delta. {166}$$

For each molecule, the values of $x_{i,0}$, $x_{k,0}$ obtained for the current molecule from Eq.(160) or Eqns.(165), (166) are compared to the previous values $x_{i,0}^{(n)}$, $x_{k,0}^{(n)}$ (obtained from the same conditions for a previous molecule). The new estimate of is then set to the minimum of previous and current estimate

$$x_{i,0}^{(n+1)} = \min \left\{ x_{i,0}, \ x_{i,0}^{(n)} \right\}$$

$$x_{k,0}^{(n+1)} = \min \left\{ x_{k,0}, \ x_{k,0}^{(n)} \right\}$$
(167)

The initial guess for the current molecule is then computed as

$$x_{i,k} = D_{i,k} \frac{x_{i,0}^{(n+1)} x_{k,0}^{(n+1)}}{x_{e,0}}.$$
(168)

For simplicity (and stability), the initial guess for the electron fraction is not updated when changing the initial guesses x_i for the elements involved in molecule formation.

14.2.5 Variable names

DAB	$D_{i,k}/x_e$	
DF00	$\vec{R} - \vec{R}_n$	
FRACEL	x_e	
FRACEL0	f_e	
FRACEL1	$\sum_{i \in \{i_{mol}\}}$.	$f_i \overline{Z}_i$
FRACI	f_i	
FRACJ	$x_i S_{i,j}$	(atoms and ions, $j = 1 \dots 4$)
	$x_{i,k}$	(molecules)
FREEI	x_i	
NATMOL	N	
PNUC	$N_{\rm Kern} k T$	$T = P_e/x_e$
RIJSUM	F_{i}	
SAHAJ	$S_{i,j}$	(atoms and ions, $j = 1 \dots 4$)
	$K_{i,k}$	(molecules)
ZEFF	$rac{K_{i,k}}{Z_i}$	

15 ionopa

Linfor3D computes opacities, level populations, pressures and densities with the IDL/GDL routine ionopa.pro. It has evolved quite considerably over many versions of Linfor3D and this routine has now been replaced by ionopa2.pro. It calls on the IONDIS library described above, is fairly easy to use, and can be used separately from Linfor3D to compute various properties for 1D and 3D models. As this routine has developed, the call sequence has changed significantly. The call sequence described here is correct for the last version of ionopa.pro, which was running as of Linfor3D version 5.1.5 and deprecated after version 6.1.1:

```
ionopa, temp, pin, alam, pout, densnc, okappa, osigma, pgas=pgas, $
    namj=namj, fracj=fracj, zeta=zeta, init=init, $
    dm=dm, dalpha=dalpha, avm=avm, ehe=ehe, abupath=abupath, $
    nami=nami, abui=abui
```

A brief description of all entries into ionopa are now listed.

15.1	temp		
	description	:	gas temperature(s) in kelvins
	input/output	:	input
	required	:	always
	type	:	float
	properties	:	scalar, 1D array, 2D array, 3D array: must have same dimensions as pin
	values	:	5777, [4000:6000]

15.2	pin		
	description	:	input pressure(s) in dyn/cm ²
	input/output	:	input
	required	:	always
	type	:	float
	properties	:	scalar, 1D array, 2D array, 3D array: must have same dimensions as temp
	values	:	1e4, [1e4:5e4]

15.3	alam		
	description	:	wavelength range in angstroms
	input/output	:	input
	required	:	always
	type	:	float
	properties	:	scalar, 1D array
	values	:	5500, [4000:6000]

108 15 IONOPA

15.4 pout

description : output pressure(s) in dyn/cm²

input/output : output required : always type : float

properties : same dimensions as temp and pin, i.e. scalar, 1D, 2D, 3D array

values : 1e4, [1e4:5e4]

15.5 densnc

description : number densities of atomic nuclei

input/output : output required : always type : float

properties : same dimensions as temp and pin, i.e. scalar, 1D, 2D, 3D array

values : 1.0e14

15.6 okappa

description : true absorption continuum opacity in cm² per nucleus

input/output : output required : always type : float

properties : [N temp, N alam] if alam is an array, otherwise [N temp]

values : 1.0e-22

15.7 osigma

description : scattering continuum opacity in cm² per nucleus

input/output : output required : always type : float

properties : [N temp, N alam] if alam is an array, otherwise [N temp]

values : 1.0e-27

Continuum opacity is given by okappa + osigma

15.8 pgas

description : toggles pin and pout

input/output : input
required : optional
type : switch
properties : scalar
values : 0 or 1

pgas = 0: ionopa assumes that pin is the electron pressure and pout is the gas pressure (default).

pgas = 1: ionopa assumes that pin is the gas pressure and pout is the electron pressure (usual case).

15.9 namj

description : input ion identifier

input/output : input required : always type : float

properties : scalar, 1D array

values : 2600.0, [2600.0, 2601.0, 5600.0]

15.10 fracj

description : fractional number density n_i / densnc, where n_i is the number density

of namj elements in ionization stage j

input/output : output required : optional type : float

properties : [N temp, N namj] if namj is an array, otherwise [N temp]

values : 3.30554e-12

15.11 zeta

description : number densities such that $zeta = fracj / U_j(T)$

input/output : output required : optional type : float

properties : [N temp, N namj] if namj is an array, otherwise [N temp]

values : 4.53707e-10

110 15 IONOPA

15.12 init

description : type of abu file

input/output : input

required : for initialisation only

type : integer properties : scalar values : 1, 2, 3

init = 1: abu file is defined as kiel.abu

init = 2: abu file is defined as cifist2006.abu

init = 3: abu file is defined as special.abu

15.13 dm

description : gas metallicity

input/output : input

required : for initialisation only

type : float properties : scalar values : -1.0, 0.0

15.14 dalpha

description : gas alpha enhancement, $[\alpha/Fe]$

input/output : input

required : for initialisation only

type : float properties : scalar values : 0.0, 0.4

Affects elements O, Ne, Mg, Si, S, Ar, Ca and Ti

15.15 avm

description : average mass of nucleus for chemical composition defined by init

input/output : output required : optional type : float properties : scalar

values : 2.08985e-24

15.20 Example 111

15.16 ehe

description : ratio of helium to hydrogen number densities

input/output : output
required : optional
type : float
properties : scalar
values : 0.0851139

15.17 abupath

description : path to directory where abu file defined by init can be found

input/output : input required : always type : string properties : scalar

values : getenv('LINFOR3D_ABU')

15.18 nami

description : ion identifier from abu file defined by init

input/output : output required : optional type : integer properties : 1D array

values : 100, 200, 300, ..., 9200

15.19 abui

description : corresponding abundances of ions in nami

input/output : output required : optional type : float properties : 1D array

values : 12.0000, 10.9300, 1.10000, ..., -0.470000

15.20 Example

In order to use ionopa it first needs to be initialised. The initialisation tells ionopa properties of the model such as its metallicity, chemical abundances, alpha enhancement. An example of the initialisation may look as follows:

```
IDL> ionopa, 0.0, 0.0, 0.0, pout, densnc, okappa, osigma, init = 2, $
IDL> dm = -1.0, dalpha = 0.4, abupath = getenv('LINFOR3D_ABU'), $
IDL> nami = nami, abui = abui, ehe = ehe, avm = avm0
```

112 15 IONOPA

% Compiled module: IONOPA.

Not all of those options are required, however. Once initialised, ionopa can be executed. The input parameters should be used instead of the 0.0 values used to initialise.

```
IDL> ionopa, Tin, Pin, alam, pele, densnc, okappa, osigma, /pgas, $
IDL> namj = ions, fracj = fracj, zeta = zeta
```

16 ionopa2

ionopa2 replaced ionopa in Linfor3D version 6.2.0 onwards. The inputs and outputs of ionopa2 are fairly similar to ionopa, but there are certain differences:

A brief description of all entries into ionopa2 are now listed.

description : gas temperature(s) in kelvins input/output : input required : always type : float properties : scalar, 1D array, 2D array, 3D array: must have same dimensions as qin values : 5777, [4000:6000]

16.2	qin		
	description	:	input quantities in cgs units
	input/output	:	input
	required	:	always
	type	:	float
	properties	:	scalar, 1D array, 2D array, 3D array: must have same dimensions as temp
	values	:	1e4, [1e4:5e4]

16.3	alam		
	description	:	wavelength range in angstroms
	input/output	:	input
	required	:	always
	type	:	float
	properties	:	scalar, 1D array
	values	:	5500, [4000:6000]

```
description : electron pressure(s) in dyn/cm² input/output : output required : always type : float properties : same dimensions as temp and qin, i.e. scalar, 1D, 2D, 3D array values : 1e4, [1e4:5e4]
```

114 16 IONOPA2

description : gas pressure(s) in dyn/cm² input/output : output required : always type : float properties : same dimensions as temp and qin, i.e. scalar, 1D, 2D, 3D array values : 1e4, [1e4:5e4]

description : number densities of atomic nuclei
input/output : output
required : always
type : float
properties : same dimensions as temp and qin, i.e. scalar, 1D, 2D, 3D array
values : 1.0e14

description : true absorption continuum opacity in cm² per nucleus input/output : output required : always type : float properties : [N temp, N alam] if alam is an array, otherwise [N temp] values : 1.0e-22

description : scattering continuum opacity in cm² per nucleus input/output : output required : always type : float properties : [N temp, N alam] if alam is an array, otherwise [N temp] values : 1.0e-27

Continuum opacity is given by okappa + osigma

16.9 qflg

description : toggles qin input/output : input

required : optional. Set to 0 if ignored

type : switch
properties : scalar
values : 0, 1, 2, 3

qflg = 0: qin is defined as the electron pressure, P_e (default).

qflg = 1: qin is defined as the gas pressure (usual case), P_{gas} .

qflg = 2: qin is defined as $P_{gas} - P_e$.

qflg = 3: qin is defined as continuum opacity per unit volume, densnc * (okappa + osigma).

16.10 namj

description : input ion identifier

input/output : input required : always type : float

properties : scalar, 1D array

values : 2600.0, [2600.0, 2601.0, 5600.0]

16.11 fracj

description : fractional number density n_i / densnc, where n_i is the number density

of namj elements in ionization stage j

input/output : output required : optional type : float

properties : [N temp, N namj] if namj is an array, otherwise [N temp]

values : 3.30554e-12

16.12 zeta

description : number densities such that $zeta = fracj / U_i(T)$

input/output : output required : optional type : float

properties : [N temp, N namj] if namj is an array, otherwise [N temp]

values : 4.53707e-10

116 16 IONOPA2

16.13 init

description : type of abu file

input/output : input

required : on initalisation or when more than one abu file has been initialised

type : integer properties : scalar

values : -3, -2, -1, 1, 2, 3

init = 1: abu file is defined as kiel.abu

init = 2: abu file is defined as cifist2006.abu

init = 3: abu file is defined as special.abu

init = -1: initialise composition 1 from memory*.

init = -2: initialise composition 2 from memory*.

init = -3: initialise composition 3 from memory*.

*Used if ionopa2 has been initialised for more than one abu file.

16.14 dm

description : gas metallicity

input/output : input

required : for initialisation only

type : float properties : scalar values : -1.0, 0.0

16.15 dalpha

description : gas alpha enhancement, $[\alpha/Fe]$

input/output : input

required : for initialisation only

type : float properties : scalar values : 0.0, 0.4

Affects elements O, Ne, Mg, Si, S, Ar, Ca and Ti

16.16 avm

description : average mass of nucleus for chemical composition defined by init

input/output : output required : optional type : float properties : scalar

values : 2.08985e-24

16.17 ehe

description : ratio of helium to hydrogen number densities

input/output : output
required : optional
type : float
properties : scalar
values : 0.0851139

16.18 abupath

description : path to directory where abu file defined by init can be found

input/output : input required : always type : string properties : scalar

values : getenv('LINFOR3D_ABU')

16.19 nami

description : ion identifier from abu file defined by init

input/output : output required : optional type : integer properties : 1D array

values : 100, 200, 300, ..., 9200

16.20 abui

description : corresponding abundances of ions in nami

input/output : output required : optional type : float properties : 1D array

values : 12.0000, 10.9300, 1.10000, ..., -0.470000

118 16 IONOPA2

16.21 Example

Like ionopa, ionopa2 must first be initialised.

```
IDL> ionopa2, 0.0, 0.0, 0.0, pele, pgas, densnc, okappa, osigma, $
IDL> init = 2, dm = 0.0, dalpha = 0.0, avm=avm, ehe=ehe, $
IDL> abupath=getenv('LINFOR3D_ABU'), nami=nami, abui=abui
% Compiled module: IONOPA2.
```

Now that ionopa2 has been initialised, it can be executed.

```
IDL> ionopa2, tin, qin, alam, pele, pgas, densnc, okappa, osigma, $
IDL> qflg = 1, namj = ions, fracj = fracj, zeta = zeta
```

Additionally, ionopa2 can be initialised more than once for more than one abu file.

```
IDL> %---- initialise 1 ----
IDL> ionopa2, 0.0, 0.0, 0.0, pele, pgas, densnc, okappa, osigma, $
IDL> init = 2, dm = 0.0, dalpha = 0.0, avm = avm2, ehe = ehe2, $
IDL> abupath = getenv('LINFOR3D_ABU'), nami = nami2, abui = abui2
% Compiled module: IONOPA2.

IDL> %---- initialise 2 ----
IDL> ionopa2, 0.0, 0.0, 0.0, pele, pgas, densnc, okappa, osigma, $
IDL> init = 3, dm = 0.0, dalpha = 0.0, avm = avm3, ehe = ehe3, $
IDL> abupath = getenv('LINFOR3D_ABU'), nami = nami3, abui = abui3
```

Once it has been initialised for the requested parameters it can be executed without being reinitialised.

```
IDL> %---- execute 1 ----
IDL> ionopa2, tin2, qin2, alam, pele2, pgas2, densnc2, okappa2, osigma2, $
IDL> qflg = 1, namj=[ions], fracj = fracj2, zeta = zeta2, init = -2
IDL> %---- execute 2 ----
IDL> ionopa2, tin3, qin3, alam, pele3, pgas3, densnc3, okappa3, osigma3, $
IDL> qflg = 1, namj=[ions], fracj = fracj3, zeta = zeta3, init = -3
```

Note the use of init in these instances. As ionopa2 has been initialised for more than one abu file, init should be included from its memory.

Index

α -elements, 41, 106, 112	blends, 69
Linfor3D	data format: -1, 60
Change log, 6	data format: 0, 61
history, 3	data format: 1, 62
·	data format: 2, 64
Curve-of-Growth	data format: 3, 65
CMD, 49, 52, 53	data format: 4, 66
computations, 52	data format: 5, 67
CONST, 83	data format: 5, 67
RESULT, 90	
1120 021, 70	data format: 7, 68
F90	line.dat, 60
compilers, 17	Natural broadening, 73
Files, 31	Quadratic stark broadening, 70
install, 6	Van der Waals broadening, 71
Intel	26.
	Main program
ifort, 3, 5	Calling sequence, 27, 30
MPI, 6, 17	run_flag, 36
oneAPI, 6	Donom at an imput
version issues, 6	Parameter input
MPI, 7	execution flags, 36
Curve-of-Growth, 21	linfor_setcmd, 34
Description, 17	Plotting
Domain decomposition, 17	contribution functions, 92
DoRT, 19	Curve-of-Growth, 93
IONDIS, 17	synthesis, 91
subdomain, 17–19	D W W W W W W W W W W
	Radiative transfer, 8
GDL	Contribution functions, 11
cmake, 25	Continuum flux, 11
Eigan3, 25	Continuum Intensity, 11
installing GDL, 25	Equivalent width, 13
running, 25, 26	Line depression, 12
	Line flux, 12
HPC, 17	Line Intensity, 12
	Grey test case, 13
IDL	Transfer equation
Files, 28	the continuum intensity, 8
Structures	the line depression, 10
Common block, 28	the line intensity, 9
flow field, 29	the line intensity,
ray system, 29	Statistical equilibrium
spectrum, 29	NLTE15D, 74
IONDIS	NLTE3D, 74
atomic information, 96	Structures
ionopa, 103	ABU, 81
ionopa2, 109	ATOM, 81
treatment of molecules, 97	CMD, 81
deather of molecules, //	CONST, 81
Line Data	CONTF, 84
ABO van der Waals broadening, 72	
	CONTF3D, 90

120 INDEX

```
IMUPHI, 86
INFO, 83
LINE, 83
MAPS, 87
RESULT, 88

UIO
definition, 5
library, 28, 31
UIO information, 79
uiorestore, 79
uiosave, 36, 76, 78, 81, 84, 87, 90, 91
```